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DASH:

**A Multicomponent Time-Dependent Concentration
Diffusion with Radioactive Decay Program**

University of California



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DASH:

**A Multicomponent Time-Dependent Concentration
Diffusion with Radioactive Decay Program**

C. E. Apperson, Jr.*
C. E. Lee**
L. M. Carruthers

*Department of Nuclear Engineering, University of Virginia,
Charlottesville, VA 22903.

**Department of Nuclear Engineering, Texas A&M University,
College Station, TX 77843.

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DASH: A MULTICOMPONENT TIME-DEPENDENT CONCENTRATION DIFFUSION
WITH RADIOACTIVE DECAY PROGRAM

by

C. E. Apperson, Jr., C. E. Lee, and L. M. Carruthers

ABSTRACT

The multicomponent time-dependent diffusion with radioactive decay problem which arises in the study of high-temperature gas-cooled reactors fission product migration is solved in one-dimensional geometries. The spatial multicomponent diffusion operator is numerically represented by a conservative finite difference approximation. An analytic time-dependent solution is achieved using a matrix operator method. Comparisons of the analytic-numerical solution method with a variety of analytic solutions give excellent agreement. This solution technique has been incorporated into an algorithm for use in a computer code, DASH. The holdup of ^{90}Sr by graphite is calculated.

I. INTRODUCTION

Multicomponent time-dependent concentration diffusion and radioactive decay of isotopic species¹ is an important aspect of fission product migration and release from fuel particles and fuel elements in High-Temperature Gas-Cooled Reactors (HTGRs). Analysis techniques for solving these types of problems are well known,^{2,3} but are subject to time-step limitations to guarantee numerical accuracy and stability. These limitations are related to the magnitudes of the diffusion coefficients, decay constants, and spatial size of the system under consideration.

A one-dimensional analytic-numerical solution of this diffusion problem has been investigated. The diffusion operator is numerically approximated by a spatial finite-difference representation. The resulting time-dependent problem

is solved analytically using a matrix operator method.⁴ Comparisons to a number of known one-dimensional analytic solutions have been made. These comparison problems include the one specie and two species, two material slab, cylinder, and sphere.

In all instances considered, the agreement with analytic solutions is excellent, limited only by the accuracy limitations of the finite difference representation. The time-step limitation associated with other numerical solution methods has been eliminated.

This analytic-numerical technique has been utilized as the solution routine in a computer code, DASH, for solving the general problem of concentration diffusion with radioactive decay.

II. THEORY

The differential equation governing time-dependent multicomponent diffusion with radioactive decay is given by

$$\frac{\partial \vec{C}}{\partial t} = \nabla \cdot D \nabla \vec{C} - \lambda \vec{C} + \vec{S}, \quad (1)$$

where D is an $n \times n$ square positive definite diffusion matrix (cm^2/s), \vec{C} is an n -component column vector representing isotopic concentrations (atoms/cm^3), λ is the decay matrix including branching ratios⁵ ($1/\text{s}$), and \vec{S} is an n -component column source vector ($\text{atoms}/\text{cm}^3\text{s}$). Equation (1) is solved in one-dimensional geometries (slab, cylinder, or sphere) subject to the initial condition $\vec{C}(r, t) = \vec{C}(r, 0)$ and either homogeneous Newman ($D \nabla \vec{C} = 0$) or inhomogeneous or homogeneous Dirichlet ($\vec{C} = \vec{c}$ or $\vec{C} = 0$) boundary conditions.

A. Difference Equation Derivation

A finite-difference representation for the spatial diffusion operator is obtained by integrating Eq. (1) over a subvolume of a discrete mesh. Gauss' theorem, when applied to the integrated result, yields

$$V_k \frac{d}{dt} \vec{C}_k = -A_{k+1/2} \vec{J}_{k+1/2} + A_{k-1/2} \vec{J}_{k-1/2} - \lambda_k V_k \vec{C}_k + V_k \vec{S}_k. \quad (2)$$

In Eq. (2), \vec{C}_k is the concentration vector averaged over the k^{th} cell, V_k is the volume of the k^{th} cell (diagonal matrix), and $A_{k+1/2}$ and $\vec{J}_{k+1/2}$ are the area elements and current at the boundary between cell k

and $k \pm 1$. The cell-centered source vector averaged over the k^{th} computational cell is denoted by \vec{S}_k . The decay matrix in cell k , λ_k , is cell dependent only if neutron processes are included in addition to β decay.

The currents at the mesh boundaries, $\vec{J}_{k \pm 1/2}$, are evaluated in terms of the concentration vector

$$\vec{J}_{k \pm 1/2} = -D\nabla \vec{C}_{k \pm 1/2}. \quad (3)$$

The mesh spacing (Δr_k), area elements ($A_{k \pm 1/2}$), and volume elements (V_k) for cell k as a function of geometry are given in Table I. The notation used throughout this discussion is illustrated in Fig. 1.

In order to develop difference equations that will be amenable to concentration-dependent diffusion coefficients and concentration discontinuities, the representation⁶

TABLE I
GEOMETRIC VARIABLES

Geometry	Δr_k	$A_{k \pm 1/2}$	V_k
Slab	$r_{k+1/2} - r_{k-1/2}$	1	Δr_k
Cylinder	$r_{k+1/2} - r_{k-1/2}$	$2\pi r_{k \pm 1/2}$	$\pi(r_{k+1/2}^2 - r_{k-1/2}^2)$
Sphere	$r_{k+1/2} - r_{k-1/2}$	$4\pi r_{k \pm 1/2}^2$	$\frac{4\pi}{3}(r_{k+1/2}^3 - r_{k-1/2}^3)$

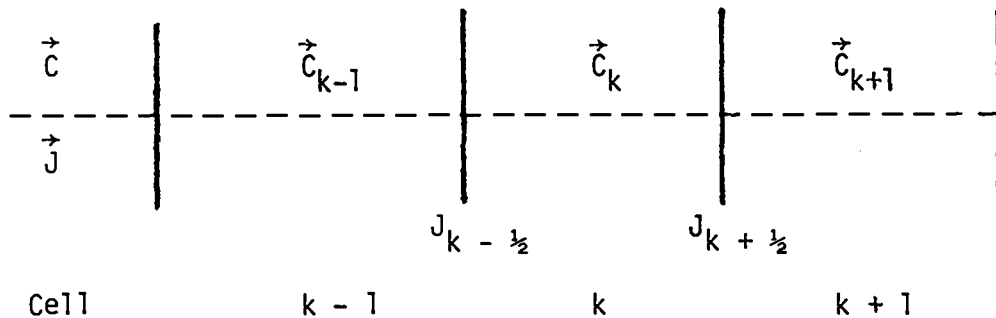


Fig. 1. Discrete mesh function representation.

$$\int_{r_k}^{r_{k+1/2}} \vec{J} dr = \int_{r_{k+1/2}}^{r_{k+1}} \vec{J} dr \quad (4)$$

is used or substituting - DVC for \vec{J} ,

$$\int_{c_k}^{c_{k+1/2}} D d\vec{C} = \int_{c_{k+1/2}}^{c_{k+1}} D d\vec{C} \quad , \quad (5)$$

For the case of continuity of concentration and concentration independent diffusion coefficients ($D \neq D(\vec{C})$), Eq. (5) yields

$$\vec{C}_{k+1/2} = (D_k + D_{k+1})^{-1} (D_k \vec{C}_k + D_{k+1} \vec{C}_{k+1}), \quad (6)$$

where D_k is the diffusion coefficient matrix in cell k. These assumptions are valid for the problem being studied.

Using Eq. (6) the current at the boundary $k + 1/2$ may be evaluated as

$$\begin{aligned} -\vec{J}_{k+1/2} &= 4 D_k (\vec{C}_{k+1/2} - \vec{C}_k) / (\Delta r_k + \Delta r_{k+1}) \\ &= 4 D_k (D_k + D_{k+1})^{-1} D_{k+1} (\vec{C}_{k+1} - \vec{C}_k) / (\Delta r_k + \Delta r_{k+1}) . \end{aligned} \quad (7)$$

Similarly, making the same argument for cells $(k-1, k)$,

$$-\vec{J}_{k-1/2} = 4 D_{k-1} (D_k + D_{k-1})^{-1} D_k (\vec{C}_k - \vec{C}_{k-1}) / (\Delta r_{k-1} + \Delta r_k). \quad (8)$$

Note that $(D_k + D_{k+1})^{-1}$ represents a matrix inverse of a positive definite diffusion coefficient matrix. Substituting Eq. (7) and (8) into Eq. (2) results in

$$V_k \frac{d\vec{C}_k}{dt} = \bar{A}_k \vec{C}_{k+1} + \bar{K}_k \vec{C}_k + \bar{B}_k \vec{C}_{k-1} + V_k \vec{S}_k, \quad (9)$$

where the coefficient matrices are given by

$$\begin{aligned} \bar{A}_k &= 4 A_k + 1/2 D_k (D_k + D_{k+1})^{-1} D_{k+1} / (\Delta r_k + \Delta r_{k+1}), \\ \bar{B}_k &= 4 A_k - 1/2 D_k - 1 (D_{k-1} + D_k)^{-1} D_k / (\Delta r_{k-1} + \Delta r_k), \text{ and} \\ \bar{K}_k &= -A_k - B_k - \lambda_k V_k. \end{aligned} \quad (10)$$

Since $\bar{A}_k = \bar{B}_k + 1$, a reciprocity relationship exists.⁷

The spatial boundary conditions treated are reflection ($\vec{J} = 0$), homogeneous Newman, and concentration specification, homogeneous and inhomogeneous Dirichlet.

For reflection at the left-hand side of the cell $k = 1$, \bar{B}_k is set to zero for $k = 1$. For reflection at the right-hand side of cell $k = K$, \bar{A}_k is set to zero for $k = K$ in Eq. (10). This procedure eliminates reference to either \vec{C}_0 or \vec{C}_{K+1} , and corresponds to a zero current boundary condition.

When the concentration is specified on the left-hand side of a slab or on the interior surface of a hollow cylinder or sphere, k is equal to $k_0 - 1/2$. A k_0 value of 1 corresponds to the first calculational cell in a slab but it corresponds to the central cell in a hollow cylinder or hollow sphere. In a hollow cylinder or sphere the first calculational cell is $k_0 = 2$. The left-hand current for both cases is given by

$$\vec{J}_{k_0 - 1/2} = 2 D_{k_0} \left(\vec{C}_{k_0} - \vec{C}_{k_0 - 1/2} \right) / \Delta r_{k_0}, \quad (11)$$

where the concentration vector $\vec{C}_{k_0 - 1/2}$ is specified. The right-hand current is given by Eq. (7) with $k = k_0$. From these results a modified set of coefficients for Eq. (9) can be evaluated

$$\bar{A}_{k_0} = 4 A_{k_0} + 1/2 D_{k_0} (D_{k_0} + D_{k_0+1})^{-1} D_{k_0+1} / (\Delta r_{k_0} + \Delta r_{k_0+1}),$$

$$\begin{aligned}\bar{B}_{k_0}' &= 2 A_{k_0} - 1/2 D_{k_0}/\Delta r_{k_0}, \\ \bar{K}_{k_0}' &= -\bar{A}_{k_0} - \bar{B}_{k_0}' - \lambda_{k_0} V_{k_0}.\end{aligned}\tag{12}$$

It should be noted that \bar{A}_k coefficients in Eqs. (10) and (12) are identical.

To account for the concentration diffusion of the material inside boundary 1, the source vector is modified.

$$V_{k_0} \vec{S}_{k_0}' = V_{k_0} \vec{S}_{k_0} + \bar{B}_{k_0}' \vec{C}_{k_0-1/2}.\tag{13}$$

Similarly, for concentration specified at the outside boundary of cell $k = K$, a modified set of coefficients for Eq. (9) must also be developed. In this case the \bar{B}_k coefficients are identical between Eq. (10) and Eq. (14).

$$\begin{aligned}\bar{A}_K' &= 2 A_K + 1/2 D_K/\Delta r_K, \\ \bar{B}_K &= 4 A_K - 1/2 D_K - 1 (D_{K-1} + D_K)^{-1} D_K/(\Delta r_{K-1} + \Delta r_K), \\ \bar{K}_K' &= -\bar{A}_K' - \bar{B}_K - \lambda_K V_K.\end{aligned}\tag{14}$$

In like manner, also the source vector must be modified to account for the concentration diffusion of the material specified on the outside boundary.

$$V_K \vec{S}_K' = V_K \vec{S}_K + \bar{A}_K' \vec{C}_K + 1/2.\tag{15}$$

The equations represented by Eqs. (9-10) and (12-15) may be written in supermatrix, supervector form as

$$V \frac{d}{dt} \vec{C} = A \vec{C} + V \vec{S},\tag{16}$$

where

$$\vec{c} = \begin{bmatrix} \bar{c}_1 \\ \bar{c}_2 \\ \cdot \\ \bar{c}_{K-1} \\ \bar{c}_K \end{bmatrix}, \quad \vec{s} = \begin{bmatrix} \bar{s}_1 \\ \bar{s}_2 \\ \cdot \\ \bar{s}_{K-1} \\ \bar{s}_K \end{bmatrix} \quad (17)$$

$$V = \begin{bmatrix} V_1 \\ & V_2 \\ & & \cdot \\ & & & \cdot \\ & & & & V_K \end{bmatrix} \quad (18)$$

and

$$A = \begin{bmatrix} \bar{K}_1 & \bar{A}_1 & & & \\ \bar{B}_2 & \bar{K}_2 & \bar{A}_2 & & \\ & & \cdot & & \\ & & & \cdot & \\ & & & & \bar{B}_{K-1} & \bar{K}_{K-1} & \bar{A}_{K-1} \\ & & & & \bar{B}_K & \bar{K}_K \end{bmatrix} \quad (19)$$

Equations (12) and (14) are included in \vec{s} for the first and/or last elements for the case of concentration specification at a boundary. The V_k in Eq. (18) are diagonal matrices of the form

$$V_k = I V, \quad (20)$$

where V is the scalar volume of the k^{th} cell and I is the n -dimensional identity matrix, where n is the number of nuclides in the radioactive decay chain. Each of the elements in A is an n -by- n matrix. The elements \bar{A}_k , \bar{B}_k , and \bar{K}_k are defined by Eq.s (10), (12), and (14).

B. Analytic Operator Solution

Although Eq. (16) could be solved by a standard implicit time-differencing technique,¹ such techniques are limited in time-step size by spectral considerations. Instead, an operator method is used.^{4,5}

By defining

$$\vec{X} = V\vec{C}, \quad \vec{g} = V\vec{S}, \quad \text{and} \quad B = AV^{-1} \quad (21)$$

and assuming A is constant over the interval $(0, t)$, Eq. (16) takes the form

$$\frac{d\vec{X}}{dt} = B\vec{X} + \vec{g}, \quad (22)$$

which has the solution^{4,5}

$$\vec{X}(t) = e^{Bt} \vec{X}(0) + tD(Bt) \vec{g}, \quad (23)$$

where

$$D(Bt) = (Bt)^{-1} (e^{Bt} - I), \quad (24)$$

and $X(0)$ is the vector of initial concentrations. Substituting Eq. (21) into Eq. (23), the solution to Eq. (16) is given by

$$\vec{C}(t) = V^{-1} e^{Bt} \vec{C}(0) + V^{-1} tD(Bt) V\vec{S}, \quad (25)$$

where $B = AV^{-1}$ (1/s) and V is a diagonal cell volume matrix. The details for evaluating the matrix operators e^{Bt} and $D(Bt)$ for arbitrary t are given in App. A.

