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AND OF ISOTOPIC SWAMPING ON TRITIUM RECOVERY AND LOSS TO
BIOSPHERE FROM FUSION REACTORS

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MIXING RULES FOR AND EFFECTS OF OTHER HYDROGEN ISOTOPES AND OF
ISOTOPIC SWAPPING ON TRITIUM RECOVERY AND LOSS TO BIOSPHERE FROM FUSION
REACTORS

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ABSTRACT

Efficient recovery of bred and unburnt tritium from fusion reactors, and control of its migration within reactors and of its escape into the biosphere are essential for self-sufficient fuel cycles and for public, plant personnel, and environmental protection. Tritium in fusion reactors will be treated with hydrogen deuterium and protium isotopes in fuel reactions and diffusion into coolant flows from steam cycles. Rational design for tritium recovery and escape prevent the most acknowledge this fact. Consequences of isotopic substitution are explored, mixing rules for predicted fusion reactor dilute-solution conditions are developed, and rules for those predicting those effects on both macroscopic variables are derived.

INTRODUCTION

Present indications are that at least the first generation of fusion reactors will be fueled with a mixture of deuterium and tritium (DT). Because the need for tritium to sustain the fusion reaction is so great, breeding from deuterium is less attractive than breeding from hydrogen isotopes. The hydrogen isotopes deuterium and tritium are lighter than helium and thus escape more easily from fusion reactors. Tritium is also more radioactive than deuterium, and tritium breeding is more difficult. Although tritium is relatively safe, it is relatively hard to separate from deuterium. Tritium is hygroscopic, diffuses rapidly, and diffuses through membranes. These biological properties are important factors in the DT problem.

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Print form will be supplied for filing applications
of Microfilm Owners to make copies of the material
they have microfilmed. The application form
will be available at the Bureau of Motion Picture
and Sound Film, and at the Bureau of Broadcast
and Motion Picture, and at the Bureau of Photo-
graphs and Motion Pictures.

He had been a good boy, and he had been a good man, and he had been a good husband, and he had been a good father, and he had been a good son, and he had been a good brother, and he had been a good friend, and he had been a good neighbor, and he had been a good citizen, and he had been a good member of his church, and he had been a good member of his community, and he had been a good member of his country, and he had been a good member of his world, and he had been a good member of his universe, and he had been a good member of his God's creation.

Each year, the number of people who die from heart disease increases. This is due to the fact that more and more people are becoming overweight. The result of this is that they have more heart trouble. In addition, many people are smoking cigarettes, which also causes heart trouble. These factors, along with other things like stress and lack of exercise, contribute to the increase in heart disease.

and deuterium. Thus, unburnt tritium and deuterium, which constitute the majority of fuel fed to fusion reactors, may not represent the majority of hydrogen isotopes recovered.

Recovery of deuterium, which is relatively abundant in nature and can be obtained at modest cost, is not necessary for economic generation of fusion energy. However, buildup of protium and deuterium within reactor subsystems to excessive levels cannot be tolerated, because of potential deleterious effects on reactor materials of construction. Tritium recovery systems will simultaneously remove protium and deuterium because of their similar physicochemical characteristics, but at a penalty of increased tritium machinery system capacity.

Present concentrations in thermonuclear reactor fuel storage will probably have to be reduced to 1% or less. The DT isotopic ratio must be adjusted by the addition of minor tritium.

Finally, although this is a procedure for the short-term, it is the part of the strategy that can be most affected by the presence of feedback. In this short assessment of the feedback effect, we tested the effects of the presence of the other two factors on the short-term performance of a group. The first factor was the presence or absence of a group leader. The second factor was the presence or absence of a group member who had been successful in the past.

But in the other case, if the other party
is not going to do what you want him to do,
then you have to make it clear that he is not
going to do what you want him to do, and that
you are going to sue him for damages if he
does not do what you want him to do. If you
do not do that, then he will not do what you
want him to do, because he will not be afraid
of you threatening to sue him for damages if
he does not do what you want him to do. So
you have to make it clear that he is not going
to do what you want him to do, and that you
are going to sue him for damages if he does
not do what you want him to do.

