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A THORIUM/URANIUM FUEL CYCLE FOR AN
ADVANCED ACCELERATOR TRANSMUTATION OF
NUCLEAR WASTE CONCEPT

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A THORIUM/URANIUM FUEL CYCLE FOR AN ADVANCED ACCELERATOR TRANSMUTATION OF NUCLEAR WASTE CONCEPT

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ABSTRACT

Utilizing the high thermal neutron flux of an accelerator driven transmuter to drive a Thorium-Uranium fuel production scheme, it is possible to produce enough energy in the transmuter not only to power the accelerator, but to have enough excess power available for commercial use. A parametric study has been initiated to determine the "optimum" equilibrium operation point in terms of the minimization of the equilibrium actinide inventory and the fuel α for various residence times in the High Flux Region (HFR) and in the Low Flux Region (LFR). For the cases considered, the "optimum" equilibrium operation point was achieved for a HFR residence time of 45 days and a LFR residence time of 60 days. For this case, the total actinide inventory in the system is about 20 tonnes and the fuel α approximately 1.46.

I. INTRODUCTION

An advanced ATW (Accelerator Transmutation of Nuclear Waste Concept) design, utilizing a Thorium-Uranium fuel cycle, is one of several accelerator driven transmuter concepts under consideration at Los Alamos National Laboratory.¹ The proposed design, as shown in Figure 1, consists of a liquid lead spallation target surrounded by a molten salt, helium cooled, graphite moderated blanket. The goal of this concept is to design a self-contained, self-sufficient transmuter which breeds and burns its own fuel, transmutes its own waste, and produces sufficient energy to power the accelerator and the transmuter's supporting facilities. Excess generating capacity would be placed on the power grid for off site commercial use. The design goal is to have the transmuter/energy producer operate at 3000 MW_{th}.

The Thorium/Uranium fuel mixture is slowly circulated through the blanket region in the form of a molten salt solution. The molten salt solution flows through two distinct regions as depicted in Figure 2; the first is a HFR (High Flux Region), a region of intense thermal neutron flux of approximately 2×10^{15} neutrons/cm²-s which enhances the production of ²³³Pa and the fissioning of ²³³U and ²³⁵U. The second region is a LFR (Low Flux Region), a region of low thermal neutron flux which provides a hold-up area for the decay of ²³³Pa to ²³³U. Part of the molten salt solution is diverted to a separate stream

to extract the fission products which have accumulated in the solution. ²³²Th is continuously added to the HFR to provide a steady source of fertile fuel.

One of the concerns associated with this advanced concept is the inventory of fissile/fertile material present in the system. Due to safety and nuclear proliferation concerns and to minimize the risk to the environment in case of an accident, it is desired to keep the material inventory at a minimum. However the minimization of the fuel inventory is only one aspect of the design. From a neutron economy and subcritical blanket multiplication factor standpoint, it is desired to minimize parasitic absorption within the molten salt fuel. A measure of the parasitic absorption taking place in the fuel is provided by α , the capture-to-fission ratio of the fuel, which affects the subcritical multiplication factor of the transmuter system. A parametric study has been initiated to determine the "optimum" equilibrium operation point in terms of the minimization of the equilibrium actinide inventory and the fuel α for the Thorium/Uranium fuel cycle of the advanced ATW concept for various residence times through the HFR and LFR regions.

II. METHOD OF SOLUTION

A. Rate Equations

The actinides comprising the Thorium/Uranium fuel cycle and their interdependency are depicted in Figure 3. The rate equations for the nuclides involved in the fuel cycle form a system of coupled first order linear differential equations which govern the time rate of change of the nuclide densities resulting from radioactive decay and transmutation by neutron absorption. The equations are of the form

$$\begin{aligned} \frac{dN_i(\bar{r}, t)}{dt} = & \Phi(\bar{r}, t) \times \sum_j N_j(\bar{r}, t) \sigma_{j \rightarrow i}(\bar{r}) \\ & + \sum_k N_k(\bar{r}, t) \lambda_{k \rightarrow i} \\ & - \Phi(\bar{r}, t) N_i(\bar{r}, t) \times \sum_l \sigma_{i \rightarrow l}(\bar{r}) \\ & - N_i(\bar{r}, t) \sum_m \lambda_{i \rightarrow m} + S_i(\bar{r}, t) \end{aligned} \quad (1)$$