III. VALIDATION AND ACCURACY EVALUATION

Although no experimental validation of DASH has been conducted, a substantial number of comparisons have been made to published analytic solutions. No attempt has been made to make all the possible comparisons, but a sufficient number of problems have been compared to establish confidence in the DASH methodology. For the problems considered, the observed errors are of the magnitude one would expect from a spatial finite-differencing technique. Some of these comparisons are discussed in detail. The test problems which are discussed were chosen because they point up unique features of the code.

A. One Material, One Specie Test Problems

The simplest problem type to utilize the full capabilities of the DASH code is the one material, one specie problem with concentration diffusion and radioactive decay. The one-dimensional geometry in the code permits the evaluation of problems involving an infinite slab, an infinite solid or hollow cylinder, and a solid or hollow sphere. The analytic solutions for comparison are taken from Crank⁸ and Carslaw and Jaeger.³ These published results are for concentration diffusion without radioactive decay or can be modified to fit this type of problem. A transformation developed by Danckwerts⁹ can be used to extend these results for time-dependent concentration diffusion to also handle radioactive decay. Danckwerts' transformation states that

$$C = \lambda \int_0^t C' e^{-\lambda t'} dt' + C' e^{\lambda t}, \quad (26)$$

where λ is the radioactive decay constant (1/s), C' is the diffusion solution without radioactive decay (atoms/cm³), t is the evaluation time (s), and C is the solution with both diffusion and decay (atoms/cm³). This transformation is valid for an initial concentration of zero, and boundary conditions of either surface-saturation or surface-resistance.

1. Slab Problem

The analytic solution for time-dependent concentration diffusion in a slab ($0 \leq x \leq \ell$) with a uniform initial distribution and different saturated surface concentrations is⁸

$$C' = C_1 + (C_2 - C_1) \frac{x}{\ell} + \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{C_2 \cos(n\pi) - C_1}{n} \sin \frac{n\pi x}{\ell} \exp \left(\frac{-Dn^2\pi^2 t}{\ell^2} \right) + \frac{4C_0}{\pi} \sum_{m=0}^{\infty} \frac{1}{2m+1} \sin \left(\frac{(2m+1)\pi x}{\ell} \right) \exp \left(\frac{-D(2m+1)^2\pi^2 t}{\ell^2} \right) \quad (27)$$

where C_0 is the initial uniform concentration, C_1 is the surface concentration at $x = 0$, C_2 is the surface concentration at $x = \ell$, D is the diffusion coefficient, and t is the evaluation time.

A simple one material, one specie infinite slab problem has been defined which can be solved both by Eqs. (26) and (27) and by DASH. The data for this problem is tabulated in Table II. The test problem was solved analytically at 27 space points at 5 different times. The DASH solution was for the same 5 times using 25 mesh cells. The maximum error observed occurred during the first time step, 0.1 days, at the center of the slab and had a magnitude of 0.28%. The magnitude of the error is defined to be the absolute value of the difference in the analytic and DASH results divided by the analytic result. The results are compared in Fig. 2. The figure resolution is such that the analytic and analytic-numerical, DASH, results fall on top of each other.

2. Cylinder Problems

a. Solid Cylinder. The time-dependent concentration diffusion problem for an infinite solid cylinder ($0 \leq r \leq a$) with a uniform initial distribution and a constant concentration at the outer radius is given analytically by⁸

TABLE II
DATA FOR VALIDATION TESTS

GEOMETRY	DIFFUSION COEFFICIENT (cm ² s ⁻¹)	DECAY CONSTANT (s ⁻¹)	UNIFORM INITIAL CONCENTRATION (atoms/cm ³)	BOUNDARY CONDITIONS		DIMENSIONS (cm)
				Left (atoms/cm ³)	Right (atoms/cm ³)	
Slab	7.234×10^{-6}	8.0225×10^{-7}	0.0	1.0×10^{10}	1.0×10^{10}	1 cm thick
Solid Cylinder	7.234×10^{-6}	8.0225×10^{-7}	0.0	REFLECTED	1.0×10^{10}	1 cm radius
Hollow Cylinder	7.234×10^{-6}	8.0225×10^{-7}	0.0	1.0×10^{10}	1.0×10^{10}	0.5 cm I.D., 2.0 cm o.d.
Solid Sphere	7.234×10^{-6}	8.0225×10^{-7}	0.0	REFLECTED	1.0×10^{10}	1 cm radius
Hollow Sphere	7.234×10^{-6}	8.0225×10^{-7}	0.0	1.0×10^{10}	1.0×10^{10}	0.5 cm I.D., 2.0 cm o.d.

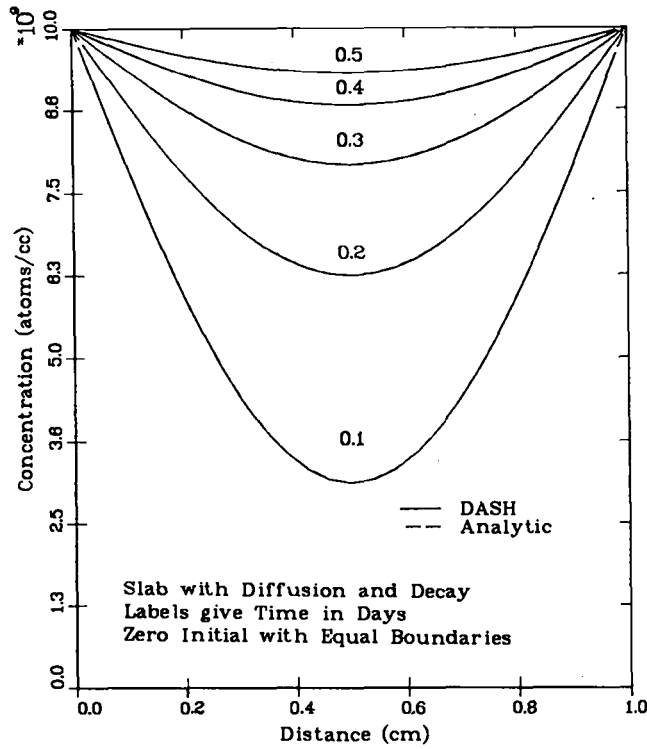


Fig. 2. Slab validation problem results.

$$C = C_1 + (C_0 - C_1) \frac{2}{a} \sum_{n=1}^{\infty} \frac{\exp(-D\alpha_n^2 t) J_0(r\alpha_n)}{\alpha_n J_1(a\alpha_n)}, \quad (28)$$

where C_0 is the initial uniform concentration, C_1 is the boundary concentration, D is the diffusion coefficient, and t is the evaluation time. The α_n 's are roots of the Bessel function of the first kind of order zero,

$$J_0(a\alpha_n) = 0, \quad (29)$$

where a is the cylinder radius. The problem defined in Table II for a solid cylinder can be solved both by Eqs. (26) and (28) and by DASH. The analytic solution was evaluated at 27 space points at 5 different times. The same 5 time points were used when the problem was solved using DASH with 25 mesh cells. The maximum observed error of 1.5%, the largest error for the one material, one specie problems studied, occurred at the center of the cylinder on the first time step, 0.1 days. The results, Fig. 3, from the two calculations again fall on top of each other due to the resolution limits of the graphic scales.

b. Hollow Cylinder. The analytic solution to the problem of flow through a cylinder wall ($a \leq r \leq b$) is⁸

$$C = \frac{C_1 \ln \frac{b}{r} + C_2 \ln \frac{r}{a}}{\ln (b/a)} + \pi C_0 \sum_{n=1}^{\infty} \frac{J_0(a\alpha_n) U_0(r\alpha_n) \exp(-D\alpha_n^2 t)}{J_0(a\alpha_n) + J_0(b\alpha_n)} \\ + \pi \sum_{n=1}^{\infty} \frac{\{C_2 J_0(a\alpha_n) - C_1 J_0(b\alpha_n)\} J_0(a\alpha_n) U_0(r\alpha_n)}{J_0^2(a\alpha_n) - J_0^2(b\alpha_n)} \exp(-D\alpha_n^2 t), \quad (30)$$

where C_0 is the initial uniform concentration, C_1 is the inner boundary concentration ($r = a$), and C_2 is the outer boundary concentration ($r = b$). The function U_0 is given by

$$U_0(r\alpha_n) = J_0(r\alpha_n) Y_0(b\alpha_n) - J_0(b\alpha_n) Y_0(r\alpha_n). \quad (31)$$

The values of α_n are the positive roots of

$$U_0(a\alpha_n) = 0, \quad (32)$$

where a is the inner radius and b is the outer radius of the hollow cylinder. The hollow cylinder problem solved both by Eqs. (26) and (30) and by DASH is stated in Table II.

Analytic solutions were evaluated at 26 space points at 5 different times. This problem was solved with DASH at the same 5 time points using 24 mesh cells. The maximum error observed was 0.24% and it was encountered at the first time step, 0.1 day. The error occurred at a point located a third of the way between the cylinder walls when measuring from the inside boundary. The results are illustrated in Fig. 4. It should be noted that the scaling of the ordinate is not the same as in the previous figures.

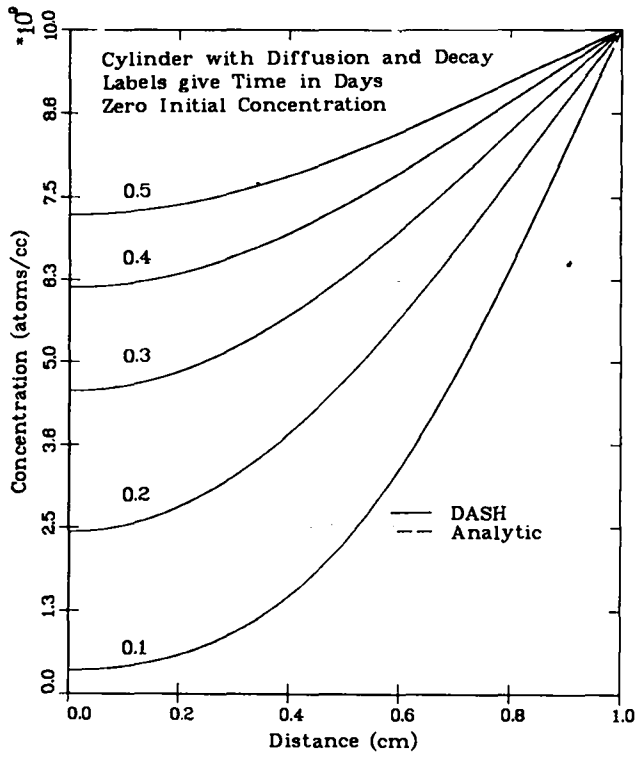


Fig. 3. Solid cylinder validation problem results.

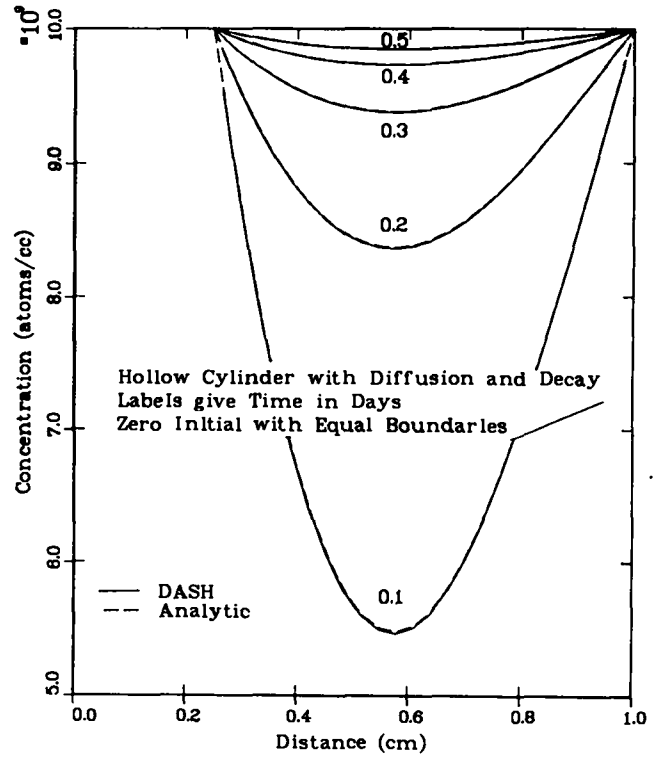


Fig. 4. Hollow cylinder validation problem results.

3. Spherical Problems

a. Solid Sphere. The problem of diffusion in a sphere ($0 < r \leq a$) has an analytic solution given by⁸

$$C = C_1 + (C_1 - C_0) \frac{2a}{\pi r} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \sin \frac{n\pi r}{a} \exp \left(\frac{-Dn^2\pi^2 t}{a^2} \right), \quad (33)$$

where C_0 is the initial uniform concentration, C_1 is the boundary concentration ($r = a$), and D is the diffusion coefficient.

Using the solid sphere data of Table II, this problem can be solved analytically by Eqs. (26) and (33) and numerically by DASH.

Analytic solutions were obtained at 27 space points for 5 time intervals. DASH solutions were calculated for the same 5 time intervals in 25 mesh cells. The maximum error for this set of problems was 0.93% and it occurred at the first time step, 0.1 days. This error was observed at a point $a/4$ from the sphere center. The analytic and DASH results are given in Fig. 5.

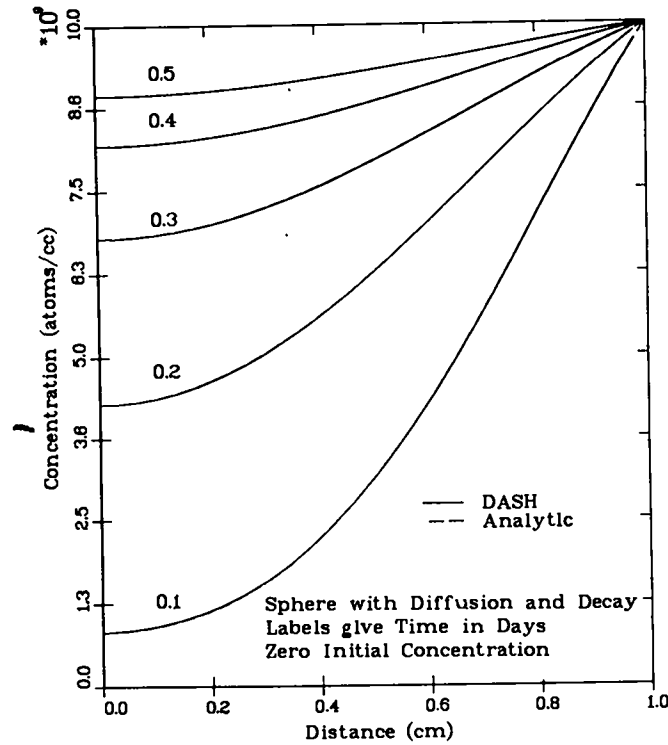


Fig. 5. Solid sphere validation problem results.

b. Hollow Sphere. The analytic solution for flow through a spherical wall ($a \leq r \leq b$) is⁸

$$C = \frac{aC_1}{r} + \frac{(bC_2 - aC_1)(r - a)}{r(b - a)} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{b(C_2 - C_0)\cos(n\pi) - a(C_1 - C_0)}{n} \sin \frac{n\pi(r - a)}{b - a} \exp \left(\frac{-Dn^2\pi^2 t}{(b - a)^2} \right), \quad (34)$$

where C_0 is the initial uniform concentration, C_1 is the boundary concentration at $r = a$, C_2 is the boundary concentration at $r = b$, and D is the diffusion coefficient.

