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Cross Sections from Proton-Deuteron Data

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Polarized Proton-Neutron Total Cross Sections from Proton-Deuteron Data

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POLARIZED PROTON-NEUTRON TOTAL CROSS SECTIONS FROM

PROTON-DEUTERON DATA

by

G. Alberi, M. Bleszynski, T. Jaroszewicz, and S. Santos

ABSTRACT

Simple expressions are derived for the polarized proton-deuteron total cross sections. Possibilities of extraction of the polarized proton-neutron cross sections from the proton-deuteron data are discussed.

Because recent measurements of the proton-proton (p-p) total cross section with polarized beam and target were successful,^{1,2} and similar experiments are planned for the proton-deuteron case,³ we are examining corrections to be applied to the raw deuteron data to obtain the polarized proton-neutron (p-n) total cross sections. These corrections were studied in detail for the unpolarized total cross sections^{4,5} and were verified⁶ using data obtained with neutron beams.

The general expression for the elastic-scattering amplitude of two particles of spin 1/2 and spin 1 can be obtained using parity and time reversal invariance.

$$\hat{\mathbf{F}} = \hat{\mathbf{F}}^{\mathbf{O}} + \hat{\vec{\mathbf{F}}} \cdot \vec{\sigma} , \qquad (1)$$

where 🕚

$$\hat{\mathbf{F}}^{\mathbf{O}} = \mathbf{F}_{\mathbf{O}}^{\mathbf{O}} + \mathbf{F}_{\mathbf{y}} \ \hat{\mathbf{J}}_{\mathbf{y}}^{\mathbf{O}} + \mathbf{F}_{\mathbf{xx}}^{\mathbf{O}} \ \hat{\mathbf{Q}}_{\mathbf{xx}} + \mathbf{F}_{\mathbf{yy}}^{\mathbf{O}} \ \hat{\mathbf{Q}}_{\mathbf{yy}} ,$$

$$\hat{\mathbf{F}}^{\mathbf{x}} = \mathbf{F}_{\mathbf{x}}^{\mathbf{x}} \ \hat{\mathbf{J}}_{\mathbf{x}} + \mathbf{F}_{\mathbf{xy}}^{\mathbf{x}} \ \hat{\mathbf{Q}}_{\mathbf{xy}} ,$$

$$\hat{\mathbf{F}}^{\mathbf{y}} = \mathbf{F}_{\mathbf{y}}^{\mathbf{y}} + \mathbf{F}_{\mathbf{y}}^{\mathbf{y}} \ \hat{\mathbf{J}}_{\mathbf{y}} + \mathbf{F}_{\mathbf{xx}}^{\mathbf{y}} \ \hat{\mathbf{Q}}_{\mathbf{xx}} + \mathbf{F}_{\mathbf{yy}}^{\mathbf{y}} \ \hat{\mathbf{Q}}_{\mathbf{yy}} ,$$
(2)
$$\hat{\mathbf{F}}^{\mathbf{y}} = \mathbf{F}_{\mathbf{O}}^{\mathbf{y}} + \mathbf{F}_{\mathbf{y}}^{\mathbf{y}} \ \hat{\mathbf{J}}_{\mathbf{y}} + \mathbf{F}_{\mathbf{xx}}^{\mathbf{y}} \ \hat{\mathbf{Q}}_{\mathbf{xx}} + \mathbf{F}_{\mathbf{yy}}^{\mathbf{y}} \ \hat{\mathbf{Q}}_{\mathbf{yy}} ,$$
and

$$\hat{\mathbf{F}}^{\mathbf{X}} = \mathbf{F}_{\mathbf{X}}^{\mathbf{X}} \hat{\mathbf{J}}_{\mathbf{X}} + \mathbf{F}_{\mathbf{Y}\mathbf{X}}^{\mathbf{X}} \hat{\mathbf{Q}}_{\mathbf{Y}\mathbf{X}}$$

Here $\vec{\sigma}$ is the Pauli matrix of the external proton, \vec{J} is the deuteron spin, and $\hat{Q}_{ik} = 1/2 \left(\hat{J}_i \hat{J}_k + \hat{J}_k \hat{J}_i \right) - 2/3 \delta_{ik}$.

As usual, the amplitude is defined in the deuteron brick-wall system' and z is along the average of the proton momentum, whereas y is orthogonal to the scattering plane. Actually, in the forward direction the brick-wall system coincides with the laboratory system and is along the incident-beam direction.