Our discussion will be confined to the dilute-solution conditions anticipated for tritium in fusion reactor breeding blankets, coolant loops, structural materials, and perhaps cavity exhaust streams. Early estimates of rates of tritium escape into steam cycles from coolant loops suggested that tritium concentrations in fusion reactor systems might have to be maintained at 1 ppm or less. As the difficulties of tritium recovery from solutions at such concentrations have become apparent, more effective concepts for prevention of tritium escape have been developed, and the importance of potential tritium hazards to fusion to other potential fusion reactors has not been adequately assessed, see, but a continuation has been given to operation with tritium concentrations an order of two higher in magnitude. Nonetheless, dilute solution theory will still be applicable, at least up to 10% tracer concentrations, for most applications.

We will focus on the development of mixing rules for equilibrium of light ion isotopic mixtures and on the effects that the presence of one or more hydrocarbons may have on the performance of tritium separation systems.

PHYSICAL PROBLEMS OF ISOTOPIC PURIFICATION MIXTURES

Most of the structure of fusion reactors will be probed by tritium. Many of the problems involved involve tritium loss from the reactor breeding tritium loops due to tritium vaporization in the loops. Clearly, the migration of tritium is affected by the presence of other atomic isotopes, in addition to tritium, in diluting tritium inventories and the performance of the various separation and purification processes. We will discuss some aspects of the relationship of hydrogen isotopes to tritium.

Many careful experiments, notably by Long and Ricca,⁽¹⁾ Picra,⁽²⁾ Streltsov and Gorbunov,⁽³⁾ Hank,⁽⁴⁾ Chen and Wu,⁽⁵⁾ and Nagasawa and Yamamoto,⁽⁶⁾ have confirmed that the em-

pirical relationship named for A. Stevarts accurately describes the temperature-dependent solubility of protium, deuterium, and tritium in metals at very low concentrations and, in some instances, at relatively high concentrations, for both pure metals and alloys with low surface-to-volume ratios so that adsorption is not a significant factor.

A theoretical justification for Stevarts' empirical law can be developed as follows. We assume, in accord with experimental evidence, e.g., see Eisenberg,⁽⁷⁾ that a hydrogen atom exists in solution in metals as an independent molecule. For present purposes it is not necessary whether the dissociation of adsorbed water is necessary for dissolution occurs in the gas phase, on the metallic surface, or in the bulk metal. An equivalent expression for the solubility of hydrogen, S_H^* , is given by

$$\frac{S_H^*}{S_D^*} = \left(\frac{P_H^*}{P_D^*} \right)^{\frac{1}{2}} \exp \left[-\frac{E_A}{RT} \right] \quad (1)$$

THEORETICAL PREDICTION OF SOLUBILITY

The complete solution of the problem of predicting the solubility of tritium in a metal requires consideration of the effect of the presence of deuterium, helium, and hydrogen. The effect of deuterium is small, and the effect of helium is negligible. The effect of hydrogen is important, however, and must be considered. The effect of hydrogen is important because hydrogen is the most abundant element in the universe and is the most abundant element in the earth's crust.

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⁽¹⁾ Temperature dependence of the solubility of tritium in standard aluminum is reported in ref. 1.

ed, then Stevens' law for the solubility of hydrogen isotopes in metals is obtained:

$$X_{H(s)} = K_{S_H}^{1/2} \left(P_{H_2}/P_{\text{atm}} \right)^{1/2}$$

$$K_{S_H}^{1/2} = \frac{0.5/M}{S_H^0} \cdot \frac{10^{\gamma_H - \gamma_{H(s)}}}{S_H^0 \gamma_{H(s)}}$$

$$S_H^0 = 20^0$$

Derivation of the mixing rule

It has been shown above that the only other approach to a solution of the problem of predicting solubilities of the individual hydrogen isotopes is to determine the gross solubility of the mixture, and then to separately predict the solubility of each isotope.