The hollow sphere problem can be solved both by Eqs. (26) and (34) and by DASH.

The analytic results were evaluated at the 26 space points at 5 different times. The DASH solutions were for the same 5 time steps using 24 mesh cells.

A maximum error of 0.38% was observed at the first time step, 0.1 days, at a point located 20% of the way between the shell boundaries when measured from the inner wall. The calculated results are illustrated in Fig. 6.

B. Two Material, Two Specie Test Problems

Steady-state solutions can be readily obtained for the two-group neutron diffusion problem in reflected critical masses. One popular technique for solving these problems analytically is the critical determinant method.¹⁰ Using this approach, the critical radius of an infinite slab, infinite cylinder, or sphere can be evaluated. With this information the steady-state fast and thermal flux shapes in the fissile and reflector material can be determined.

The problem of neutron diffusion is extremely similar to the problems of concentration diffusion being studied. Because of this, the DASH code can be used to solve the two-group neutron diffusion problem with only minor modifications to the existing input routines. This is not to say that DASH can be used as a neutron diffusion code. DASH is optimized to solve Eq. (1) and lacks certain desirable characteristics for a production code for neutron diffusion.

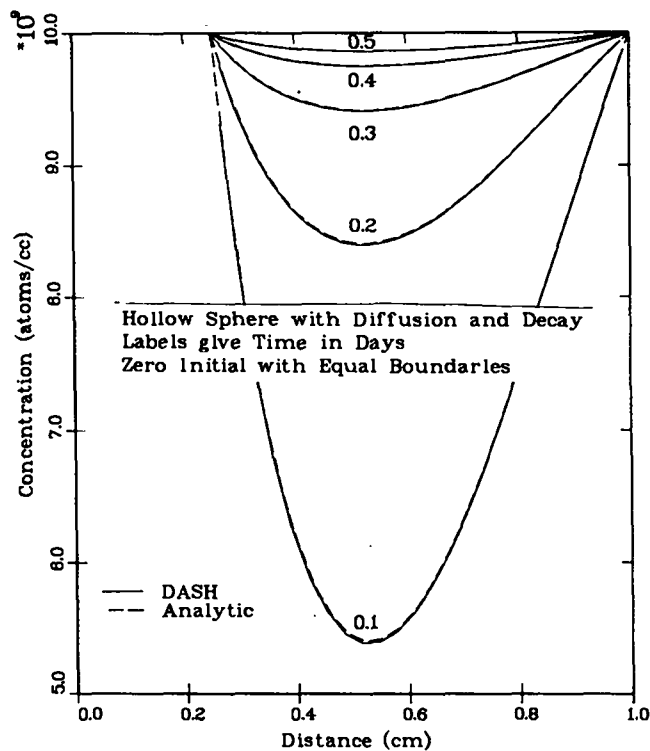


Fig. 6. Hollow sphere validation problem results.

The two-group neutron diffusion problem when set up in DASH produces full diffusion and decay matrices. This in conjunction with the two specie two-material nature of the problem provides an extensive test of the DASH code's ability to evaluate a steady-state solution. The test is further complicated by the need to reproduce the thermal flux peak. It is necessary to analytically determine the material interface for DASH, since it has no routines for evaluating the critical radius.

The basic data used in this series of problems is given in Table III. The k_{∞} is 1.388 9 and the reflector is always 25 cm thick.

1. Critical Slab

For the data given in Table III the half-thickness of a critical slab is 7.988 cm. Using the previously discussed analytic approach,¹⁰ the fast and thermal fluxes were calculated at 25 equally spaced points in material 1 and at 75 equally spaced points in material 2. More points were placed in material 2 to allow the thermal flux peak to be properly described. Numerical results were obtained with DASH using 12 mesh cells in material 1 and 38 mesh cells in material 2. These results are illustrated in Figs. 7 and 8.

The maximum error in the fast flux was 0.33% and the maximum thermal flux error was 0.60%. Both of these errors occurred in material 2 just after the material interface.

A further measure of the accuracy of the DASH results when compared to the analytic results is the fast-to-thermal flux ratio, Fig. 9. The ratio of the fast to thermal flux is plotted for both calculations. The maximum error observed in this ratio is 0.92% and it occurred in the same region as the other errors for this problem.

TABLE III
TWO GROUP VALIDATION TEST DATA

	Group 1		Group 2	
	Material 1	Material 2	Material 1	Material 2
Diffusion Coefficient (cm)	1.13	1.13	0.16	0.16
Absorption Cross-Section (cm ⁻¹)	0.0419	0.0419	0.06	0.0197
Fission Cross-Section (cm ⁻¹)	0.0	0.0	0.040258	0.0

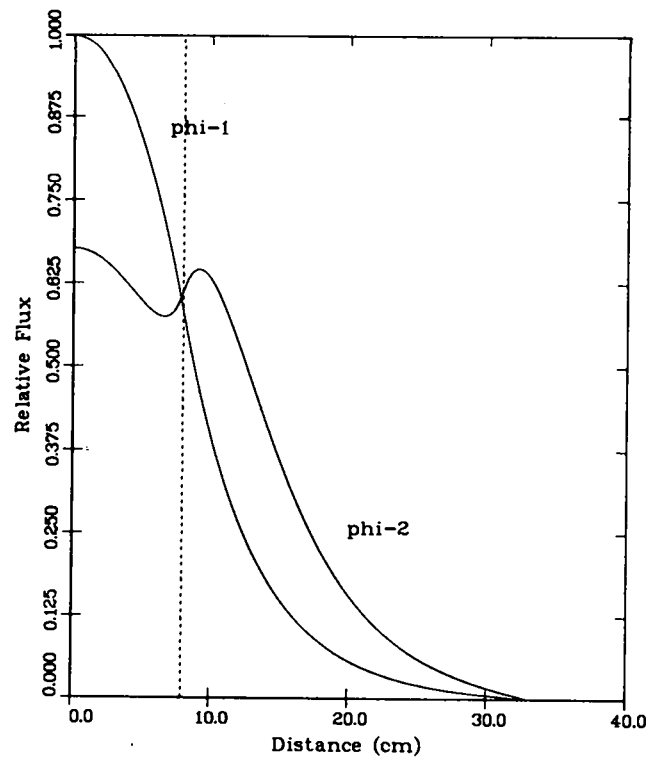


Fig. 7. Critical slab analytic results.

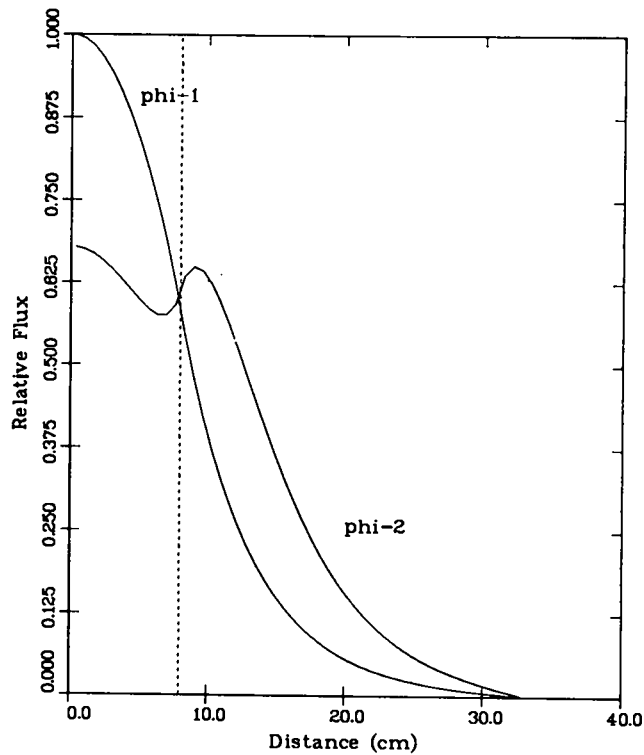


Fig. 8. Critical slab DASH results.

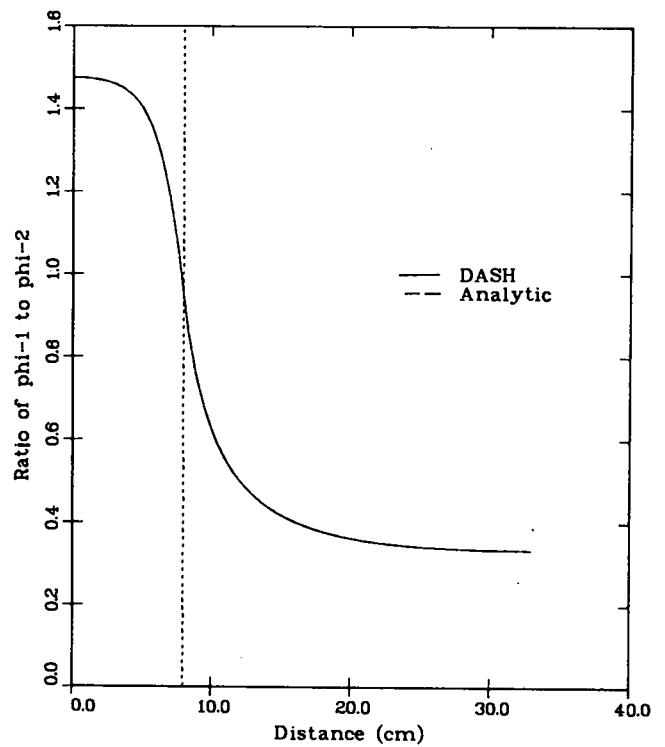


Fig. 9. Slab flux ratio comparison.

2. Critical Cylinder

The critical cylinder problem when solved using the data of Table III has a critical radius of 15.368 cm. An analytic evaluation of the fast and thermal flux was done at 25 space points in material 1 and at 75 space points in material 2. DASH results were obtained for 19 material-1 mesh cells and 31 material-2 mesh cells. These results are illustrated individually in Figs. 10 and 11. The maximum error in the fast flux occurred 40 cm from the cylinder centerline and had a magnitude of 0.58%. The maximum thermal flux error was 0.80% and occurred 15 cm from the centerline. As in the slab problem the fast-to-thermal flux ratios were also compared, Fig. 12. The largest error observed was 1.21%. This error occurred at a point essentially at the material interface.

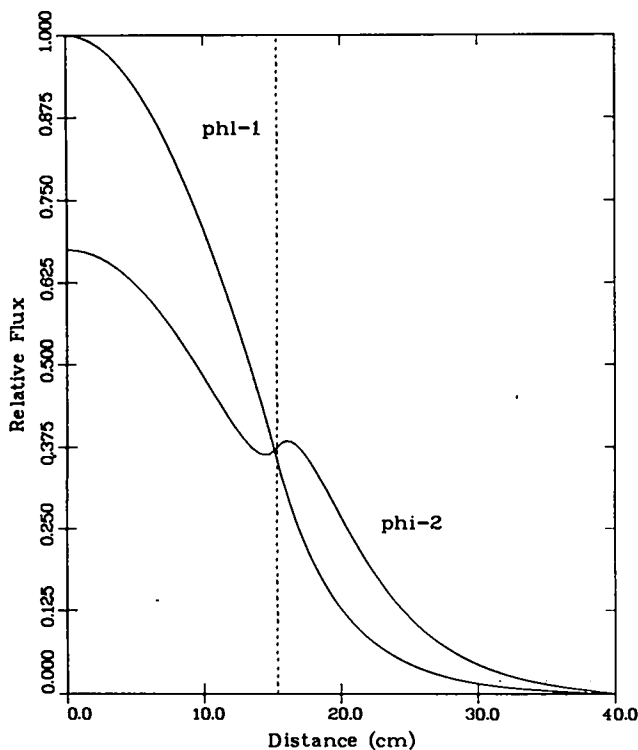


Fig. 10. Critical cylinder analytic results.

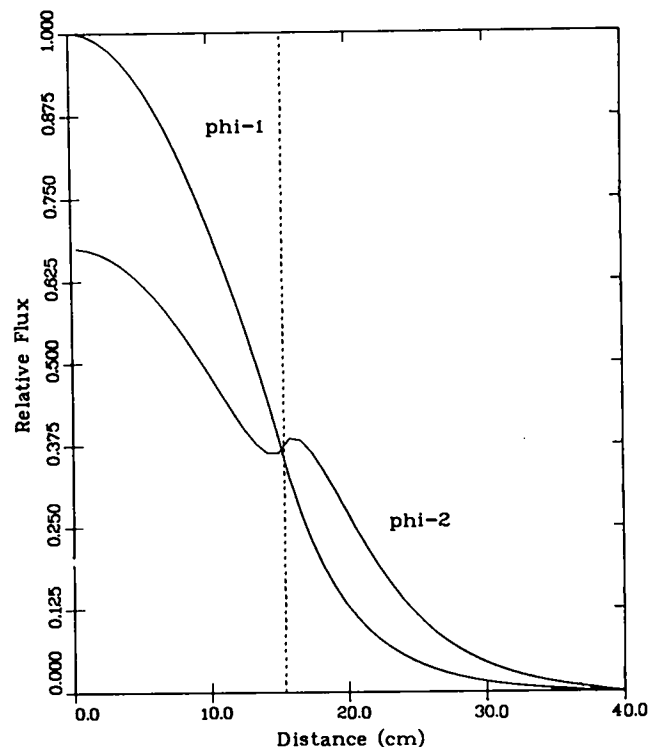


Fig. 11. Critical cylinder DASH results.

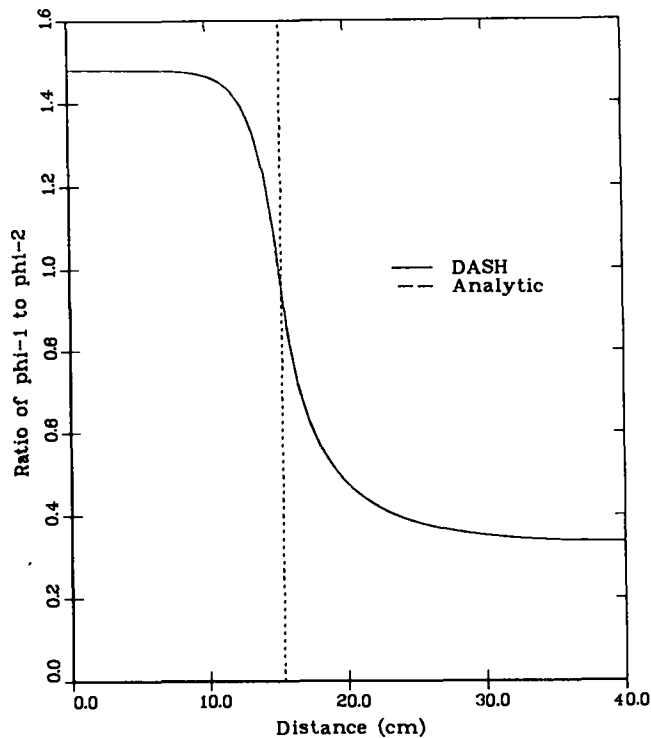


Fig. 12. Cylinder flux ratio comparison.

3. Critical Sphere

A critical radius of 21.91 cm is obtained when the Table III data is used to solve a spherical critical determinant problem. The analytically determined fluxes, Fig. 13, were evaluated at 25 space points in material 1 and at 75 space points in material 2. The DASH results, Fig. 14, were calculated based on 25 material-1 mesh cells and 25 material-2 mesh cells.

The maximum error for both flux groups occurred at the material interface. The largest fast flux error was 0.74% and the largest thermal flux error was 1.25%. The flux ratio comparison, Fig. 15, has its greatest error in material 2 near the material interface. The magnitude of this error is 0.97%.