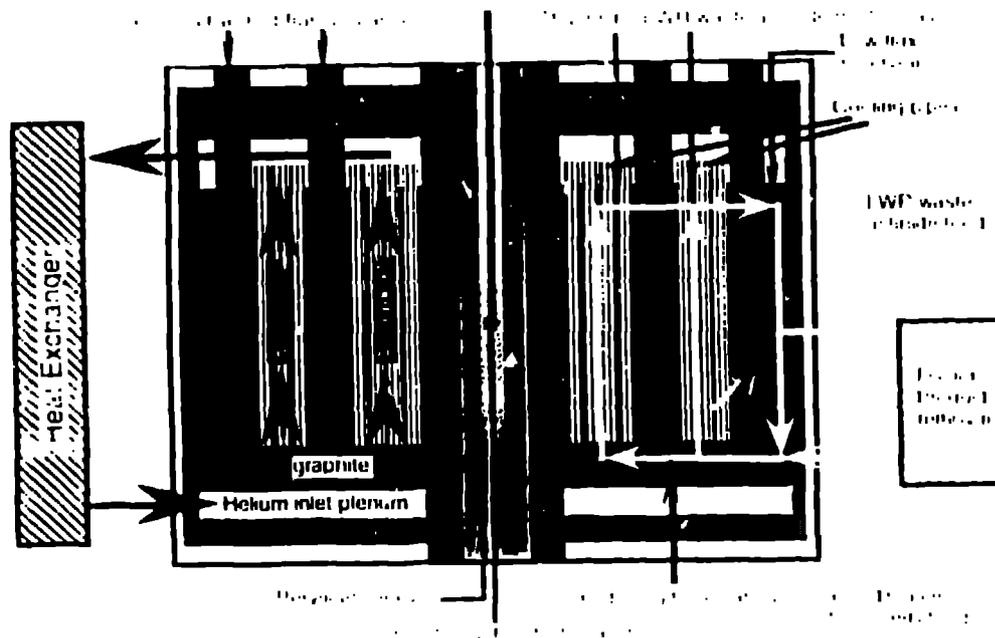


Figure 1 Schematic of the advanced ATF non-aqueous system blanket region

where:

- $N_i(\vec{r}, t)$ = number density of nuclide i at time t , at position \vec{r} ;
- $\Phi(\vec{r}, t)$ = total flux at time t , at position \vec{r} ;
- $\sigma_{n \rightarrow p}(\vec{r})$ = microscopic cross section for changing nuclide n into nuclide p at position \vec{r} ;
- $\lambda_{q \rightarrow s}$ = decay constant for nuclide q changing into nuclide s ;
- $S_i(\vec{r}, t)$ = external source of nuclide i at time t , at position \vec{r} ;

and where all references to multigroup fluxes and spectra averaged cross sections have been suppressed. The initial conditions are that $N_i(\vec{r}, 0) = N_{i0}(\vec{r})$.

Equation 1 can be cast into a general matrix equation (where the spatial variable has been suppressed),

$$\frac{d\vec{N}}{dt} = \mathbf{A} \times \vec{N}(t) + \vec{S}(t) \quad (2)$$

where

- $\vec{N}(t)$ = nuclide density vector
= $[N_1(t), N_2(t), \dots, N_N(t)]^T$;
- $\vec{S}(t)$ = external source vector
= $[S_1(t), S_2(t), \dots, S_N(t)]^T$;
- \mathbf{A} = matrix $[a_{ij}]$,
- a_{ii} = $(\sigma_{i \rightarrow i}^D \Phi + \lambda_i) \rho_{ii} + (\sigma_{j \rightarrow i}^P \Phi + \lambda_i b_{i \rightarrow j})$,
- $\sigma_{i \rightarrow i}^D$ = microscopic destruction cross section of nuclide i ;
- $\sigma_{j \rightarrow i}^P$ = microscopic production cross section of nuclide i forming nuclide j ;
- λ_i = decay constant of nuclide i .