Obviously, it is not possible to do this directly, since the solubility of the individual species would have to be known. Instead, Stevens' law is used to predict the total solubility.

$$X_{\text{Total}} = X_{D(s)} \frac{P_D^{1/2}}{P_{\text{Total}}^{1/2}}$$

By substituting the simple form of the law

$$X_D = K_D^{1/2} \left(P_D/P_{\text{atm}} \right)^{1/2}$$

into eq. (1), we find that the solubility of holes in the metal due to one isotope is available for calculation if we know the solubility due to the other isotope. This is true for both isotopes, and is not dependent on the isotopes.

Hicks and co-workers¹ have calculated the solubility of holes in the metal due to each of proton and deuteron, and the solubility of tritium and alpha. In the form of these experimental results, we can write that the useful Stevens' law describes the solubility of the mixture as

After some rearrangement, the mixing rule suggested by Hicks¹ for calculating the results of

experiments which investigated the permeation of gaseous mixtures through the walls of tubes of the same alloy. They claimed acceptable agreement between their experimental results and those of analysis based on Hickman's hydrogen mixing rule.

However, the fact that Stevens' law accurately predicts the solubility of hydrogen isotopes in many metals and alloys up to relatively high concentrations, suggests, for systems sufficiently dilute in the dissolved hydrogen isotopes, that the system is also relatively dilute in comparison to the number of holes in a stable valence band. The large isotopic differences in solubility, as reflected by differences in Stevens' law constants, suggest that a mixture of hydrogen isotopes cannot be treated as a single chemical substance for all purposes. Therefore, the following analysis, which explores the consequences of validity of Stevens' law for the solution of individual hydrogen isotopes in metals, was performed to develop an alternative, which has been theoretical basis, to the mixing rule.

On an atomic basis, in solution, sufficiently dilute in all solutes, solute atoms are surrounded by and interact with virtually all the atoms in the solvent atom rather than with other solute atoms. Therefore, in such solutions, the solubility of one solute is independent of the others, primarily by its properties and by those of the solvent, and the effects are negligible for the properties of other solutes. This interpretation should also be valid if the solvent is a mixture of species, as long as one estes of concentration of the species in the solvent is sufficiently large. If the solvent is an alloy, dilute, or otherwise,

Thus we conclude that Stevens' law descriptions obtained by fitting experimental solubility data for pure isotopes are inapplicable to multicomponent gaseous mixtures when hydrogen isotopes are involved. Therefore, for a system containing all three hydrogen isotopes, we write:

$$X_{\text{Total}} = X_{D(s)} + X_{T(s)} + X_{\alpha(s)}$$

$$= K_D^{1/2} \left(P_D/P_{\text{atm}} \right)^{1/2} + K_T^{1/2} \left(P_T/P_{\text{atm}} \right)^{1/2} + K_\alpha^{1/2} \left(P_\alpha/P_{\text{atm}} \right)^{1/2}$$

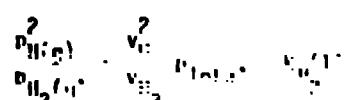
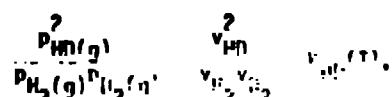
$$= \left[K_{S_H}(T) y_{H_2}^{1/2} + K_{S_D}(T) y_{D_2}^{1/2} + K_{S_T}(T) y_{T_2}^{1/2} \right] P_{\text{Total}}^{1/2}$$

$$= K_{S_{\text{Total}}}(T) P_{\text{Total}}^{1/2}$$

In an isotopic mixture there will be isotopic exchange in the gas phase, i.e., in addition to the molecular species $H_2(g)$, $D_2(g)$, and $T_2(g)$ the species $HD(g)$, $DT(g)$, and $TH(g)$ will be present. In addition, the diatomic molecules can dissociate to yield the atomic species $H(a)$, $D(a)$, and $T(a)$. The following set of six gas-phase reactions are independent:



The corresponding equilibria can be expressed in the form:



T, K	EQUILIBRIUM CONCENTRATIONS, MOLES/LITER, AT T = 25°C FOR A 1:1:1:1:1:1 MIXTURE OF H, D, AND T AT TOTAL PRESSURE = 1 ATM					
	$K_{HD}(T)^{1/2}, \text{ atm}^{-1}$	$K_{HT}(T)^{1/2}, \text{ atm}^{-1}$	$K_{TD}(T)^{1/2}, \text{ atm}^{-1}$	$y_{H_2}, \text{ atm}^{-1}$	$y_{D_2}, \text{ atm}^{-1}$	$y_{T_2}, \text{ atm}^{-1}$
300	13.39×10^{-72}	1.219×10^{-72}	---	3.79	2.46	2.46
400	---	---	---	3.48	2.00	2.00
500	4.632×10^{-14}	1.171×10^{-41}	---	3.62	3.26	3.26
600	---	---	---	3.71	3.45	3.45
700	---	---	---	3.79	3.56	3.56
800	---	---	---	3.83	3.68	3.68
900	---	---	---	3.87	3.76	3.76
1000	5.174×10^{-16}	2.972×10^{-10}	1.0×10^{-11}	3.93	3.85	3.85
1250	---	---	---	3.95	3.92	3.92
1500	3.100×10^{-10}	2.220×10^{-10}	7.44×10^{-10}	3.96	3.93	3.93
2000	2.651×10^{-6}	2.227×10^{-6}	2.35×10^{-10}	3.97	3.97	3.97

*Woolley, et al.⁽³²⁾

**Jewell⁽³³⁾

with similar expressions for the other reactions. Experimental values for the equilibrium constants are listed in Table I.

In terms of y_{H_2} , y_{D_2} , and y_{T_2} the equilibrium relationships for the gas phase can be written, in the absence of significant molecular dissociation to form the atomic species, in the form:

$$\frac{\{y_{H_2} - y_{H_2}^{1/2} y_{D_2}^{1/2} y_{T_2}^{1/2}\}^2}{y_{H_2} y_{D_2} y_{T_2}} = K_{HD}(T)$$

Upon substitution of the equilibrium expression for y_{H_2} as:

$$y_{H_2} = \{y_{H_2}^{1/2} y_{D_2}^{1/2} y_{T_2}^{1/2}\}^2 / \{y_{D_2}^{1/2} y_{T_2}^{1/2}\}$$

Solution for the mole fraction of the three gaseous species may lead to the following relationships. Substitution of the equilibrium expression for the diatomic species yields the following equations giving an answer in terms of the mole fractions of the species:

If dissociation is negligible, we find the following equilibrium concentrations for the situation of equal partial pressures of the isotopes:

expressions for y_{H_2} , y_{D_2} , and y_{T_2} for substitution into the first three equilibrium relations are now of the form:

$$y_{HD} = \frac{(y_H y_{H_2})^2 (y_D y_{D_2})^2 (y_T y_{T_2})^2}{\left[\sqrt{\frac{K_H(T)}{P_{Total}}} + \sqrt{\frac{K_D(T)}{P_{Total}}} + \sqrt{\frac{K_T(T)}{P_{Total}}} \right]^2}$$

To obtain a meaningful comparison with the intuitive mixing rule of Dickman, we consider a mixture of protium and deuterium only at temperatures sufficiently low and pressures sufficiently high that dissociation to form the third isotope can be neglected. But, it is argued, it is reasonable that the equilibrium constant $K_T(T)$ is very negligible from A_3 , the probability of ionization. Based on these assumptions, solution for the molecular ratio fraction gives

$$y_{D_2}^2 / y_{H_2}^2 = y_D^2 / y_H^2$$

Substitution of this result into the mixing rule yields a result identical to that of the mixing rule based on the Dickman mixing rule. The Dickman mixing rule is the most appropriate mixing rule. We note that, in the case of a mixture of protium and deuterium containing $\sim 20\%$ deuterium, y_D^2 / y_H^2 is the value 0.04, and the resulting ratio of deuterium to protium is 0.2. This result goes far beyond the range of validity of the Dickman mixing rule, which is only valid for ratios of deuterium to protium small enough to satisfy the condition $y_D^2 / y_H^2 \ll 1$. The Dickman mixing rule is not appropriate for isotopic swapping.