The missing terms change sign for either parity or time reversal transformation, where the x-, y-, and z-directions are defined in terms of the ingoing and outgoing momenta. Other terms are missing because they are not independent. When both beam and target are polarized along the i-th axis, the initial density matrix is

$$\hat{P} = \left(\frac{1}{2} - \frac{1}{2} \hat{P}_{i} \hat{\sigma}_{i}\right) \left(\frac{1}{3} + \frac{1}{2} D_{i} \hat{J}_{i} + \frac{1}{2} A_{i} \hat{Q}_{ii}\right) , \qquad (3)$$

where P_i and D_i are the proton and deuteron polarizations along i, and A_i is the alignment of the deuteron defined⁷ as

$$P_{i} = Tr \left[\hat{\rho} \sigma_{i} \right], D_{i} = Tr \left[\hat{\rho} \hat{J}_{i} \right], A_{i} = 3 Tr \left[\hat{Q}_{ii} \hat{\rho} \right] .$$

The total cross section for the general density matrix, Eq. (3), becomes

$$\sigma_{\rm T} = \frac{1}{\sqrt{\lambda (S, M^2, m^2)}} \, \operatorname{Im} \left(\operatorname{Tr} \left[\hat{F} \hat{\rho} \right] \right), \tag{4}$$

where m and M are the nucleon and deuteron masses, s is the square of total c.m. energies of the system, and λ is a variable of relativistic kinematics.⁸ From Ref. 6 for the transverse (y-direction) polarizations of the beam and the target,

$$\sigma_{\rm T} = \frac{1}{\sqrt{\lambda \, ({\rm s}, {\rm M}^2, {\rm m}^2)}} \, {\rm Im} \left\{ \left(F_{\rm O}^{\rm O} + {\rm P}_{\rm Y} {\rm D}_{\rm Y} {\rm F}_{\rm Y}^{\rm Y} + \frac{1}{6} \, {\rm A}_{\rm Y} \, {\rm F}_{\rm XX}^{\rm O} + \frac{1}{6} \, {\rm A}_{\rm Y} {\rm P}_{\rm Y} {\rm F}_{\rm YY}^{\rm Y} \right) \right\} , \qquad (5a)$$

and for the longitudinal (z-direction) polarizations,

$$\sigma_{\rm T} = \frac{1}{\sqrt{\lambda (s, M^2, m^2)}} \quad \operatorname{Im} \left\{ \left(F_{\rm O}^{\rm O} + P_{\rm Z} D_{\rm Z} F_{\rm Z}^{\rm Z} - \frac{1}{6} A_{\rm Z} \left(F_{\rm XX}^{\rm O} + F_{\rm YY}^{\rm O} \right) \right) \right\} \quad . \tag{5b}$$

For a purely vector-polarized deuteron target and a polarized beam, we can measure the $\Delta\sigma_{\rm L}$ and $\Delta\sigma_{\rm T}$ (Ref. 9) for proton-deuteron scattering, which are easily expressed as functions of the proton-deuteron spin amplitudes. These amplitudes are linear and bilinear expressions of the elementary c.m.* nucleon-nucleon amlitudes, in exactly the same way as the nonflip amplitude $F_{\rm O}^{\rm O}$ (Ref. 4,5). Since the deuteron is larger in size than the nucleon, we can calculate the double-scattering integral^{4,5} neglecting the t-dependence of the amplitudes. The result reads

$$\Delta \sigma_{\rm L} = \sigma \ (z) - \sigma \ (z) = \frac{4}{\sqrt{\lambda} (S_r M^2, m^2)} \ \operatorname{Im} \left(F_{\rm Z}^2 \right)$$

$$= \frac{4}{\sqrt{\lambda} (S_r M^2, m^2)} \left\{ \operatorname{Im} \left[\varepsilon_{\rm p}(0) + \varepsilon_{\rm n}(0) \right] \ \left(1 - \frac{3}{2} P_{\rm D} \right) \right\}$$

$$+ \operatorname{Re} \left[2 \varepsilon_{\rm p}(0) \alpha_{\rm n}(0) + 2 \varepsilon_{\rm n}(0) \alpha_{\rm p}(0) - \alpha_{\rm p}(0) \varepsilon_{\rm p}(0) - \alpha_{\rm n}(0) \varepsilon_{\rm n}(0) \right]$$

$$\times \operatorname{R}_{\rm L} \frac{1}{4\pi\sqrt{\lambda} (S_r m^2, m^2)} \right\} , \qquad (6a)$$