- $b_{j \rightarrow i}$ = branching ratio of a decay from nuclide j to nuclide i ;
- δ_{ij} = the Kronecker delta

Several numerical algorithms have been developed for the solution of large matrix systems as obtained in the above general matrix form. The method employed in this paper to determine the equilibrium actinide concentrations (^{232}Th to ^{241}Am) is a variant of the MEM method (Matrix Exponential Method)^{2,3} which we have termed the EMEM method (Eigenvalue Matrix Exponential Method).⁴ As with the standard MEM method, EMEM operates on the general solution of matrix Equation 2. For a time independent external source ($\vec{S}(t) = \vec{S}$) Equation 2 has the solution,

$$\vec{N}(t) = e^{\mathbf{A}t} \times \vec{N}(0) + (1 - e^{\mathbf{A}t}) \times \mathbf{A}^{-1} \times \vec{S} \quad (3)$$

where \mathbf{I} is the identity matrix, $e^{\mathbf{A}t}$ is the matrix exponential function and $\vec{N}(0)$ is the initial concentration vector

In the MEM method the matrix exponential function is represented by its series expansion:

$$e^{\mathbf{A}t} = \mathbf{I} + \frac{\mathbf{A}}{1!}t + \frac{\mathbf{A}^2}{2!}t^2 + \frac{\mathbf{A}^3}{3!}t^3 + \dots + \frac{\mathbf{A}^n}{n!}t^n + \dots \quad (4)$$

To evaluate the exponential function at a specific time t , the time period (interval) t , is subdivided into time steps of width Δt . The series in Equation 4 is truncated incorporating sufficient terms so that the answer achieves a specific degree of accuracy at the end of time step Δt .¹ The computational speed associated with the method is thus dependent on the size of the time step which in turn is dependent on the magnitudes of the destruction rates contained in matrix \mathbf{A} .

and the following limiting values as $n \rightarrow \infty$:

$$\lim_{n \rightarrow \infty} (D^{n-1} + D^{n-2} + \dots + D + I) = (I - D)^{-1}$$

and

$$\lim_{n \rightarrow \infty} D^{n-1} = 0.$$

Equation 6 becomes:

$$\begin{aligned} \bar{N}_{Eq}^{LFR} &= -(I - D)^{-1} \times P \times (I - e^{A \Delta t_1}) \\ &\times A^{-1} \times P^{-1} \times \bar{S}. \end{aligned} \quad (7)$$

The expression derived above is for the actinide equilibrium concentrations of the molten salt fuel at the entrance to the LFR region. The actinide equilibrium concentrations at the entrance to the HFR region are computed from the expression:

$$\bar{N}_{Eq}^{HFR} = e^{B \Delta t_2} \times \bar{N}_{Eq}^{LFR}. \quad (8)$$

C. Equilibrium Inventory Calculation

Now that the equilibrium concentrations have been obtained for a given feedrate, Equations 7 and 8 can be integrated over the time interval that a unit volume of molten salt fuel spends in the HFR and LFR regions. The total inventory of actinide material contained within the HFR is obtained from the integration:

$$\begin{aligned} \bar{N}_{Inv}^{HFR} &= \int_0^{\Delta t_1} [\text{Eq. 3}] dt' = \int_0^{\Delta t_1} \\ &[e^{A t'} \times \bar{N}(0) - (I - e^{A t'}) \times A^{-1} \times \bar{S}] dt' \quad (9) \end{aligned}$$

where $\bar{N}(0)$ holds the equilibrium concentrations entering the HFR region (i.e. $\bar{N}(0) \equiv \bar{N}_{Eq}^{HFR}$). Utilizing the eigenvalue-eigenvector decomposition of matrix A and performing the indicated integration, Equation 9 has the solution:

$$\begin{aligned} \bar{N}_{Inv}^{HFR} &= -P \times (I - e^{A \Delta t_1}) \times A^{-1} \times P^{-1} \times \bar{N}_{Eq}^{HFR} \\ &- P \times \left[\Delta t_1 I + (I - e^{A \Delta t_1}) \times A^{-1} \right] \\ &\times A^{-1} \times P^{-1} \times \bar{S}. \end{aligned} \quad (10)$$

The inventory of actinide material contained in the LFR region is:

$$\bar{N}_{Inv}^{LFR} = -Q \times (I - e^{\Gamma \Delta t_2}) \times \Gamma^{-1} \times Q^{-1} \times \bar{N}_{Eq}^{LFR} \quad (11)$$

where

$$e^{B \Delta t_2} = Q \times e^{\Gamma \Delta t_2} \times Q^{-1},$$

and

$$\begin{aligned} \Gamma &= \text{diagonal eigenvalue matrix of B;} \\ Q &= \text{eigenvector matrix of B;} \\ Q^{-1} &= \text{inverse of Q.} \end{aligned}$$

Once the total actinide inventory has been established, the thermal power produced in the HFR is computed. Six nuclides are assumed to contribute to the power of the transmuted, they are, ^{233}U , ^{235}U , ^{238}Np , ^{238}Pu , ^{239}Pu and ^{242}Pu . Each fissile species is assumed to produce 190 MeV/fission. If the computed thermal power does not equal 3000 MW, then the ^{232}Th feedrate is adjusted. Two iterations are required to obtain the actinide total inventory.