The introduction of large amounts of protium into fusion reactor systems has an alternative to promote recovery of tritium in that lower tritium concentrations result in lower inventories and escape rates, as the next point. This process, referred to as isotopic swapping, can be beneficial if:

- required capacities of tritium recovery and isotopic separation systems are not increased inordinately as a result of isotopic swapping,
- isotopic swapping significantly decreases residual tritium concentrations or enhances the effectiveness of barriers to tritium escape by mechanisms not otherwise available,
- the use of tritium recovery methods which are inherently less expensive, e.g., whose capital and/or operating costs are less, is made feasible through isotopic swapping.

These characteristics represent the basis upon which a rule of thumb for a priori assessments of potential beneficial effects of isotopic swapping on fusion reactor tritium recovery methods can be established. Many processes have been proposed for recovery and/or concentration of bred tritium from tritium-breeding blanket and coolant-loop streams, and unburnt tritium from cavity exhaust streams. The effects of isotopic swapping on all these proposed processes cannot be discussed here, and we are forced to concentrate on only a few. In particular, we will discuss effects of isotopic swapping on recovery of tritium by means of tritium window and cold transfer of liquid-metal breeding cycle and secondary coolant loops and on escape of tritium into the biosphere by seepage through a barrier barrier.

Isotopic Swapping Effects on Tritium Recovery

Hickman¹¹ examined the effects of isotopic swapping on self-sustained processes for tritium extraction from liquid tritium, which possessed the following characteristics:

- Sieverts' law of solubility of hydrogen isotopes in metals and Hickman's mixing rule for dissolution of hydrogen isotopes in metals are both applicable,
- The only significant resistance to permeation through the window is the resistance to diffusion of the bulk metal of the window membrane,
- Tritium extraction is performed under steady state, isothermal conditions.

- Equilibrium with respect to isotopic interchange between diatomic molecular hydrogenic species in the gas phase is attained at all times, the high-temperature limiting values of the isotopic interchange equilibrium constants are applicable, and molecular dissociation to give the atomic species can be neglected.

The stated assumptions imply that expressions for the permeation fluxes of protium and tritium through the tritium window can be written in the forms:

$$J_{T_2} = \frac{C_{T_2}(T)}{k} = (P_{T_2}^{1/2} - P_{T_2}^{1/2})^2 \cdot \frac{D_T(1)}{k} \cdot [(y_T p_{Total})]^{1/2}$$

$$- (y_T p_{Total})^{1/2} \cdot \frac{D_M}{k} \cdot \frac{D_T(1)}{k} \cdot (x_1 - x_{T_2})$$

$$= \frac{C_{T_2}(T)}{k} \cdot [(y_{T_2} p_{Total})]^{1/2} \cdot [(y_T p_{Total})]^{1/2}$$

$$= \frac{C_{T_2}(T)}{k} \cdot P_{T_2} \cdot D_T \cdot \frac{C_T}{C_{T_2}} \cdot \frac{C_T}{C_{T_2}}$$

If all three hydrogen isotopes are present and/or if dissociation of the molecular species to give the atomic species in the gas phase cannot be neglected, then the analysis will be more complex, but similar.

Now let the total pressure on the low-pressure side be negligible and consider the addition of protium to a system containing initially only tritium. Then the ratio of the tritium flux to its initial value is:

$$J_{T_2}/J_{T_2}^0 = y_T(p_{Total})/P_{T_2}^0$$

whereas the ratio of the effective system tritium inventories under the same conditions is:

$$C_T/C_{T_2}^0 (P_{T_2} + P_{H_2})/P_{T_2}^0 \cdot y_{T_2}(p_{Total})/P_{T_2}^0$$

$$C_T/C_{T_2}^0 p_{T_2}/P_{T_2}^0 \cdot y_{T_2}^2 p_{Total}/P_{T_2}^0$$

respectively, for a gas-phase and a liquid-metal phase constituting the principal tritium reservoir.

If the system tritium inventory is maintained constant, then, respectively, for the two cases:

$$y_T^2 p_{Total}/P_{Total}, \quad y_T^2 p_{Total}/P_{Total},$$

$$J_{T_2}/J_{T_2}^0 = y_T^{1/2} + 1, \quad J_{T_2}/J_{T_2}^0 = 1.$$

In the first case, although the system tritium inventory has not been reduced, the tritium window area will have to be increased to remove tritium from the system at the same total rate. In the second case the isotopic swamping has not affected the required tritium window area. Thus, depending on what type of phase represents the principal tritium reservoir, the tritium window area required for a constant total rate of tritium recovery is either increased or not affected for a constant tritium inventory, but clearly is increased if the tritium inventory is to be reduced.