C. Inherent Differencing Error

The DASH solution is obtained through the application of both analytic and numerical solution techniques. The procedure employed uses a matrix operator method to evaluate the time-dependent solution after the spatial variable has been differenced. The inherent error in the spatial differencing can be determined by expressing the difference equation with a Taylor's series.

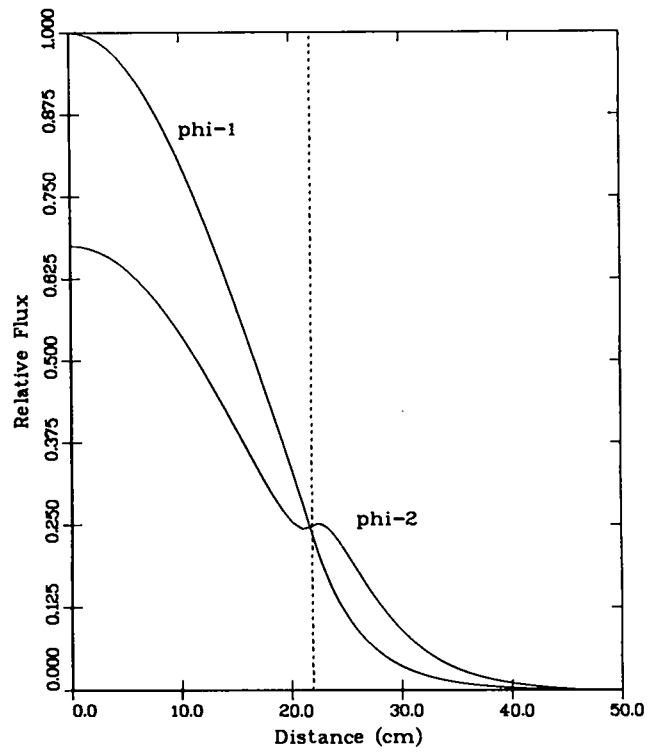


Fig. 13. Critical sphere analytic results.

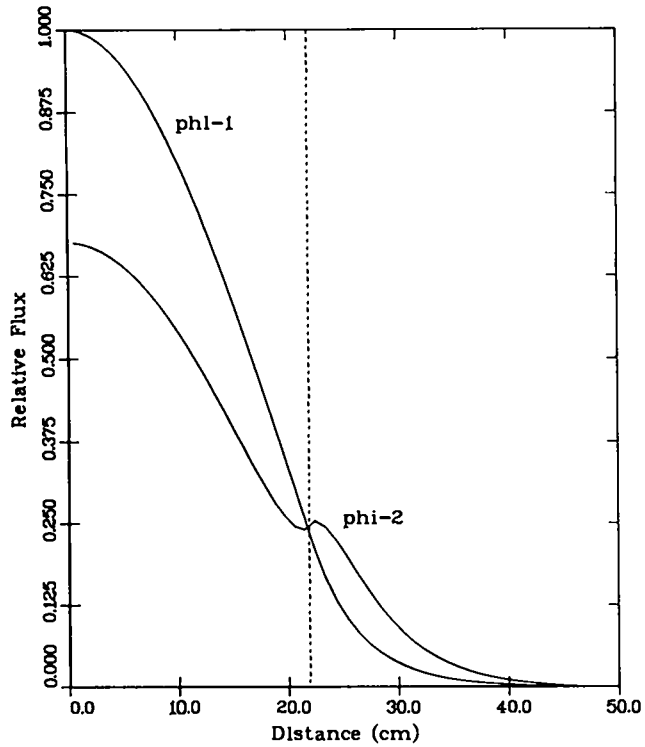


Fig. 14. Critical sphere DASH results.

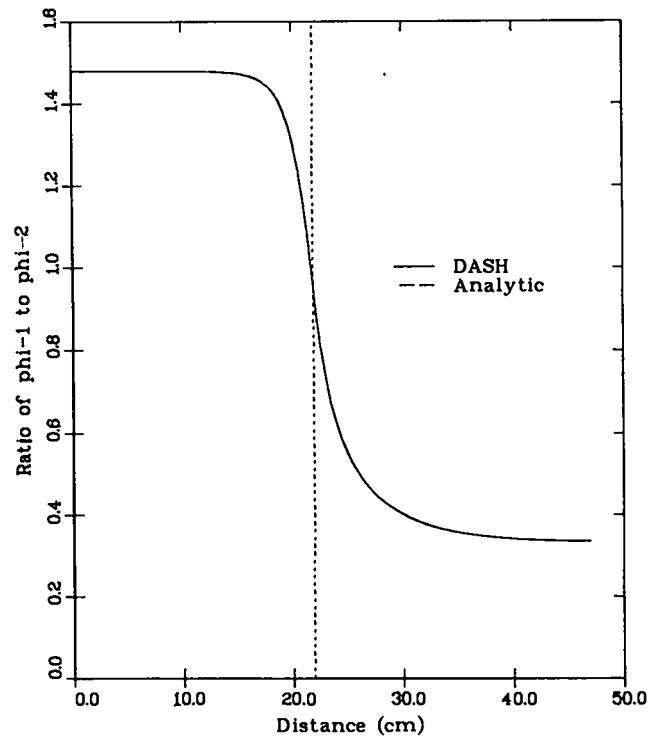


Fig. 15. Spherical flux ratio comparison.

From the Taylor's series representation, the inherent error can be represented by an even power series of h , the mesh spacing. When h is small, the principal error contribution comes from the h^2 term. Under these conditions, it is acceptable to assume that the inherent error due to spatially differencing Eq. (1) is proportional to h^2 .

$$\epsilon = kh^2, \quad (35)$$

where

ϵ = inherent error
 k = proportionality constant
 h = mesh spacing.

By substituting L/n for the mesh spacing in Eq. (35), where L is the thickness of the sample and n is the number of cells in L , a more general expression can be obtained.

$$\epsilon = (kL^2) \frac{1}{n^2}. \quad (36)$$

For a given geometry kL^2 is constant. The analytic-numerical DASH solution accuracy, therefore, should vary inversely with the square of the number of cells if the code is properly constructed.

As a test of this property, the slab problem of paragraph III,A,1 was evaluated at five different mesh sizes. The results of this exercise are given in Table IV and Fig. 16. The maximum observed error over five time steps was used in this study. One can see from Table IV that ϵn^2 is approximately constant.

TABLE IV
SPATIAL DIFFERENCING ERROR

n	ϵ	n^2	ϵn^2	Normalized ϵ
5	0.061320	25	1.53	1.000
10	0.016860	100	1.69	0.275
15	0.007778	225	1.75	0.127
20	0.004370	400	1.75	0.071
25	0.002820	625	1.76	0.046

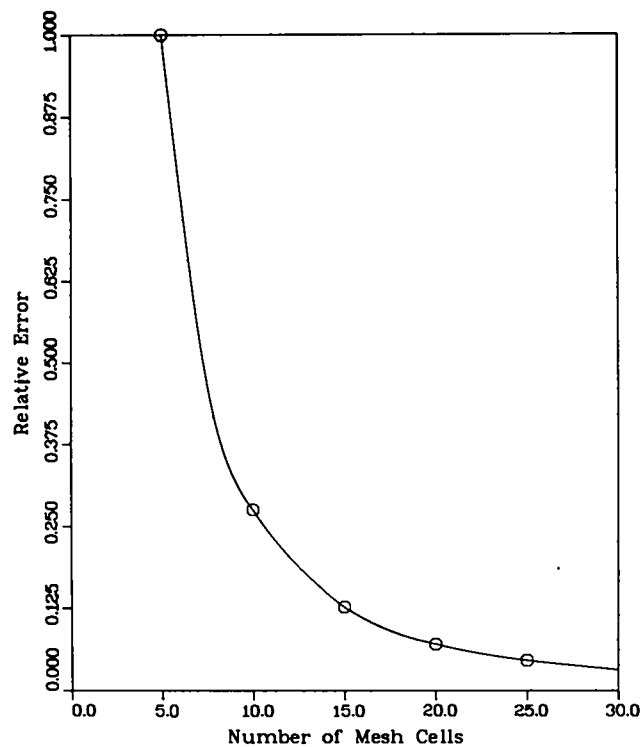


Fig. 16. Relative inherent differencing error.

D. Numerical Errors Associated with Matrix Inversion and Matrix Operator Solution

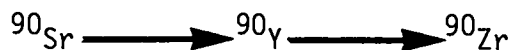
The basic equation to be solved [Eq. (16)] involves a supermatrix A given by Eq. (19) whose coefficients \bar{A} and \bar{B} depend on the inverse of the diffusion matrix [see Eq. (10)]. This inverse will be difficult to perform in some numerical situations. For submatrices with no off-diagonal terms this is not a problem, however.

The full set of equations involving the supermatrix is solved by a matrix operator method which involves summing the terms in the matrix as a first step. This sum is used to decide how many times the matrix should be divided by two to reduce the terms of the matrix to manageable size. If the matrix has a few very large terms, this method may cause the part of the solution which results from this operation to disappear. One type of problem which has this difficulty is one in which the cells are of very uneven sizes. The individual terms have Δr in the denominator and this causes the elements of the supermatrix to be large if the cell they refer to is small.

IV. HOLDUP OF ^{90}Sr BY GRAPHITE

A parameter study of the release and diffusion-decay of isotopes of strontium in a simplified one-dimensional slab model of an HTGR core block has been carried out. A typical element of the core block and the coolant hole was modeled as shown in Fig. 17; the dimensions of each region were taken from Ref. 11.

A decay chain used for the test problem is



with yields and decay constants shown in Table V. The boundary conditions used are reflection at $x = 0$, zero concentration at $x = 1.05$.

The approach is to use data from the work of Appel and Roos¹¹ and calculate the distribution of the isotopes of this decay chain in the fuel matrix and structural graphite. The source term for ^{90}Sr is taken to be 7.3×10^9 atoms/(cm³.s) as given in Ref. 11. The source terms for the other isotopes in the chain are taken in proportion to the yields of Table V.

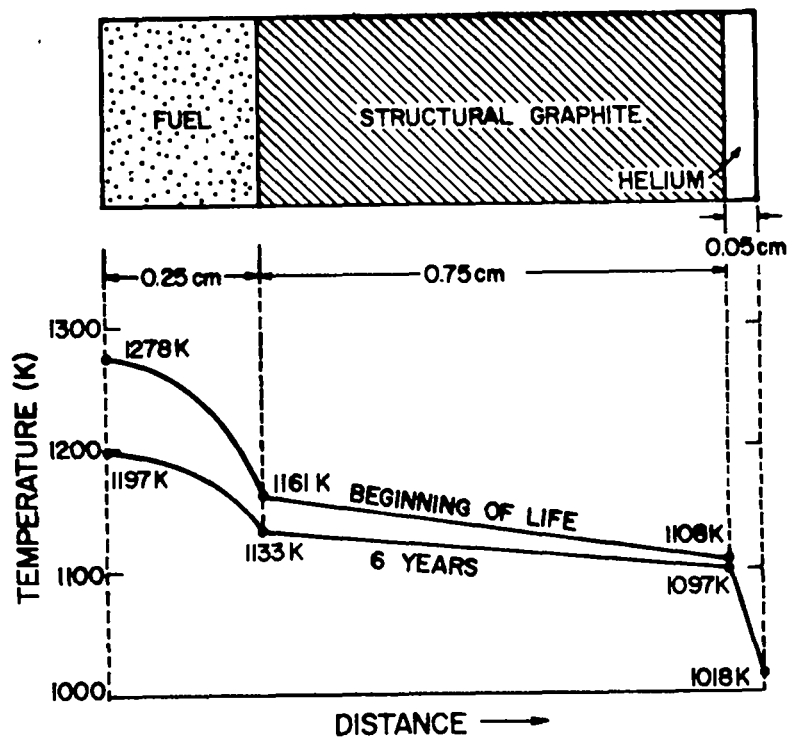


Fig. 17. Fuel-graphite-helium calculational model and beginning-of-life and six-year temperature profiles.

The temperature changes from the beginning to the end of the calculation (six years duration) are shown in Fig. 17. Temperatures at intermediate times are calculated by linear interpolation.

Data are given in Ref. 12 for the diagonal terms of the 3x3 diffusion matrix for the three species making up this problem. For the Arrhenius representation,

TABLE V
DATA FOR MASS-90 DECAY CHAIN

ISOTOPE	YIELD %	DECAY CONSTANT/s
^{90}Sr	5.77	7.844×10^{-10}
^{90}Y	5.77	2.994×10^{-6}
^{90}Zr	0.0	1.0×10^{-20}

$$-\log_{10} D = A + 1000 B/T,$$

(37)

the coefficients A and B are given in Table VI. The data were taken from Ref. 12.

Appel and Roos¹¹ assume that the concentration of ⁹⁰Sr drops by a factor of 300 at the fuel-graphite interface corresponding to the distribution coefficient between the two substances. This is handled in DASH by putting a small region (10⁻⁵ cm thick) at the boundary and adjusting the diffusion coefficient of the region introduced until the ratio of ⁹⁰Sr concentrations is 300. Except for this boundary region, the mesh spacing is taken as 0.05 cm throughout.

To compare with the work of Appel and Roos, the concentrations of ⁹⁰Sr were calculated at the end of one year using the diffusion coefficient data from Ref. 11 [A = -2.477 and B = 13.1 in Eq. (37)] and the data of Table VI for comparison. The comparisons are shown in Table VII.

TABLE VI
DIFFUSION COEFFICIENT PARAMETERS

<u>SPECIE</u>	<u>A</u>	<u>B</u>
⁹⁰ Sr	0.34	6.5
⁹⁰ Y	0.74	14.2
⁹⁰ Zr	1.19	22.8

TABLE VII
COMPARISON OF ⁹⁰Sr CONCENTRATIONS AT ONE YEAR

<u>POSITION</u> (cm)	<u>MATERIAL</u>	Results from Ref. 11 (atoms/cm ³)	<u>DASH Results</u>	
			<u>Ref. 11</u> <u>Coefficients</u>	<u>Ref. 12</u> <u>Coefficients</u>
0.125	Fuel	1.7 x 10 ¹⁸	2.27 x 10 ¹⁷	1.80 x 10 ¹⁷
0.30	Graphite	3.0 x 10 ¹⁵	5.41 x 10 ¹⁴	5.68 x 10 ¹⁴
0.50	Graphite	6.0 x 10 ¹⁴	1.06 x 10 ¹⁴	4.30 x 10 ¹⁴
0.75	Graphite	1.0 x 10 ¹³	4.62 x 10 ¹²	2.23 x 10 ¹⁴

It is apparent in looking at Table VII that the ^{90}Sr concentration in the fuel matrix as given by Appel and Roos is larger than that which a source of $7.3 \times 10^9 \text{ atoms}/(\text{cm}^3 \cdot \text{s})$ would produce in one year with no diffusion. Further investigation leads us to believe that Appel and Roos used a source of 7.3×10^{11} which probably explains the difference between DASH and the Appel and Roos results.

A more realistic treatment of the source¹³ allows for an increased source strength in later years caused by an increase in fuel particle failure rates. We assumed that the initial source ($S_0 = 7.3 \times 10^9 \text{ atoms}/\text{cm}^3 \cdot \text{s}$) increases with time such that S_0 is used for the first year, $2S_0$ for the second year, $3S_0$ for the third year, etc. Numerical results for ^{90}Sr concentration are listed in Table VIII and shown in Fig. 18. The diffusion coefficient data of Table VI was employed in this calculation. The ^{90}Y concentration profiles are shown in Fig. 19. Comparison of the amount of ^{90}Sr produced with amount retained is the fuel and structural graphite indicates that even at six years almost half of this species is held up by the presence of the graphite. On the other hand, the ^{90}Y does not diffuse significantly but decays into ^{90}Zr .