and

$$\Delta \sigma_{\rm T} = \sigma (\uparrow\uparrow) - \sigma (\downarrow\uparrow) = \frac{4}{\sqrt{\lambda (s, M^2, m^2)}} \operatorname{Im} \left(F_{\rm Y}^{\rm Y} \right)$$

$$= \frac{4}{\sqrt{\lambda (s, M^2, m^2)}} \left\{ \operatorname{Im} \left[\beta_{\rm p}(0) + \beta_{\rm n}(0) \right] \left(1 - \frac{3}{2} P_{\rm D} \right) + \operatorname{Re} \left[2\beta_{\rm p}(0) \alpha_{\rm n}(0) + \beta_{\rm n}(0) \alpha_{\rm p}(0) - \alpha_{\rm p}(0) \varepsilon_{\rm p}(0) - \alpha_{\rm n}(0) \alpha_{\rm n}(0) \right] \right\}$$

$$\times R_{\rm T} \frac{1}{4\pi\sqrt{\lambda (s, m^2, m^2)}} , \qquad (6b)$$

*Actually the nucleon-nucleon spin amplitudes are calculated in the deuteron brick-wall frame, and they are connected to the c.m. amplitudes by a Wigner rotation.¹⁰ However, in the forward direction the Wigner angle is zero.

where α , ϵ , and β are nucleon-nucleon c.m. amplitudes in the notation of Goldberger and Watson.¹¹ They are normalized as Im α (O) = $\sqrt{\lambda} (s, m^2, m^2) \sigma_T$; s is the square c.m. energy of the nucleon-nucleon system and p and n refer to protonneutron scattering. The quantities R_L , R_T , and P_D can be expressed through the radial wave functions of the deuteron.¹²,13

$$R_{\rm L} = \int_{\infty}^{\infty} dr r^{-2} \left[u(r) + \frac{1}{\sqrt{2}} w(r) \right]^{2} ,$$

$$R_{\rm T} = \int_{\infty}^{\infty} dr r^{-2} \left[u(r) + \frac{1}{\sqrt{2}} w(r) \right] \left[u(r) - \sqrt{2} w(r) \right] , \qquad (7)$$

$$P_{\rm D} = \int_{\infty}^{\infty} dr w^{2}(r) \qquad (D\text{-wave percentage}) .$$

The values of R_L and R_T are given in Table I for three wave functions of the deuteron.^{12,13} Also given are the D-wave percentages and the corresponding values for $\langle 1/r^2 \rangle$ for the S-wave renormalized to 1.

To take into account the t-dependence of the amplitudes, $R_{\rm L}$ and $R_{\rm T}$ must be expressed as q^2 integrals of the deuteron form factors.

$$R_{\rm L} = \frac{1}{2\pi} \int d^2 q \ \epsilon (q^2) \alpha^{-1} (0) \alpha (q^2) \alpha^{-1} (0) \times \int_0^\infty dr \left[u^2 (r) - \frac{w^2 (r)}{2} \right] j_0 (qr) + \sqrt{\frac{1}{2}} \left[u(r) w(r) + \frac{w^2 (r)}{2} \right] j_2 (qr)$$

TABLE I
VALUES OF R_L, R_T, AND
$$\langle \frac{1}{r^2} \rangle$$
 FOR THREE DEUTERON WAVE FUNCTIONS

•••	$R_{L}(fm^{-2})$	$R_{T}(fm^{-2})$	P ^a D	$\langle \frac{1}{r^2} \rangle^{b} (\text{fm}^{-2})$
McGee ¹³	0.449	0.164	0.069	0.300
Reid S.C. ¹²	0.382	0.157	0.064	0.265
Reid H.C. ¹²	0.374	0.148	0.065	0.256

^aD-wave percentage.

b For the S-wave renormalized to 1. and

$$R_{\rm T} = \frac{1}{2\pi} \int d^2 q \quad \beta(q^2) \beta^{-1}(0) \alpha(q^2) \alpha^{-1}(0) \cdot \int_0^{\infty} dr \left[u^2(r) - \frac{w^2(r)}{2} \right] j_0(qr) - \frac{1}{2\sqrt{2}} \left[u(r)w(r) + \frac{w^2(r)}{2} \right] j_2(qr) .$$

If we neglect higher order terms in the spin correlation expression C_{NN} in protonproton scattering and we assume that the α and β phases do not vary with q^2 , then q^2 behavior of $\beta(q^2)$ is related directly to the q^2 behavior of C_{NN} . For example,

$$\beta (q^2) / \beta (O) = \alpha (q^2) / \alpha (O) \cdot C_{NN} (q^2) / C_{NN} (O)$$

Although rough, this approximation allows qualitative testing of the R_L and R_T sensitivities to the amplitude t-dependence.