If, instead, the total hydrogen isotope pressure is maintained constant, then:

$$J_{T_2}/J_{T_2}^0 = y_T^2 \lambda$$

in both cases, while respectively:

$$C_T/C_{T_2}^0 y_{T_2}^2, \quad C_T/C_{T_2}^0 y_{T_2}^2$$

Thus, in both cases, the tritium window area required to reflect the indicated inventory reduction at a constant tritium inventory rate is increased by the factor $1/\lambda$, but the tritium inventory reduction is greater in the second case.

It is also clear that isotopic swamping will either enhance or not affect the performance of barriers to tritium migration for all the cases considered. Note also that the increase in tritium window area required for removal of tritium at a constant rate when no protium is added is $1/\lambda$ when the tritium inventory level is reduced by the factor λ in either a gas phase or a liquid-metal phase.

Isotopic Swamping Effects When Surface Processes are Rate Determining

Hickman⁽³⁵⁾ and Varon⁽³⁶⁾ examined another case of tritium recovery through a tritium window from a fluid stream that had been isotopically swamped with protium. This case involved the postulate that the permeation rate-limiting step was a slow surface process, the recombination of hydrogen isotope atoms followed by desorption from the low tritium partial-pressure side of the membrane. Adsorption-desorption processes, even if consideration is restricted to adsorption and desorption of hydrogen isotopes only, can be complex and there is a vast, often contradictory literature concerning this topic. Therefore, we can only briefly touch upon the subject. If the adsorption and dissociation step on the upstream side of the barrier is permeation rate controlling then a similar approach can be used in the analysis.

This particular step in the permeation process is carefully examined because there is evidence that, under projected thermonuclear reactor conditions, the recombination and desorption of tritium atoms may indeed be rate-limiting. For example, Gondoli, et al.,⁽³⁷⁾ explained the results of their experiments coincident with permeation of hydrogen isotopes from liquid lithium through niobium membranes on the basis of such a rate-limiting step.

The model for hydrogen isotope permeation which we shall consider involves the following assumptions, and approximations:

- All resistances to permeation other than those due to the desorption process are negligible.
- The partial pressures of tritium and protium on the low partial pressure side of the barrier are so small that the adsorption rate on that side of the barrier is negligible in comparison to the desorption rate.
- The simple Langmuir adsorption theory with a single class of active sites adequately describes the adsorption process.
- Dissociation in the gas phase to form the atomic hydrogen isotope species from the diatomic molecular species can be neglected,

- The adsorptive characteristics of the high and low partial-pressure barrier surfaces do not differ significantly.
- The permeation occurs under steady-state, isothermal conditions.

The essence of the elementary Langmuir theory of adsorption may be stated as follows. Adsorption of molecules from the gas phase onto solid surfaces can occur only at certain active "sites" on the surface which have an affinity for the species being adsorbed, are uniformly distributed, and have equal affinities for the adsorbed species. Each such site is assumed to be capable of adsorbing only a single atom or molecule of the adsorbed species and, because the forces that are responsible for the adsorption are short range, the adsorption at any site is assumed to be independent of whether or not an adjacent site is occupied. If the adsorption involves a dissociation, say of a diatomic molecule, such as tritium molecules, to form the atomic species, then the adsorption process is assumed to involve a reaction between the diatomic molecule and two adjacent sites on the solid surface. The number of pairs of adjacent sites, based on the above listed characteristics of the active sites, is proportional to the square of the number of unoccupied sites, which can be represented in terms of a fractional occupancy of active sites by the adsorbed species, often called the surface coverage by the adsorbed species. In terms of the surface coverage by the adsorbed species and the partial pressure of the gas phase molecular form, a kinetically third-order expression for the rate of adsorption is postulated:

$$r_{T_2\text{Ads}} = k_{T_2\text{Ads}}(T)(1-\theta_T)^2 p_{T_2} .$$

Similarly, the desorption reaction is assumed to involve the kinetically second order reaction of two adsorbed atoms on adjacent active sites whose number is taken as proportional to the square of the fractional coverage and, in terms of surface coverage by the adsorbed species, a rate expression is written as:

$$r_{T_2\text{Des}} = k_{T_2\text{Des}}(T) \gamma_T^2$$

Under conditions of adsorption equilibrium, the two rate expressions for adsorption and desorption can be equated and solved for θ_T to obtain:

$$\theta_T = \frac{\left[\frac{k_{T_2\text{Ads}}(T)}{k_{T_2\text{Des}}(T) p_{T_2}} \right]^{1/2}}{1 + \left[\frac{k_{T_2\text{Ads}}(T)}{k_{T_2\text{Des}}(T) p_{T_2}} \right]^{1/2}}$$

Although other, more complex theories may describe the adsorption behavior in a particular system more accurately, the results obtained with the simple Langmuir theory should be representative and may be the most accurate in some cases, e.g., see Smith. (38) Examples of other types of models for hydrogen isotope adsorption on, and desorption from metals are those of Bucur, et al., (39) and Bucur (40) for adsorption of protium on palladium films. They considered multiple types of active sites and surface reactions and there are many other such treatments. The general approach to analyzing of adsorption or desorption-step-limited permeation processes by using more complex adsorption and desorption models is similar.

The listed assumptions imply that the permeation flux, when only tritium is present, is given by the Langmuir expression for the rate of desorption of tritium from the downstream barrier surface. The surface coverage in the absence of significant upstream surface adsorption and bulk barrier metal diffusive resistances is that corresponding to equilibrium with the upstream molecular tritium partial pressure. The rate expression is therefore:

$$J_{T_2} = \frac{k_{T_2\text{Ads}}(T) p_{T_2}}{\left\{ 1 + \left[\frac{k_{T_2\text{Ads}}(T)}{k_{T_2\text{Des}}(T) p_{T_2}} \right]^{1/2} \right\}^2}$$

A similar analysis based on the same assumptions when both tritium and protium are present can be summarized as follows. The rate expressions are of the form:

$$J_{T_2} = k_{T_2\text{Des}}(T) c_{T_2}^2 + \frac{1}{2} k_{HT\text{Des}}(T) \theta_{T_2} \theta_{H_2}$$

and the absorption equilibrium expressions are of the form:

$$k_{T_2\text{Ads}}(T) \theta_{T_2}^2 + \frac{1}{2} k_{HT\text{Des}}(T) \theta_{T_2} \theta_{H_2}$$

$$= k_{T_2\text{Ads}}(T) (1 - \theta_{T_2} - \theta_{H_2})^2 p_{T_2}$$

$$+ \frac{1}{2} k_{HT\text{Ads}}(T) (1 - \theta_{T_2} - \theta_{H_2})^2 p_{HT}$$

The preceding adsorption equilibrium expression and the gas-phase isotopic interchange equilibrium expression can be solved for the diatomic protium and tritium and HT partial pressures in terms of the protium and tritium atom fractions in the gas phase and of the total hydrogen isotope partial pressure, although the solution may have to be obtained by numerical techniques, and the results inserted into the rate expressions. The presence of the third hydrogen isotope, deuterium, and significant dissociation of the molecular species to form the atomic species in the gas phase further complicate the problem, but the same principles are applicable.

If the tritium is isotopically swamped with protium, we have:

$$p_{H_2} \approx p_{HT} \approx p_{T_2}, \theta_H \approx \theta_T$$

and the rate and adsorption equilibrium expressions become, respectively:

$$J_{T_2} = \frac{1}{2} k_{HT\text{Des}}(T) \theta_{T_2} \theta_{H_2} + J_{HT} k_{HT\text{Des}}(T) \theta_{HT}^2$$

and:

$$\frac{1}{2} k_{T_2\text{Des}}(T) \theta_{T_2} \theta_{H_2} + \frac{1}{2} k_{HT\text{Des}}(T) (1 - \theta_{H_2})^2 p_{HT}$$

Chapter, the role of government in foreign
affairs will be affected. The role of government
will be diminished by the introduction of
the market mechanism, so that the
effect of government intervention in
the economy will be reduced. This
will lead to a more open economy,
which will be more responsive to
international influences.

and differences in the two groups regarding rates
of initiation of the first child, the percentage
of the two groups having children.