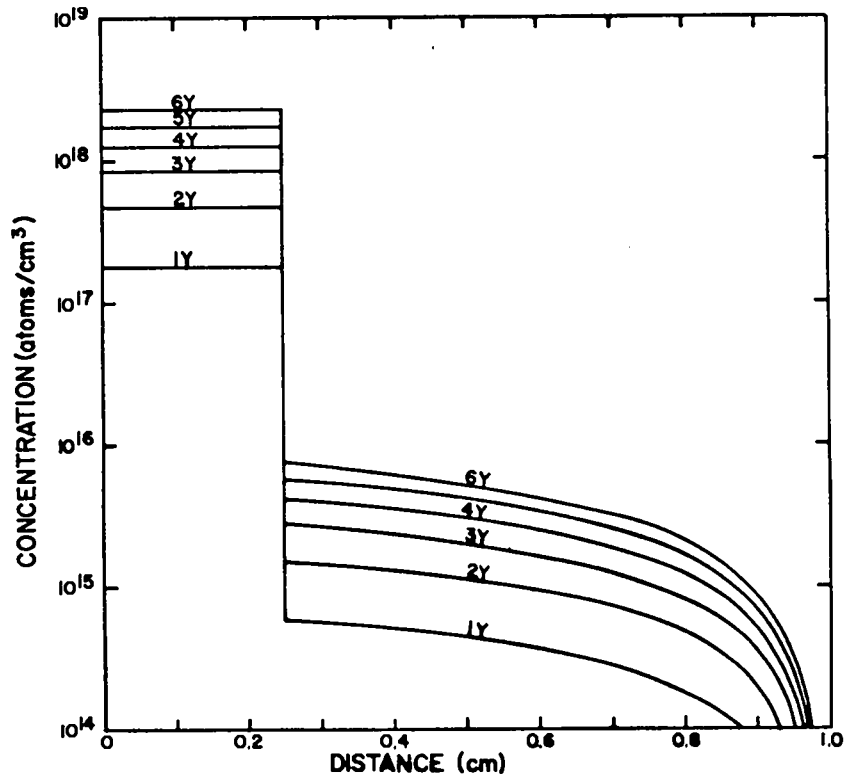
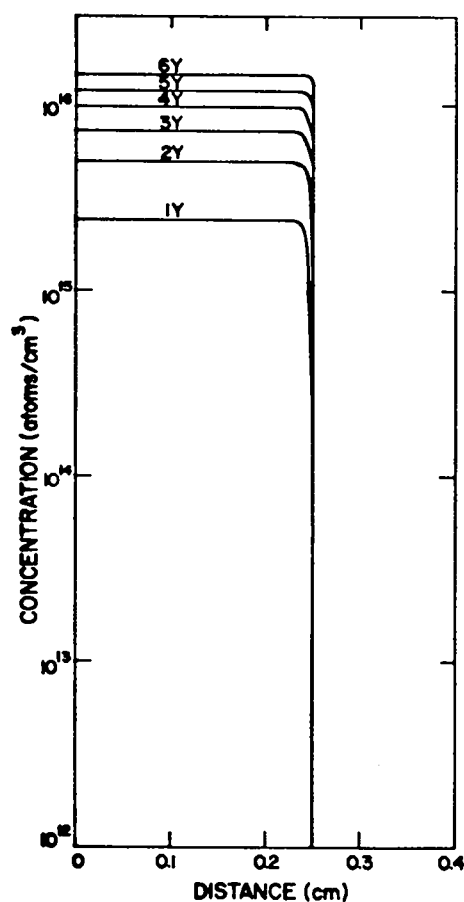


Fig. 18. ^{90}Sr concentration profiles.

TABLE VIII

 ^{90}Sr CONCENTRATION IN FUEL MATRIX WITH INCREASING SOURCE

Time (y)	Total Source Units	Fuel Concentration (atom/cm ³)	Fuel Concentration if no Diffusion (atom/cm ³)	Fraction Retained
1	1	1.80×10^{17}	2.30×10^{17}	0.78
2	1 + 2 = 3	4.74×10^{17}	6.91×10^{17}	0.69
3	3 + 3 = 6	8.45×10^{17}	1.38×10^{18}	0.61
4	4 + 6 = 10	1.27×10^{16}	2.30×10^{18}	0.55
5	5 + 10 = 15	1.75×10^{18}	3.46×10^{18}	0.51
6	6 + 15 = 21	2.27×10^{18}	4.84×10^{18}	0.47

Fig. 19. ^{90}Y concentration profiles.

V. PROGRAM STRUCTURE

A. Role and Function of Subroutines

The DASH program consists of a driver routine, DASH1, and 34 functions and subroutines. The functions and subroutines can be divided into three classifications: primary, secondary, and graphic. The primary routines are those that are called directly by the controlling routine, DASH1, and perform major tasks. The secondary routines are utility routines called by the primary subroutines that do vector and matrix operations and function evaluations. The graphic routines are available for the generation of plots on 35-mm film.

1. Primary Routines

The 15 primary routines are discussed in the order in which they are called by DASH1.

a. INPA. The subroutine INPA reads and prints the basic nuclear data used in constructing the radioactive decay chain matrix. The input is stored locally so that it is readily available for subsequently called routines.

b. INPB. The subroutine INPB reads and prints the problem-dependent data.

c. GEOM. The subroutine GEOM calculates the geometric information required by the solution routines. From data supplied in INPB, this routine evaluates the mesh cell dimensions, area, and volume.

d. TEMADJ. The routine TEMADJ takes the temperature data supplied in INPB and fits it to a spline. From the fit, the routine calculates effective mesh cell temperatures for all the cells in the problem.

e. INPLT. The routine INPLT displays the calculational cells graphically. The mesh cells are illustrated with boundary condition and dimensional data. The purpose of this routine is to facilitate the debugging of the geometric input.

f. DIJADJ. The routine DIJADJ use the Arrhenius relation to temperature correct the input diffusion coefficients on a cell-by-cell basis. The temperatures calculated in TEMADJ are used along with the activation energies and diffusion coefficients read by INPB.

g. BCONL. The routine BCONL is used to establish the left-hand spatial boundary condition. Based on input data a modified value of \bar{B}_k , Eq. (12), is evaluated for Eq. (9). The modified source, Eq. (13), due to the left boundary is also determined in this routine.

h. MAKLAM. The routine MAKLAM utilizes the nuclear data from INPA to construct the radioactive decay matrix, Eq. (2).

i. BIGEL. The routine BIGEL constructs all the matrices necessary for the matrix A, Eq. (19), except \bar{K}_k . This determination is carried out on a cell-by-cell basis.

j. MAKEB. The routine MAKEB assembles the matrix B. It takes the matrices created by BIGEL, multiplies them by the inverse volume element matrix, and inserts them in the matrix B.

k. BCONR. The routine BCONR is used to establish the right-hand spatial boundary condition. Based on input data a modified value of \bar{A}_k , Eq. (14), is evaluated for Eq. (9). The modified source, Eq. (15), due to the right boundary is also determined in this routine.

l. SOLVER. The subroutine SOLVER operates on the matrix generated by MAKEB to calculate the two matrix operators, $D(Bt)$ and e^{Bt} . The recursion relations discussed in App. A are part of this routine.

m. MAKVOL. The routine MAKVOL assembles the diagonal volume element matrix, Eq. (20), used in FSOLVE.

n. FSOLVE. The subroutine FSOLVE uses the operators calculated in SOLVER, the initial concentration vector, and the diagonal volume matrix to evaluate the time-dependent spatial concentrations according to Eq. (25). This routine is evaluated for each time interval specified in INPB.

o. CONCPLT. The routine CONCPLT prints the results from FSOLVE in a detailed manner as a function of time and space point in either terminal or line printer format.

2. Secondary Routines

There are 14 secondary routines in DASH. These routines do utility operations such as vector and matrix operations, curve fitting, and function evaluation.

- a. The general mathematic routines are listed below.
 - SCALAR - Multiplies a local matrix by a scalar.
 - SCAECS - Multiplies an extended core storage matrix by a scalar.
 - IFACT - Evaluates factorials.
 - GENID - Generates an identity matrix.
 - MATMOV - Equivalences two local matrices.
 - MOVECS - Equivalences two extended core storage matrices.

- MATMPY - Multiplies combinations of local vectors and local matrices.
 - MPYEC3 - Multiplies combinations of extended core storage vectors and matrices.
 - MPYEC1 - Multiplies combinations of local and extended core storage vectors and matrices.
- b. The specialized input and output routines are listed below.
- PRIM - Prints a local matrix.
 - PRIMES - Prints an extended core storage matrix.
 - PRIV - Prints a local vector.
 - REAG - Reads floating point data.
 - REAI - Reads integer data.
- c. There is one special purpose secondary routine.
- WXSEC - Collapses multigroup cross sections by flux weighting.

3. Graphics

The graphic routines generate 35-mm-film output in the form of plots of the calculated results for each time step in the problem. The plots make use of the DISSPLA* system which should facilitate the transfer to other computer centers. The plotting is done entirely in subroutine DRAW. The plots can be deleted without affecting the remainder of the code.

- DRAW - Controls the plotting of time-dependent results.

The DISSPLA routines employed are

- GPLOT - Device-independent initialization routine.
- BGNPL - Begins a plot.
- HEIGHT - Sets the basic character height.
- TITLE - Draws axes and titles.
- GRAF - Scales axes.
- CURVE - Draws a curve.
- ENDPL - Ends a plot.
- DONEPL - Plot termination.

* DISSPLA is a proprietary software product developed by Integrated Software Systems Corporation, San Diego, CA. It is available at about 200 computer installations.

B. Program Flow

The flow of the DASH program is illustrated in Fig. 20. The name of the primary subroutine involved in a given step is enclosed by parenthesis.

C. DASH Input Instructions

The DASH input is contained in 17 cards which are divided into 4 sets. The first set consists of card 0, which establishes the print options. The second set consists of cards 1 and 2 and defines the nuclear decay chains.

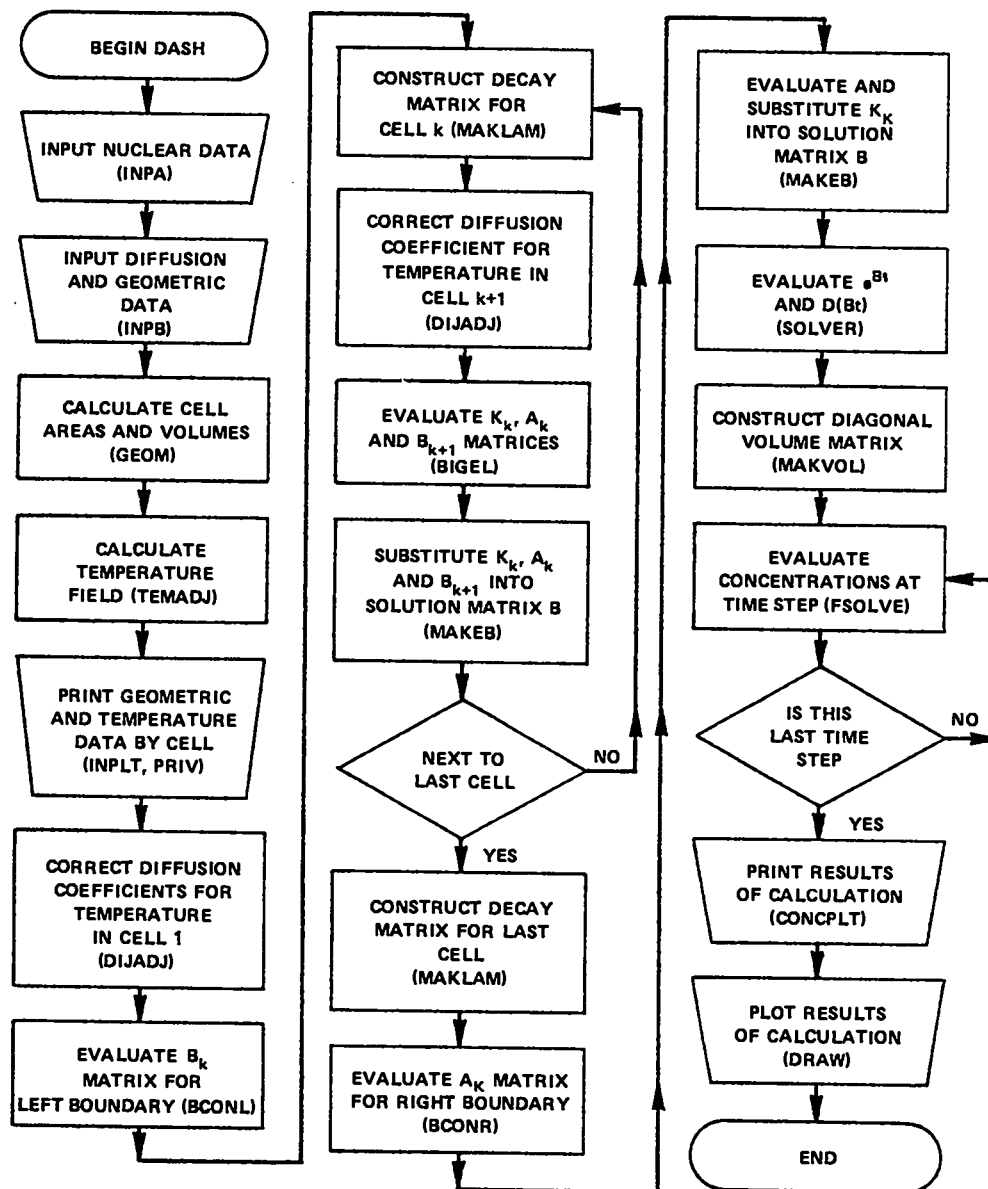


Fig. 20, DASH flow diagram.

Cards 3 and 4 compose the third card set, which contains the multigroup cross-section data. The fourth set, cards 5-16, defines the physical characteristics of the system being evaluated.

The specific data for the four sets are detailed in Table IX. The user should note that if words 3 and/or 4 of card 1 are negative, 1 or 2 branching ratio cards, card 2 must follow card 1 before the next card 1. It should also be noted that cards 2 and 3 and cards 4 and 5 are separated by a blank card.

The diffusion coefficients are input as two matrices DIJO and AIJS. The full diffusion coefficients are:

$$D = D_0 e^{-\frac{A}{RT}} \quad (38)$$

$$= DIJO * EXP(- AIJO / (R * T))$$

for each element of DIJO and AIJO. Values must be supplied for each isotope in each material.