D. Calculation of Alpha - The Capture-to-Fission Ratio of the Fuel

The molten salt subcritical blanket multiplication factor, M , is related to the neutron multiplication factor, k , by the following expression

$$M = \frac{1}{1 - k}$$

where

$$k = \frac{\sum_{i=1}^N \nu_i \Sigma_f^i}{\sum_{i=1}^N \Sigma_a^i + \Sigma_a^{\text{other}}}$$

Σ_f^i = macroscopic fission cross section of the i 'th fuel nuclide,

Σ_a^i = macroscopic absorption cross section of the i 'th fuel nuclide,

Σ_a^{other} = macroscopic absorption cross section of non-fuel constituents, and

ν_i = the average number of neutrons released per fission for the i 'th fuel nuclide.

Defining an effective average number of neutrons released per fission for the fuel $\bar{\nu}$, leads to the following expression for k :

$$k = \frac{\bar{\nu}}{1 + \alpha + c}$$

where

$$\bar{\nu} = \frac{\sum_{i=1}^N \nu_i \Sigma_f^i}{\sum_{i=1}^N \Sigma_f^i}, \quad \alpha = \frac{\sum_{i=1}^N \Sigma_a^i}{\sum_{i=1}^N \Sigma_f^i}, \quad \text{and} \quad c = \frac{\Sigma_a^{\text{other}}}{\sum_{i=1}^N \Sigma_f^i}.$$

We note that α is the ratio of the capture to fission cross sections of the fuel and that it plays an important role in determining k and hence the multiplication, M , of the subcritical system. A lower value of α (fewer parasitic absorptions in the fuel) implies a larger value of k which in turn implies a larger value of M . All nuclides in the ^{232}Th transmutation and decay scheme (see Figure 3) are considered fuel constituents and are included in the calculation of α .

E. Data

A brief comment on the data used for the calculations. The molten salt fuel within the advanced ATW system is assumed to

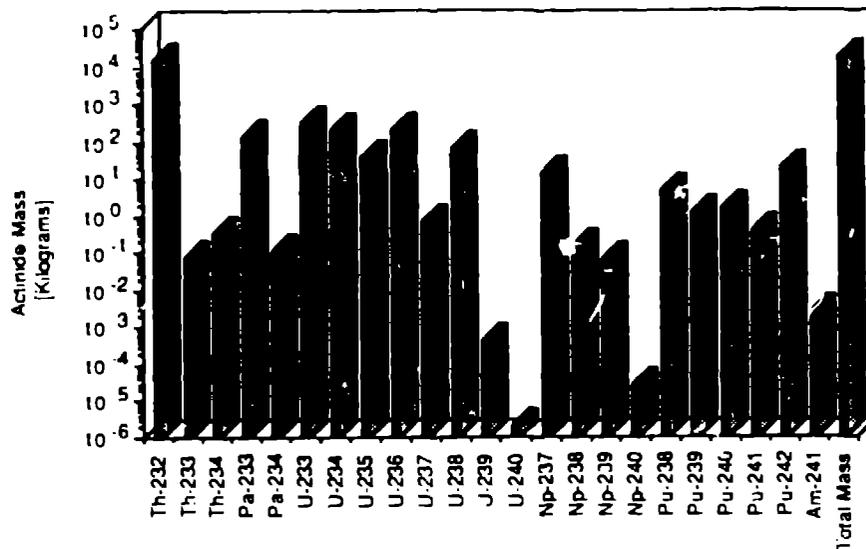


Figure 4 Equilibrium Composition for the 45 day HFR - 90 day LFR residence time case.