The results for 2 GeV/c are given in Table II; the same dependence as for $\beta(q^2)$ is assumed for $\epsilon(q^2).^{14}$

We can express Eqs. (6a) and (6b) in terms of the polarized cross section³ for the elementary processes p-p and p-n through relations of the type 2 Im $\left[\epsilon_{p}(0)\right] = \sqrt{\lambda(s,m^{2},m^{2})} \cdot \Delta\sigma_{L}(0)$. The result¹⁵ looks very similar to the famous Glauber formula⁴ for the total cross sections. To do this however, we must neglect the real parts of the double-spin-flip amplitudes that could be large compared with the imaginary parts. Actually, the real parts were calculated by Grein and Kroll¹⁶ using dispersion relations and the ratio $\rho_{\beta}^{p} = \left\{ \text{Re}[\beta_{p}(0)] \right\} / \left\{ \text{Im}[\beta_{p}(0)] \right\} \sim 6$ around 5 GeV/c. For a ratio $\rho_{\alpha}^{p} = \left\{ \text{Re}[\alpha_{p}(0)] \right\} / \left\{ \text{Im}[\alpha_{p}(0)] \right\} \sim -0.3$, we find that the Galuber formula is multiplied by a factor of 2.8. The ρ_{β}^{n} value, not known, must be calculated from the $\Delta\sigma_{T}$ values for proton-neutron scattering, extracted from deuteron data with the assumption $\rho_{\beta}^{n} = \rho_{\beta}^{p}$.

TABLE II

 $R_{T_{\rm c}}$ and $R_{\rm p}$ values calculated with t-dependence of the nucleon-nucleon amplitudes

	$R_1(fm^{-2})$	$R_{T}(fm^{-2})$
McGee ¹³	0.401	0.115
Reid S.C. ¹²	0.307	0.111
Reid H.C. ¹²	0.306	0.105

It also can be determined self-consistently, for instance with an iterative procedure.

Although our discussion has been on pure Glauber theory, there are non-eikonal¹⁷ corrections at intermediate energies ($P_{Lab} \leq 2$ GeV/c). The effect of these corrections is to modify the expressions for R_L and R_T [Eq. (6)] as follows.¹⁸

$$R_{\rm L}^{\prime} = \eta_{\rm L} R_{\rm L} = 1 + \int_{\infty}^{\infty} dr \ r^{-2} \left[u(r) + \frac{w(r)}{\sqrt{2}} \right] e^{2ikr} \left[\frac{w(r)}{\sqrt{2}} \left[2 - 3 j_{\rm O}(kr) \right] e^{-ikr} - u(r) \right]$$

and

$$R_{\rm T}^{\prime} = \eta_{\rm T} R_{\rm T} = 1 + \int_{\infty}^{\infty} dr \ r^{-2} \left[u(r) + \frac{w(r)}{\sqrt{2}} \right] e^{2ikr} \left\{ \frac{w(r)}{2\sqrt{2}} \left[1 + 3 \ j_{\rm O}(kr) \ e^{-ikr} \right] - u(r) \right\} .$$

The $\eta_{\rm L}$ and $\eta_{\rm T}$ values, listed in Table III for the incident-proton laboratory momenta, were calculated with the Reid soft-core wave function.¹² The non-eikonal corrections change mainly the R_T and R_L phases (by $\sim 5\%$ for P_{Lab} = 1.7 GeV/c).

It was suggested recently that around 1.3 GeV the intermediate production of Δ_{33} plays an important role in proton-nucleus elastic scattering, but for a π^- exchange model for Δ production, the spin structure of the vertices NmN and Nm Δ is such that there is no contribution to the polarized cross section. At higher energies intermediate diffractive production should become important, but too little is known about the spin structure of diffractive production to be conclusive.

TABLE III

	<u>т</u> ц			
K _{LAB} (GeV)	$\operatorname{Re}(n_{L})$	Im(n _L)	Re (n _T)	Im (ŋ_)
0.5	1.01	-0.15	1.12	0.35
1.0	1.00	-0.07	0.98	0.11
1.5	1.00	-0.04	0.99	0.06
2.0	1.00	-0.03	1.00	0.04
2.5	1.00	-0.03	1.00	0.04
3.0	1.00	-0.02	1.00	0.03

VALUES	ΟF η _τ	AND	n _T FOR	SEVERAL	INCIDENT-PROTON	MOMENTA
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