TABLE IX
DASH INPUT INSTRUCTIONS

CARD	WORD	SYMBOL	FORMAT	DESCRIPTION
0				PRINT OPTIONS
	1	NPRINT	I4	0/1 LINE PRINTER/TERMINAL
	2	NPLOT	I4	0/1 NO PLOT/PLOT
1	-ONE CARD PER NUCLIDE -			BASIC NUCLIDE DATA
	1	NANMAT(I,1)	A7	NUCLIDE NAME
	2	NANMAT(I,2)	I4	ID NUMBER
	3	NANMAT(I,3)	I4	DECAY PARENT 1
	4	NANMAT(I,4)	I4	DECAY PARENT 2
	5	NANMAT(I,5)	I4	CAPTURE PARENT 1
	6	NANMAT(I,6)	I4	CAPTURE PARENT 2
	7	NANMAT(I,7)	I4	N-2N PARENT
	8	NANMAT(I,8)	I4	N-ALPHA PARENT
	9	NANMAT(I,9)	I4	N-P PARENT
	10	ANMAT (I,1)	E12.5	DECAY CONSTANT (1/s)
2	-ONE CARD PER BRANCH FOR EACH NEGATIVE VALUE OF NANMAT(I,3-4)-			BRANCHING RATIO
	1	BRV(IBR)	E12.5	BRANCHING RATIO
-- BLANK CARD AFTER LAST SET OF CARDS 1 and 2 -- ISO = NUMBER OF NUCLIDE CARDS				
3				CROSS SECTION TITLE CARD
	1	NXSEC(II,1)	A6	TITLE 1
	2	NXSEC(II,2)	A6	TITLE 2
	3	NXSEC(II,3)	I4	NUMBER OF GROUPS
	4	NXSEC(II,4)	I4	NUCLIDE ID
4	-NXSEC(II,3) CARDS-			CROSS SECTION DATA
	1	XSEC(II,KX,1)	E12.5	MICROSCOPIC CROSS SECTIONS (cm ²) SIGMA N-GAMMA SIGMA N-2N SIGMA N-ALPHA SIGMA N-P
	2	XSEC(II,KX,2)	E12.5	
	3	XSEC(II,KX,3)	E12.5	
	4	XSEC(II,KX,4)	E12.5	

TABLE IX (cont)

CARD	WORD	SYMBOL	FORMAT	DESCRIPTION
--BLANK CARD AFTER LAST SET OF CARDS 3 and 4--				
5				PROBLEM RELATED DATA
	1	NCELLS	I4	Number of cells in problem
	2	NGEOM	I4	1/2/3 Slab/Cylinder/Sphere
	3	NBCL	I4	Left boundary condition 1/2 re- flected/concentration specified
	4	NBCR	I4	Right boundary condition 1/2 re- flected/concentration specified
	5	NTEMPS	I4	Number of entries for specifying temperature field
	6	IMATS	I4	Number of materials
	7	IGP	I4	Number of neutron energy groups
6				TIME STEP DATA
	1	TINT	E12.6	Initial time (days)
	2	TINC	E12.6	Number of time steps
	3	TIMAX	E12.6	Time at end of problem (days)
7				DIMENSIONS
	1	DIST(1)	SPECIAL	0.0
	2	DIST(2)	SPECIAL	First cell right boundary (cm)
	3	DIST(3)	SPECIAL	Second cell right boundary (cm)
	NCELLS+1	DIST(NCELLS+1)	SPECIAL	Last cell right boundary (cm)
8				ASSIGN MATERIALS
	1	MATS(1)	SPECIAL	Material ID for cell 1
	2	MATS(2)	SPECIAL	Material ID for cell 2
	.			
	.			
	NCELLS	MATS(NCELLS)	SPECIAL	Material ID for cell NCELLS
9				Dependent value for temperature field
	1	TEMPS(1)	SPECIAL	Temperature 1 (K)
	2	TEMPS(2)	SPECIAL	Temperature 2 (K)
	NTEMPS	TEMPS(NTEMPS)	SPECIAL	Temperature NTEMPS (K)
10				Independent value for temperature field
	1	TEMCOR(1)	SPECIAL	Coordinate of temperature 1 (cm)
	2	TEMCOR(2)	SPECIAL	Coordinate of temperature 2 (cm)
	NTEMPS	TEMCOR(NTEMPS)	SPECIAL	Coordinate of temperature NTEMPS (cm)

TABLE IX (cont)

CARD	WORD	SYMBOL	FORMAT	DESCRIPTION
11	- One set of cards 11 and 12 for each of IMATS materials -			Diffusion Matrix (cm^2/s)
	1	DIJO(1,1,1)	SPECIAL	Material 1 element (1,1)
	2	DIJO(2,1,1)	SPECIAL	Material 1 element (1,2)

	ISO	DIJO(ISO,1,1)	SPECIAL	Material 1 element (1,ISO)
	ISO + 1	DIJO(1,2,1)	SPECIAL	Material 1 element (2,1)

	ISO*ISO	DIJO(ISO,ISO,1)	SPECIAL	Material 1 element (ISO,ISO)
	ISO*ISO+1	DIJO(1,1,2)	SPECIAL	Material 2 element (1,1)

	ISO*ISO*N	DIJO(ISO,ISO,N)	SPECIAL	Material N element (ISO,ISO)
12	- One set of cards 11 and 12 for each of IMATS materials			Activation Energy Matrix(cal/mole)
	1	AIJS(1,1,1)	SPECIAL	Material 1 element (1,1)
	2	AIJS(2,1,1)	SPECIAL	Material 1 element (1,2)

	ISO	AIJS(ISO,1,1)	SPECIAL	Material 1 element (1,ISO)
	ISO + 1	AIJS(1,2,1)	SPECIAL	Material 1 element (2,1)

	ISO*ISO	AIJS(ISO,ISO,1)	SPECIAL	Material 1 element (ISO,ISO)
	ISO*ISO+1	AIJS(1,1,2)	SPECIAL	Material 2 element (1,1)

	ISO*ISO*N	AIJS(ISO,ISO,N)	SPECIAL	Material N element (ISO,ISO)
13	- One continuous set of card 13 for IGP groups -			Fluxes
	- Supply only if cross sections are present -			
	1	PHI(1,N)	SPECIAL	Group N flux in cell 1($\text{n}/\text{cm}^2\text{-s}$)
	2	PHI(2,N)	SPECIAL	Group N flux in cell 2($\text{n}/\text{cm}^2\text{-s}$)

	NCELLS	PHI(NCELLS,N)	SPECIAL	Group N flux in cell NCELLS ($\text{n}/\text{cm}^2\text{-s}$)
	NCELLS + 1	PHI(1,N+1)	SPECIAL	Group N + 1 flux in cell 1 ($\text{n}/\text{cm}^2\text{-s}$)

TABLE V Continued

TABLE IX (cont)

CARD	WORD	SYMBOL	FORMAT	DESCRIPTION
14	- Supply only if NBCL = 2			Left boundary concentrations
	1	CONBOU(1,1)	SPECIAL	Specie 1 left boundary concentration (atoms/cc)
	2	CONBOU(2,1)	SPECIAL	Specie 2 left boundary concentration (atoms/cc)
	ISO	CONBOU(ISO,1)	SPECIAL	Specie ISO left boundary concentration (atoms/cc)
15	- Supply only if NBCR = 2 -			Right boundary concentrations
	1	CONBOU(1,2)	SPECIAL	Specie 1 right boundary concentrations (atoms/cc)
	2	CONBOU(2,2)	SPECIAL	Specie 2 right boundary concentrations (atoms/cc)
	ISO	CONBOU(ISO,2)	SPECIAL	Specie ISO right boundary concentrations (atoms/cc)
16				Initial concentration
	1	CONINT(1)	SPECIAL	Initial concentration cell 1 specie 1 (atoms/cc)
	2	CONINT(2)	SPECIAL	Initial concentration cell 1 specie 2 (atoms/cc)
	ISO	CONINT(ISO)	SPECIAL	Initial concentration cell 1 specie ISO (atoms/cc)
	ISO + 1	CONINT(ISO+1)	SPECIAL	Initial concentration cell 2 specie 1
	ISO*NCELLS	CONINT(ISO*NCELLS)	SPECIAL	Initial concentration cell NCELLS specie ISO
17	1	SOURCE(1)	SPECIAL	Source cell 1 specie 1(atoms/s)
	2	SOURCE(2)	SPECIAL	Source cell 1 specie 2(atoms/s)
	ISO	SOURCE(ISO)	SPECIAL	Source cell 1 specie ISO(atoms/s)
	ISO+1	SOURCE(ISO+1)	SPECIAL	Source cell 2 specie 1(atoms/s)
	ISO*NCELLS	SOURCE(ISO*NCELLS)	SPECIAL	Source cell NCELLS specie ISO (atoms/s)

There are two special read formats. One is for integer data 6(I1, I2, I9), one for floating point data 6(I1, I2, E9.3). In each of these formats the first integer field, I1, designates the options listed in Table X. The second integer field, I2, controls the execution of the option, and the remainder of the field, I9 or E9.3, is for the input data. All data blocks read with these formats must be ended with a 3 in the I1 field after the last word of the block.

TABLE X
SPECIAL READ FORMAT OPTIONS

<u>Value of I1</u>	<u>Description</u>
0/blank	No action
1	Repeat data word in 9 field number of times indicated in I2 field.
2	Place number of linear interpolants indicated in I2 field between data word in 9 field and data word in next 9 field (not allowed for integers).
3	Terminate reading of the data block. A 3 must follow last data word of all blocks.

D. Machine Requirements

The DASH code requires both 35-mm-film hardware for graphics and the large core memory (LCM) capabilities of a CDC-7600. DASH was designed to operate on a CDC-7600 using the FTN compiler. The code is listed in App. 8.

VI. DASH TEST PROBLEM

To demonstrate the application of the DASH code to solving a problem, a two-specie, three-material sample problem has been defined. The absorbent is a slab 5 cm thick consisting of three equal material regions. Initially, there is no diffusant in the absorbent. The material data for the two materials is summarized in Table XI. The test problem was run for 10 days with the results tabulated every 2 days. A detailed listing of the input and output is given in App. C. The graphic output is given here (Figs. 21 and 22). This problem requires approximately 5.5 CPU seconds of CDC-7600 time.

TABLE XI
SAMPLE PROBLEM DATA

DIFFUSANT	DECAY CONSTANT (s^{-1})	DIFFUSION COEFFICIENT (cm^2/s)			BOUNDARY CONCENTRATIONS	
		1	2	3	Left	Right
A	8.0225×10^{-7}	5.426×10^{-6}	1.266×10^{-5}	1.808×10^{-6}	1.0×10^{10}	0.0
B	1.6045×10^{-6}	2.713×10^{-6}	6.330×10^{-6}	9.042×10^{-7}	5.0×10^9	0.0

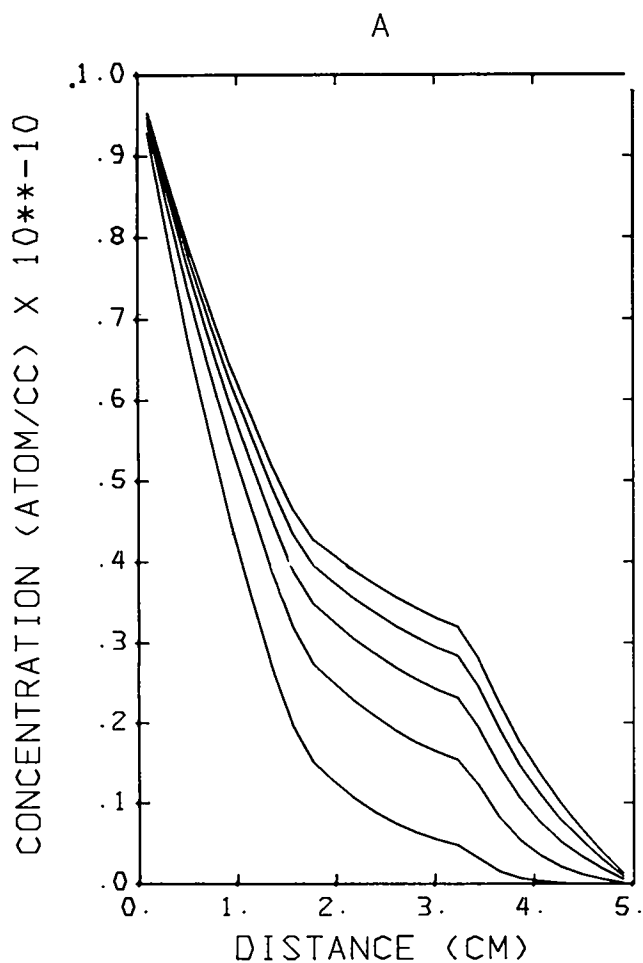


Fig. 21. Sample problem results for Diffusant A.

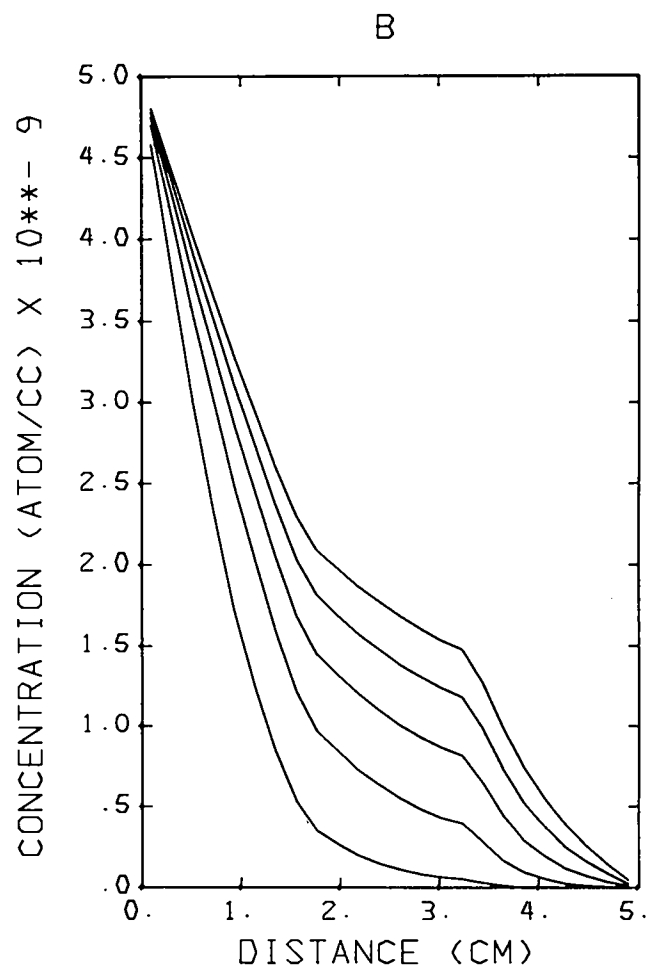


Fig. 22. Sample problem results for Diffusant B.