Table 1. Actinide Mass Within the ATW System

Nuclide	45 HFR/ 90 LFR	45 HFR/ 150LFR	30 HFR/ 75 LFR
	Mass [kg]	Mass [kg]	Mass [kg]
²³² Th	1.465e+4*	2.116e+4	1.709e+4
²³³ Th	7.334e-2	7.334e-2	7.332e-2
²³⁴ Th	2.952e-1	2.953e-1	2.954e-1
²³³ Pa	1.191e+2	1.200e+2	1.208e+2
²³⁴ Pa	1.0004e-1	9.395e-2	8.237e-2
²³³ U	2.752e+2	4.423e+2	2.989e+2
²³⁴ U	1.946e+2	2.737e+2	2.094e+2
²³⁵ U	3.554e+1	4.992e+1	3.831e+1
²³⁶ U	1.935e+2	2.718e+2	2.085e+2
²³⁷ U	6.564e-1	6.385e-1	6.204e-1
²³⁸ U	6.617e+1	9.300e+1	6.461e+1
²³⁹ U	3.880e-4	3.774e-4	3.247e-4
²⁴⁰ U	2.053e-6	1.957e-6	1.718e-6
²³⁷ Np	1.292e+1	1.843e+1	1.416e+1
²³⁸ Np	1.392e-1	1.354e-1	1.330e-1
²³⁹ Np	5.704e-2	5.549e-2	4.807e-2
²⁴⁰ Np	2.398e-5	2.333e-5	1.939e-5
²³⁹ Pu	4.569e+0	6.459e+0	5.102e+0
²⁴⁰ Pu	1.153e+0	1.645e+0	1.243e+0
²⁴¹ Pu	1.531e+0	2.149e+0	1.647e+0
²⁴² Pu	3.470e-1	4.853e-1	3.734e-1
²⁴³ Pu	1.792e+1	2.514e+1	1.927e+1
²⁴¹ Am	2.370e-3	5.270e-3	2.586e-3
Total Mass	1.558e+4	2.247e+4	1.808e+4
Fissile Mass	3.170e+2	5.009e+2	3.441e+2
²³² Th Feedrate [atoms/s]	2.54e+13	2.54e+13	3.81e+13

*read as 1.465 x 10⁴

be at a temperature of 1500°C. The cross section data utilized for the calculations was taken from MCNP⁵ cross section data files at the operating temperature.

III. RESULTS

The equilibrium actinide inventories for the advanced ATW concept for a 45 day residence time in the HFR and a 90 day residence time in the LFR (45 HFR/90 LFR) are depicted in Figure 4. ²³²Th dominates the inventory of the system contributing to over 94% of the mass in the system. The large inventory of ²³²Th is required for the production of ²³³U and to a lesser degree ²³⁵U as they dominate the energy production in the system. A comparison of the actinide inventories for the 45 HFR/90 LFR, 45 HFR/150 LFR and the 30 HFR/75 LFR cases is presented in Table 1. Of the 3 cases presented, the 45 HFR/90 LFR case has the lowest total actinide and fissile inventories.

The percentage of power produced by each fissile isotope considered is presented in Table 2. For all cases presented ²³³U produces over 84% of the power followed by ²³⁵U with approximately 13%. Of the other fissile isotopes only ²⁴¹Pu contributes more than 1% of the power.

Figure 5 summarizes the 45 day HFR residence time total actinide inventory and fuel ρ results for varying LFR residence times. As the residence time in the LFR increases the total actinide mass in the system increases (i.e., the inventory of material residing in the LFR increases as the holdup time is increased). We note that ρ decreases to an asymptotic value as the LFR residence time increases. This reflects the production of ²³³U from the decay of ²³¹Pa in the LFR. Over 98% of the ²³¹Pa will have decayed to ²³³U for a residence time corresponding to six ²³¹Pa half-lives, hence there is little incentive to increase the holdup time beyond this duration. ρ decreases because of an increase in ²³³U. We note that the minimization of the fuel ρ and the total actinide mass in the system are in opposing directions. The curves intersect at approximately 60

Table 2. Power Production from Fissile Isotopes

Nuclide	45 HFR/90 LFR		45 HFR/150 LFR		30 HFR/75 LFR	
	Power [MW]	Percent of Total [%]	Power [MW]	Percent of Total [%]	Power [MW]	Percent of Total [%]
²³³ U	2525.07	84.17	2525.07	84.17	2561.27	85.38
²³⁵ U	408.70	13.62	408.70	13.62	377.50	12.58
²³⁸ Np	18.86	0.63	18.86	0.63	17.43	0.58
²³⁸ Pu	1.26	0.04	1.26	0.04	1.21	0.04
²³⁹ Pu	34.46	1.15	34.46	1.15	31.85	1.06
²⁴¹ Pu	11.65	0.39	11.65	0.39	10.74	0.36
Total	3000.00	100.00	3000.00	100.00	3000.00	100.00