RESULTS

INITIATION OF CHILDREN

Table 1 shows the initiation rates of children
in the two groups.

INITIATION RATES IN THE TWO GROUPS

The initiation rates of children in the two groups
are shown in Table 1. The initiation rate of children
in the group with a history of breast feeding
is significantly higher than that in the group
without a history of breast feeding. This
difference is statistically significant at the
0.05 level.

It is also evident from Table 1 that the initiation

INITIATION RATES

INITIATION RATES

of initiation is lower in the non-breast feeding group. The non-
breast feeding group has a higher rate of initiation of
children than the breast feeding group. The difference
is statistically significant at the 0.05 level.
This difference is statistically significant at the
0.05 level.

INITIATION RATES IN THE TWO GROUPS

INITIATION RATES

- If tritium recovery system performance is determined primarily by transport rates, then isotopic swamping probably is not cost-effective and may be completely useless.
 - If tritium recovery system performance is determined primarily by equilibrium considerations, then isotopic swamping may be cost effective, but there is no guarantee that this will be the case.
 - Isotopic swamping will either not significantly affect or will enhance the performance of barriers to tritium escape into the tritium loop for a specified tritium concentration level. The judgment of cost-effectiveness must, of course, involve consideration of changes in, e.g., required recovery system capacity, requirements for isotopic separation, benefits resulting from reductions in tritium inventories and in rates of escape of tritium into the tritium loop, effects on other fusion reactor systems, potential use of less expensive construction materials, or lower energy consumption, and so on, of a unit of recovery system capacity.
- (1028)
- Because of limitations imposed on the length of papers, we were unable to discuss the effects of the unavoidable presence of other hydrogen isotopes and of isotopic swamping on other fusion reactor tritium recovery systems and tritium migration mechanisms within and from fusion power plants. Examples of tritium recovery processes and migration mechanisms for which interesting analyses using similar methods can be performed include:
- the gas kinetic-limited permeation process discussed by Levin and Stickney,⁽⁶⁰⁾
 - the nonequilibrium permeation process described by Shepp and Stickney,⁽⁵¹⁾
 - high-temperature lithium distillation for tritium recovery suggested by Hile and Wu,⁽³¹⁾
 - the molten-salt extraction process for tritium recovery from liquid lithium described by Maroni, et al.,⁽⁵²⁾
 - permeation through potential nonmetallic materials of construction for fusion reactors,
- e.g., organic polymeric materials used for, e.g., gaskets and seals, and ceramics, such as those discussed by Fowler, et al.,⁽⁵³⁾ and oxide or other corrosion layers that are potentially useful as tritium barriers, as discussed by Strehlow and Savage,⁽⁵²⁾ and
- thermal diffusion processes discussed by Pendleton.⁽³⁰⁾

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C Concentration

D Diffusivity

D_e^{eff} Effective diffusivity of the cylinder

D^0 Standard-state free-energy change

H^0 Standard enthalpy change

H Permeation saturation and recovery rate

J_{tr}^{perm} Permeation current

K Adiabatic coefficient (state function)

$K_{tr,perm}$ Tritium permeability

L_s Surface layer thickness

R_s Siverts' law constant

R_s^0 Siverts' law desorption-adsorption constant

ρ Material or weight

Q_{tr}

Surface flow rates

P_{tr} Pressure

R_s Siverts' law exponential constant

r Adsorption or desorption rate

R Ideal gas constant

S^0 Standard entropy change

T Absolute temperature

T^0 Tritium recovery rate

X Mole fraction

y, y' Mole, atom fractions

Greek letters

δ Tritium window or permeation barrier thickness

γ Activity coefficient

θ Fractional surface coverage by adsorbed species

λ Tritium concentration (local)

ρ Density

ϵ Permeability