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APPENDIX A MATRIX OPERATOR EVALUATION

The time-dependent equation to be solved using the matrix operator method is

$$\frac{d\vec{X}}{dt} = B\vec{X} + \vec{g}. \quad (A-1)$$

If the matrix B is constant in the time interval (0, t), we may construct the matricant $\Omega_0^t(B)$, Eq. (A-2), using the Volterra method of the multiplicative integral.^{4,14,15}

$$\Omega_0^t(B) = \exp \left[\int_0^t B(s) ds \right] = \exp [Bt]. \quad (A-2)$$

The solution to Eq. (A-1) is given by

$$\vec{X}(t) = \Omega_0^t(B) \vec{X}(0) + \int_0^t dt' K(t, t') \vec{g}(t'), \quad (A-3)$$

where

$$K(t, t') = \Omega_0^t(B) \left[\Omega_0^{t'}(B) \right]^{-1}. \quad (A-4)$$

Substituting Eq. (A-2) into Eqs. (A-3) and (A-4) gives

$$\vec{X}(t) = e^{Bt} \vec{X}(0) + e^{Bt} \int_0^t dt' e^{-Bt'} \vec{g}(t'). \quad (A-5)$$

Assuming that $\vec{g}(t) = \vec{g}$ is constant over the interval (0, t), Eq. (A-5) becomes

$$\vec{X}(t) = e^{Bt} \vec{X}(0) + \vec{g}^{-1} (e^{Bt} - I) \vec{g}. \quad (A-6)$$

Defining the matrix operator D(C) by⁴

$$D(C) = C^{-1} (e^C - I) \quad (A-7)$$

or

$$tD(Bt) = B^{-1} (e^{Bt} - I), \quad (A-8)$$

Eq. (A-6) becomes

$$\begin{aligned} \vec{X}(t) &= \vec{X}(0) + tBD(Bt) \vec{X}(0) + tD(Bt) \vec{g} \\ &= \vec{X}(0) + tD(Bt) [\vec{BX}(0) + \vec{g}]. \end{aligned} \quad (A-9)$$

Note that the matrix operator $D(C)$ defined by

$$D(C) = C^{-1} (e^C - I) = \sum_{n=0}^{\infty} \frac{C^n}{(n+1)!} \quad (A-10)$$

exists even if $C = Bt$ is singular. Although the eigenvalues of e^C are bound by unity, and the eigenvalues of C are bound, but not necessarily by unity, the direct evaluation of $D(C)$ would prove difficult computationally if Eq. (A-10) is used. The matrix C can be scaled so that the eigenvalues are bound by unity. Define

$$H = 2^{-p}C, \quad (A-11)$$

where p is determined by

$$||H|| < \frac{1}{2} \quad (A-12)$$

or^{4,15}

$$p > \ln \left(\sum_{ij} |C_{ij}|^2 \right) / (2 \ln 2). \quad (A-13)$$

We approximate the $D(H)$ matrix operator by a finite number of terms M using Eq. (A-10).

$$D^M(H) \approx \sum_{n=0}^M \frac{H^n}{(n+1)!} \quad (A-14)$$

The value of M is chosen such that the excluded terms have an error less than ϵ ,⁴ or

$$\frac{(|H|)^{M+1}}{(M+2)!} < \frac{1}{2^{M+1}(M+2)!} < \epsilon. \quad (A-15)$$

Knowing $D(H)$ we may recur upwards by powers of 2 in H to find $D(C)$ where $C = 2^p H$, using the recursion relation

$$D(2^{p+1}H) = D(2^p H) \left[I + \frac{1}{2} (2^p H) D(2^p H) \right]. \quad (A-16)$$

The recursion relation is readily proven by induction. Define

$$D(H) = H^{-1} (e^H - I) \quad (A-17)$$

and

$$C = 2^p H. \quad (A-18)$$

Clearly if $p = 0$, $D(C)$ is equal to $D(H)$. If $p = 1$, Eq. (A-16) yields

$$\begin{aligned} D(C) &= D(2H) = (2H)^{-1} (e^{2H} - I) \\ &= H^{-1} (e^H - I) \frac{(e^H + I)}{2} \\ &= D(H) \left[I + \frac{1}{2} H D(H) \right]. \end{aligned} \quad (A-19)$$

Induction based on Eq. (A-19) yields

$$D(2^{p+1}H) = D(2^p H) \left[I + \frac{1}{2} (2^p H) D(2^p H) \right]. \quad (A-20)$$

Assume Eq. (A-20), which is true for $p = 0$ and 1, is true for $p = n$. Evaluate $D(2^{n+1}H)$ as

$$\begin{aligned}
D(2^n + 1_H) &= (2^n + 1_H)^{-1} (e^{2^n + 1_H} - I) \\
&= (2^{n_H})^{-1} (e^{2^{n_H}} - I)^{\frac{1}{2}} (e^{2^{n_H}} + I) \\
&= D(2^{n_H}) \left[I + \frac{1}{2} (2^{n_H}) D(2^{n_H}) \right] .
\end{aligned}
\tag{A-21}$$

Since Eq. (A-20) is true for $p = 0$ and 1 , and if it is assumed true for $p = n$, it is true for $p = n + 1$; then by transfinite induction it is true for all p .

APPENDIX B DASH CODE LISTING (LASL Code LP-1055)

PROGRAM DASH1 (INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT)
DASH - A MULTICOMPONENT TIME DEPENDENT CONCENTRATION DIFFUSION
WITH RADIOACTIVE DECAY PROGRAM.

BY COURTNEY E. APPERSON, JR.
LUCY M. CARRUTHERS
JUDITH F. SHINN
ENERGY DIVISION
LOS ALAMOS SCIENTIFIC LABORATORY
AND
CLARENCE E. LEE
TEXAS A AND M UNIVERSITY
MARCH 1979

THE PROGRAM DASH CALCULATES THE TRANSIENT CONCENTRATION OF
MULTIPLY DIFFUSING SPECIE WITH RADIOACTIVE DECAY USING FINITE
DIFFERENCE AND EXPONENTIAL OPERATOR TECHNIQUES.

THIS IS THE FOURTH VERSION OF DASH. IT WAS CREATED
ON 15 MARCH 1979.

RECOGNIZING THAT GRAPHICS HARDWARE AND SOFTWARE ARE USUALLY
UNIQUE TO A PARTICULAR INSTALLATION THE GRAPHICS PACKAGE IN
DASH CAN BE READILY DELETED WITHOUT EFFECTING THE REMAINDER
OF THE CODE.

INPUT INSTRUCTIONS FOR THE CODE ARE--

CARD	WORD	SYMBOL	FORMAT	DESCRIPTION
0				PRINT OPTIONS
	1	NPRINT	I4	0/1 LINE PRINTER/TERMINAL
	2	NPLOT	I4	0/1 NO PLOT/PLOT

1 --ONE CARD PER NUCLIDE--

BASIC NUCLIDE DATA

1	NANMAT(I,1)	A7	NUCLIDE NAME
2	NANMAT(I,2)	I4	ID NUMBER
3	NANMAT(I,3)	I4	DECAY PARENT 1
4	NANMAT(I,4)	I4	DECAY PARENT 2
5	NANMAT(I,5)	I4	CAPTURE PARENT 1
6	NANMAT(I,6)	I4	CAPTURE PARENT 2
7	NANMAT(I,7)	I4	N-2N PARENT
8	NANMAT(I,8)	I4	N-ALPHA PARENT
9	NANMAT(I,9)	I4	N-P PARENT
10	ANMAT(I,1)	E12.5	DECAY CONSTANT (1/S)

2 --ONE CARD PER BRANCH FOR EACH NEGATIVE VALUE
OF NANMAT(I,3-9)--

1	BRV(IBR)	E12.5	BRANCHING RATIO
---	----------	-------	-----------------

--BLANK CARD AFTER LAST SET OF CARDS 1 AND 2--

3

CROSS SECTION TITLE CARD

1	NXSEC(II,1)	A6	TITLE 1
2	NXSEC(II,2)	A6	TITLE 2
3	NXSEC(II,3)	I4	NUMBER OF GROUPS
4	NXSEC(II,4)	I4	NUCLIDE ID

4 --NXSEC(II,3) CARDS--

CROSS SECTION DATA

1	XSEC(II,KX,1)	E12.5	SIGMA N-GAMMA
2	XSEC(II,KX,2)	E12.5	SIGMA N-2N
3	XSEC(II,KX,3)	E12.5	SIGMA N-ALPHA
4	XSEC(II,KX,4)	E12.5	SIGMA N-P

--BLANK CARD AFTER LAST SET OF CARDS 3 AND 4--

5

PROBLEM RELATED DATA

1	NCELLS	I4	NUMBER OF CELLS IN PROBLEM
2	NGEOM	I4	1/2/3 SLAB/CYLINDER/SPHERE
3	NBCL	I4	LEFT BOUNDARY CONDITION
			1/2 REFLECTED/CONCENTRATION SPECIFIED
4	NBCR	I4	RIGHT BOUNDARY CONDITION
			1/2 REFLECTED/CONCENTRATION SPECIFIED
5	NTEMPS	I4	NUMBER OF ENTRIES FOR SPECIFYING TEMPERATURE FIELD
6	IMATS	I4	NUMBER OF MATERIALS
7	IGP	I4	NUMBER OF NEUTRON ENERGY GROUPS

6

TIME STEP DATA

1	TINT	E12.6	INITIAL TIME (DAYS)
2	TINC	E12.6	NUMBER OF TIME STEPS
3	T1MAX	E12.6	TIME AT END OF PROBLEM (DAYS)

7

GEOMETRY (CM)

1	DIST(1)	SPECIAL	0.0
2	DIST(2)	SPECIAL	FIRST CELL RIGHT BOUNDARY
3	DIST(3)	SPECIAL	SECOND CELL RIGHT BOUNDARY
NCELLS+1	DIST(NCELLS+1)	SPECIAL	LAST CELL RIGHT BOUNDARY

```

8          ASSIGN MATERIALS
          1      MATS(1)    SPECIAL  MATERIAL ID FOR CELL 1
          2      MATS(2)    SPECIAL  MATERIAL ID FOR CELL 2
    NCELLS    MATS(NCELLS) SPECIAL  MATERIAL ID FOR CELL NCELLS
9
          DEPENDENT VALUE FOR
          TEMPERATURE FIELD (K)
          1      TEMPS(1)   SPECIAL  TEMPERATURE 1
          2      TEMPS(2)   SPECIAL  TEMPERATURE 2
    NTEMPS    TEMPS(NTEMPS) SPECIAL  TEMPERATURE NTEMPS
10
          INDEPENDENT VALUE FOR
          TEMPERATURE FIELD (CM)
          1      TEMCOR(1)   SPECIAL  COORDINATE OF TEMPERATURE 1
          2      TEMCOR(2)   SPECIAL  COORDINATE OF TEMPERATURE 2
    NTEMPS    TEMCOR(NTEMPS) SPECIAL  COORDINATE OF TEMPERATURE
    NTEMPS
11  --ONE SET OF CARDS 11 AND 12 FOR EACH OF IMATS MATERIALS--
          DIFFUSION MATRIX (CM**2/S)
          1      DIJO(1,1,N) SPECIAL  MATERIAL N ELEMENT(1,1)
          2      DIJO(2,1,N) SPECIAL  MATERIAL N ELEMENT(1,2)
    ISO      DIJO(ISO,1,N) SPECIAL  MATERIAL N ELEMENT(1,ISO)
    ISO+1    DIJO(1,2,N) SPECIAL  MATERIAL N ELEMENT(2,1)
    ISO*ISO  DIJO(ISO,ISO,N) SPECIAL  MATERIAL N ELEMENT(ISO,ISO)
12  --ONE SET OF CARDS 11 AND 12 FOR EACH OF IMATS MATERIALS--
          ACTIVATION ENERGY MATRIX
          (CAL/MOLE)
          1      AIJS(1,1,N) SPECIAL  MATERIAL N ELEMENT(1,1)
          2      AIJS(2,1,N) SPECIAL  MATERIAL N ELEMENT(1,2)
    ISO      AIJS(ISO,1,N) SPECIAL  MATERIAL N ELEMENT(1,ISO)
    ISO+1    AIJS(1,2,N) SPECIAL  MATERIAL N ELEMENT(2,1)
    ISO*ISO  AIJS(ISO,ISO,N) SPECIAL  MATERIAL N ELEMENT(ISO,ISO)
13  --ONE CONTINUOUS SET OF CARD 13 FOR IGP GROUPS--
    --SUPPLY ONLY IF CROSS SECTIONS ARE PRESENT--
          FLUXES (NEUTRONS/CM**2-S)
          1      PHI(1,N)    SPECIAL  GROUP N FLUX IN CELL 1
          2      PHI(2,N)    SPECIAL  GROUP N FLUX IN CELL 2
    NCELLS    PHI(NCELLS,N) SPECIAL  GROUP N FLUX IN CELL NCELLS
    NCELLS+1  PHI(1,N+1)    SPECIAL  GROUP N+1 FLUX IN CELL 1
14  --SUPPLY ONLY IF NBCL = 2--
          LEFT BOUNDARY CONCENTRATIONS
          (ATOMS/CC)
          1      CONBOU(1,1) SPECIAL  SPECIE 1 LEFT BOUNDARY CONC
          2      CONBOU(2,1) SPECIAL  SPECIE 2 LEFT BOUNDARY CONC
    ISO      CONBOU(ISO,1) SPECIAL  SPECIE ISO LEFT BOUNDARY
    CONC

```



```

C   DIMENSION SOURCE(MM),DIFDUM1(NISO,NISO),DIFDUM2(NISO,NISO),
C   1 CONBOU(NISO,2),IPVT(NISO),AK(NISO,NISO),BK(NISO,NISO),
C   2 CKK(NISO,NISO),CONINT(MM),CONCEN(MM),DUM33(MM)
C   WHERE MM=NISO*NCELL
C   DIMENSION NANMAT(6,9), ANMAT(6,2), BRV(10), NXSEC(11,4), XSEC(10,4
1   ,4), NPP(25)
C   DIMENSION DIST(26), MATS(25), TEMPS(25), TEMCOR(25), DIJO(5,5,5),
1   AIJS(5,5,5), DUM1(25), DUM2(25)
C   DIMENSION DUM11(100), DUM22(100), ALAM(5,5), BB(5,5)
C   DIMENSION DELR(25), AREA(25), VOL(25), RBAR(25), PHI(25,4), W(25),
1   DUM3(25), DIFFK(5,5), DIFFK1(5,5), DAPLOT(5,25,11)
C   COMMON /SOLS/ BIGB(125,125), B(125,125), C(125,125), D(125,125), E
1   (125,125), F(125,125)
C   DIMENSION SOURCE(125), DIFDUM1(5,5), DIFDUM2(5,5), CONBOU(5,2),
1   IPVT(5), AK(5,5), BK(5,5), CKK(5,5), CONINT(125), CONCEN(125),
2   DUM33(125)
C   LEVEL 2, BIGB, B, C, D, E, F
C   COMMON /IO/ NINP, NOUT, IER, NPRINT
C   COMMON /NUCDAT/ ISO, IBR, IXS, IGP
C   COMMON /TIMES/ TINT, TINC, TIMAX
C   TAPE5 IS INPUT UNIT
C   NINP=5
C   TAPE6 IS OUTPUT UNIT
C   NOUT=6
C   READ (NINP,100) NPRINT,NPLOT
C   NISO=5
C   NISO1=NISO+1
C   NN=100
C   NN IS THE GREATER OF NISO*NISO AND NGP*NCELL
C   NBR=10
C   NXS=10
C   NXSP=NXS+1
C   NGP=4
C   NCELL=25
C   NCELL1=NCELL+1
C   MM=NISO*NCELL
C   NTEM=25
C   NTEM MUST BE GREATER THAN OR EQUAL TO NCELL
C   NMATS=5
C   NTIME=11
C   CALL INPA (NANMAT,ANMAT,BRV,NXSEC,XSEC,NGP,NXS,NBR,NISO1,NXSP)
C   CALL INPB (NCELLS,NGEOM,NBCR,NBCL,NTEMPS,IMATS,DIST,MATS,PHI,TEMPS
1   ,TEMCOR,DIJO,AIJS,NCELL1,NCELL,NTEM,NISO,NMATS,NGP,DUM11,DUM22,NN
2   ,CONBOU,CONINT,SOURCE,MM)
C   N=NCELLS+1
C   CALL GEOM (NGEOM,DIST,DELR,AREA,VOL,RBAR,N,NCELLS)
C   CALL INPLT (NCELL,NCELL1,NBCL,NBCR,MATS,DIST,NGEOM,NCELLS)
C   CALL PRIV(DIST,N,NCELL1,10H DISTANCES,10H )
C   CALL PRIV(DELR,NCELLS,NCELL1,10H DELR ,10H )
C   CALL PRIV(AREA,NCELLS,NCELL1,10H AREA ,10H )
C   CALL PRIV(VOL,NCELLS,NCELL1,10H VOLUME ,10H )
C   CALL PRIV(RBAR,NCELLS,NCELL1,10H RBAR ,10H )
C   CALL TEMADJ (TEMPS,TEMCOR,NTEMPS,RBAR,NCELLS,W,DUM1,DUM2,DUM3,NTEM
1   )
C   CALL PRIV (TEMPS,NCELLS,NTEM,10H MESH TEMP,10HERATURES )
C   IF(IXS.EQ.0) GO TO 5
C   CALL PRIM(PHI,NCELLS,IGP,NCELL,NGP,10H FLUXES ,10H )
C   5 CONTINUE
C   DO 20 I=1,MM
C   DO 10 J=1,MM
C   BIGH(I,J)=0.0
10 CONTINUE
20 CONTINUE
C   II=1
C   MAKE ADJUSTMENTS FOR HOLLOW CYLINDER AND SPHERE
C   IF (NBCL.EQ.2.AND.NGEOM.GT.1) II=2
C   MAT=MATS(II)
C   CALL DIJADJ (DIJO,AIJS,TEMPS,DIFFK,NISO,NMATS,NCELL,ISO,II,MAT)
C   CALL PRIM(DIFFK,ISO,ISO,ISO,ISO,10H DIFFK ,10H )