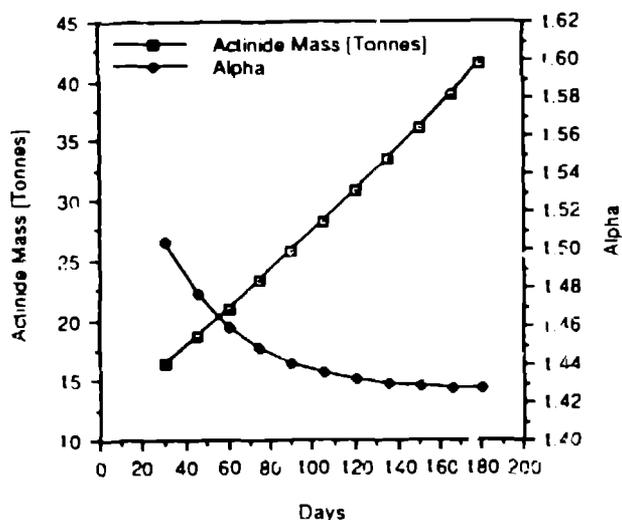


Figure 5. Total actinide mass and fuel α for a 45 day residence time in the HFR and varying residence times in the LFR.

days in the LFR. At this LFR residence time the total actinide inventory in the system is approximately 20 tonnes and the fuel α is about 1.46.

Figure 6 summarizes the 90 day LFR residence time total actinide inventory and fuel α results for varying HFR residence times. We note that the total actinide mass in the system decreases as the residence time in the HFR increases. The reason for this is that as the residence time in the HFR increases more of the ²³³Pa decays to ²³³U while still residing in the HFR. However α increases as the residence time in the HFR increases due to parasitic absorption in Pa and higher mass U isotopes in the fuel. For the specific case of 90 days in the LFR, the total actinide mass and α curves intersect at approximately 60 days in the HFR. The total actinide inventory and α values are approximately 22.5 tonnes and 1.47, respectively.

IV. SUMMARY

A parametric study has been initiated to determine the "optimum" equilibrium operation point in terms of the minimization of the minimum equilibrium actinide inventory and

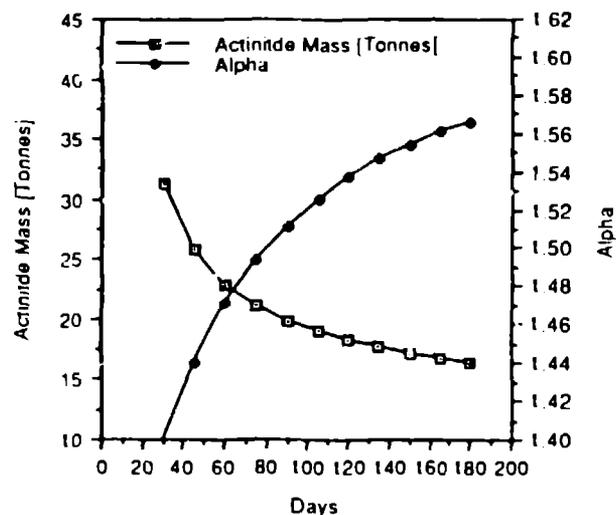


Figure 6. Total actinide mass and fuel α for a 90 day residence time in the LFR and varying residence times in the HFR.

the fuel α for various residence time through the HFR and LFR regions of the advanced ATW concept. From the results of this study, the minimization of α and the total actinide inventory in the system are in opposing directions. For the cases considered, the "optimum" equilibrium operation point was achieved for a HFR residence time of 45 days and a LFR residence time of 60 days. At this operation point, the total actinide inventory in the system is about 20 tonnes and the fuel α approximately 1.46. The next step in the analysis of the advanced ATW concept is to include additional Americium and Curium isotopes and to investigate the actinide inventories and fuel α during the equilibration phase of the transmuted.

A brief note about the computer program. The computer code developed for this parametric study utilizes the Eigenvalue Matrix Exponential Method for the solution of the system of first order differential equation which govern the actinide concentrations in the system. The method has proven itself to be computational efficient; no time step control or series expansion is necessary. Radioactive decay loops were not considered in the fuel cycle analysis, they can be easily incorporated along the lines of the Avalanche method.⁶

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