```

```

      NIC=ISO*(NCELLS+1-II)
      CALL BCONL (BK,AREA,DIFFK,DELR,SOURCE,CONBOU,NCELLS,ISO,NBCL,NGEOM
1      ,NISO,NIC,DUM11,DUM33)
C      CALL PRIM(BK,ISO,ISO,ISO,ISO,10H EK          ,10H          )
      NM1=NCELLS-1
      ICOL=1
      DO 30 I=II,NM1
      CALL MAKLAM (NANMAT,ANMAT,XSEC,NXSEC,PHI,BRV,ALAM,BB,NISO1,NXS
1      ,NXSP,NBR,NGP,ISO,IXS,IGP,NCELL,I)
C      CALL PRIM(ALAM,ISO,ISO,ISO,ISO,10H LAMBDA      ,10H          )
      K=I+1
      MAT=MATS(K)
      CALL DIJADJ (DIJO,AIJS,TEMPS,DIFFK1,NISO,NMATS,NCELL,ISO,K,MAT)
C      CALL PRIM(DIFFK1,ISO,ISO,ISO,ISO,10H DIFFK1      ,10H          )
      CALL BIGEL (DIFFK,DIFFK1,DIFDUM1,DIFDUM2,ALAM,AK,BK,CKK,ISO,AREA
1      ,VOL,DELR,NCELLS,IPVT,DUM11,I)
C      CALL PRIM(CKK,ISO,ISO,ISO,ISO,10H KK          ,10H          )
C      CALL PRIM(AK,ISO,ISO,ISO,ISO,10H AK          ,10H          )
C      CALL PRIM(BK,ISO,ISO,ISO,ISO,10H BK          ,10H          )
      CALL MATMOV (ISO,ISO,DIFFK1,ISO,DIFFK,ISO)
      CALL MAKEB (BIGB,AK,BK,CKK,NIC,ISO,VOL,NCELLS,ICOL,II)
30      CONTINUE
      CALL MAKLAM (NANMAT,ANMAT,XSEC,NXSEC,PHI,BRV,ALAM,BB,NISO1,NXS
1      ,NXSP,NBR,NGP,ISO,IXS,IGP,NCELL,NCELLS)
C      CALL PRIM(ALAM,ISO,ISO,ISO,ISO,10H LAMBDA      ,10H          )
      CALL BCONR (AK,AREA,DIFFK,DELR,SOURCE,CONBOU,NCELLS,ISO,NBCR,NISO
1      ,NIC,DUM11,DUM22,BK,CKK,ALAM,VOL,DIFDUM1)
C      CALL PRIM(CKK,ISO,ISO,ISO,ISO,10H KK          ,10H          )
C      CALL PRIM(AK,ISO,ISO,ISO,ISO,10H AK          ,10H          )
C      CALL PRIM(SOURCE,NIC,NIC,10H SOURCE          ,10H          )
      CALL MAKEBL (BIGB,AK,BK,CKK,NIC,ISO,VOL,NCELLS,ICOL,II)
C      CALL PRIMES(BIGB,NIC,NIC,NIC,NIC,10H BIGB      ,10H          )
      DTIME=(TIMAX/TIMC)*24.*3600.
      NSTEP=TINC
      CALL SOLVER (BIGB,B,C,D,E,F,DTIME,NIC,NIC)
C      CALL PRIMES(E,NIC,NIC,NIC,NIC,10H E          ,10H          )
C      CALL PRIMES(D,NIC,NIC,NIC,NIC,10H D          ,10H          )
      NP=NCELLS-II+1
      DO 50 J=1,NP
      DO 40 I=1,ISO
      I1=ISO*(J-1)+I
      DAPLOT(I,J,1)=CONINT(I1)
40      CONTINUE
50      CONTINUE
      CALL MAKVOL (B,NIC,VOL,NCELLS,II,ISO)
C      CALL PRIMES(B,NIC,NIC,NIC,NIC,10H VOLMAT      ,10H          )
      DO 90 I=1,NSTEP
      CALL FSOLVE (B,C,D,E,DUM33,DTIME,NIC,CONINT,SOURCE,CONCEN)
      DO 70 J=1,NP
      DO 60 JI=1,ISO
      I1=ISO*(J-1)+JI
      DAPLOT(JI,J,I+1)=CONCEN(I1)
60      CONTINUE
70      CONTINUE
      DO 80 J=1,NIC
      CONINT(J)=CONCEN(J)
80      CONTINUE
90      CONTINUE
      NTIM=NSTEP+1
      CALL CONCPLOT (NANMAT,CONBOU,DAPLOT,ISO,NCELL,NISO1,NISO,NTIME,NP
1      ,NTIM,NPP,NBCL,NBCR,VOL)
      IF (NPLOT.NE.0) CALL DRAW (NANMAT,RBAR,DAPLOT,NTIM,NP,CONCEN,DUM33
1      ,NISO,NCELLS,NCELL,NTIME,ISO,NISO1,CONBOU,DIST,NCELL1,NBCL,NBCR)
      STOP
C
100      FORMAT (2I4)
      END

```

```

SUBROUTINE INPA (NANMAT,ANMAT,BRV,NXSEC,XSEC,NGP,NXS,NBR,NISO1
1,NXSP)
C INPUTA READS AND PRINTS THE NUCLEAR DATA
DIMENSION NANMAT(NISO1,9), ANMAT(NISO1,2), BRV(NBR), NXSEC(NXSP,4)
1, HBRP(3,10), XSEC(NXS,NGP,4)
COMMON /IO/ NINP, NOUT, IER, NPRINT
COMMON /NUCDAT/ ISO, IER, IXS, IGP
DATA NHJ /6H /
I=1
IBR=1
II=1
C READ NUCLEAR DATA
10 READ (NINP,130) (NANMAT(I,J),J=1,9),ANMAT(I,1)
IF (NANMAT(I,1).EQ.NHJ) GO TO 40
C TEST FOR BRANCHING RATIOS
DO 30 J=3,6
IF (NANMAT(I,J)) 20,30,30
20 READ (NINP,140) BRV(IBR)
HBRP(1,IBR)=IABS(NANMAT(I,J))
HBRP(2,IBR)=I
HBRP(3,IBR)=BRV(IBR)
IBR=IBR+1
30 CONTINUE
I=I+1
GO TO 10
40 I=I-1
IBR=IBR-1
IGP=0
C READ CROSS SECTION DATA
50 READ (NINP,150) (NXSEC(II,J),J=1,4)
IF (NXSEC(II,1).EQ.NHJ) GO TO 70
IGP=NXSEC(II,3)
DO 60 J=1,IGP
READ (NINP,140) (XSEC(II,J,JJ),JJ=1,4)
60 CONTINUE
II=II+1
GO TO 50
70 II=II-1
C PRINT DECAY DATA
WRITE (NOUT,160)
WRITE (NOUT,180)
WRITE (NOUT,190)
WRITE (NOUT,180)
WRITE (NOUT,200)
WRITE (NOUT,170)
LCNT=13
DO 80 J=1,I
WRITE (NOUT,210) (NANMAT(J,JJ),JJ=1,9),ANMAT(J,1)
LCNT=LCNT+2
IF (LCNT.GE.60) WRITE (NOUT,160)
80 CONTINUE
C PRINT BRANCHING RATIOS
IF (IBR.EQ.0) GO TO 100
WRITE (NOUT,160)
WRITE (NOUT,180)
WRITE (NOUT,220)
DO 90 J=1,IBR
WRITE (NOUT,230) HBRP(1,J),HBRP(2,J),HBRP(3,J)
90 CONTINUE
100 CONTINUE
C PRINT CROSS SECTIONS
IF (II.EQ.0) GO TO 120
WRITE (NOUT,160)
WRITE (NOUT,180)
WRITE (NOUT,240)
DO 110 J=1,II
WRITE (NOUT,250) (NXSEC(J,JN),JN=1,4)
DO 110 JJ=1,IGP
110 WRITE (NOUT,260) JJ,(XSEC(J,JJ,JN),JN=1,4)
120 CONTINUE
ISO=I

```



```

IXS=II
RETURN
C
130 FORMAT (A7,8I4,E12.5)
140 FORMAT (6(E12.5))
150 FORMAT (2A6,2I4)
160 FORMAT (1H1)
170 FORMAT (/)
180 FORMAT (/////)
190 FORMAT (29X,37HDECAY CHAINS AND NUCLIDE RELATED DATA)
200 FORMAT (24X,5HDECAY,7X,7HCAPTURE,28X,5HDECAY,/,24X,6HPARENT,6X,6HP
1ARENT,4X,21HN-2N N-ALPHA N-P ,3X,8HCONSTANT,/,5X,7HNUCLIDE,5X
2,2HID,2(5X,7H1 2),/)
210 FORMAT (5X,A7,1X,6(2X,I4),3X,I4,4X,I4,3X,1PE12.5)
220 FORMAT (9X,15HBRANCHING RATIO,/,5X,4HFROM,4X,2HTO,6X,5HRATIO,/)
230 FORMAT (5X,F4.0,3X,F4.0,3X,F7.4)
240 FORMAT (10X,42HCROSS SECTIONS FOR TRANSMUTATION REACTIONS,///)
250 FORMAT (//,10X,2A6,2I4,/,4X,5HGROU,8X,7HN-GAMMA,11X,4HN-2N,12X,7H
1N-ALPHA,12X,3HN-P)
260 FORMAT (5X,I3,1X,4(5X,1PE12.5))
END
SUBROUTINE INPB (NCELLS,NGEOM,NBCR,NBCL,NTEMPS,IMATS,DIST,MATS,PHI
1 ,TEMPS,TEMCOR,DIJO,AIJS,NCELL1,NCELL,NTEM,NISO,NMATS,NGP,DUM11
2 ,DUM22,NN,CONBOU,CONINT,SOURCE,MM)
C
READ PROBLEM RELATED DATA
DIMENSION DIST(NCELL1), MATS(NCELL), TEMPS(NTEM), TEMCOR(NTEM),
1 DIJO(NISO,NISO,NMATS), AIJS(NISO,NISO,NMATS), DUM11(NN), DUM22(NN
2 ), PHI(NCELL,NGP), CONBOU(NISO,2), CONINT(MM), SOURCE(MM)
DIMENSION IGEOM(3)
COMMON /IO/ NINP, NOUT, IER, NPRINT
COMMON /NUCDAT/ ISO, IBR, IXS, IGP
COMMON /TIMES/ TINT, TINC, TIMAX
DATA IGEOM(1), IGEOM(2), IGEOM(3) /9HSLAB. ,9HCYLINDER.,9HSPHER
1E. /
READ (NINP,130) NCELLS,NGEOM,NBCL,NBCR,NTEMPS,IMATS,IGP
PRINT (NOUT,140) IGEOM(NGEOM),NBCL,NBCR
READ (NINP,150) TINT,TINC,TIMAX
NRADI=NCELLS+1
CALL REAG (DIST,NRADI,6HRADII,6H )
CALL REAI (MATS,NCELLS,6HMATERI,6HALS )
CALL REAG (TEMPS,NTEMPS,6HTEMPER,6HATURES)
CALL REAG (TEMCOR,NTEMPS,6HTEMP R,6HADII )
INDEX=ISO*ISO
DO 30 I=1,IMATS
CALL REAG (DUM11,INDEX,6HDIJ-0 ,6H )
CALL REAG (DUM22,INDEX,6HAIJ ,6H )
DO 20 J=1,ISO
DO 10 JJ=1,ISO
IND=(J-1)*ISO+JJ
DIJO(JJ,J,I)=DUM11(IND)
AIJS(JJ,J,I)=DUM22(IND)
10 CONTINUE
20 CONTINUE
30 CONTINUE
IF (IXS.EQ.0) GO TO 60
INDEX=IGP*NCELLS
CALL REAG (DUM11,INDEX,6HCELL F,6HLUXES )
DO 50 I=1,NCELLS
DO 40 JJ=1,IGP
IND=(I-1)*IGP+JJ
PHI(I,JJ)=DUM11(IND)
40 CONTINUE
50 CONTINUE
60 DO 80 I=1,2
DO 70 J=1,ISO
CONBOU(J,I)=0.0
70 CONTINUE
80 CONTINUE
IF (NBCL.NE.2) GO TO 100
CALL REAG (DUM11,ISO,6HLEFT C,6HONCEN )
DO 90 I=1,ISO

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      CONBOU(I,1)=DUM11(I)
90  CONTINUE
100 IF (NBCR.NE.2) GO TO 120
    CALL REAG (DUM11,ISO,6HRIGHT ,6HCONCEN)
    DO 110 I=1,ISO
      CONBOU(I,2)=DUM11(I)
110 CONTINUE
120 CONTINUE
    INDEX=ISO*NCELLS
    IF (NGEOM.GT.1.AND.NBCL.EQ.2) INDEX=INDEX-ISO
    CALL REAG (CONINT,INDEX,6HINITIA,6HL CONC)
    INDEX=ISO*NCELLS
    CALL REAG (SOURCE,INDEX,6HSOURCE,6H INPUT)
    RETURN
C
130 FORMAT (18I4)
140 FORMAT (///,1X,*THE GEOMETRY FOR THIS PROBLEM IS A *,A9,/,2X,*THE
1 LEFT BOUNDARY CONDITION IS =*,I2,/,2X*THE RIGHT BOUNDARY CONDITION
2 IS =*,I2,/)
150 FORMAT (3E12.6,I12)
    END
    SUBROUTINE GEOM (NGEOM,DIST,DELR,AREA,VOL,RBAR,N,NCELLS)
C   SET UP GEOMETRY
C   CALCULATE CELL AREAS AND VOLUMES
    DIMENSION DIST(N), DELR(NCELLS), AREA(NCELLS), VOL(NCELLS), RBAR
1 (NCELLS)
C   N=NCELLS+1
C   NGEOM=1,2,3 - SLAB,CYLINDER,SPHERE
    PI=3.1415926
    IF (NGEOM-2) 10,30,50
10  DO 20 I=1,NCELLS
      DELR(I)=DIST(I+1)-DIST(I)
      RBAR(I)=0.5*(DIST(I+1)+DIST(I))
      AREA(I)=1.0
      VOL(I)=DELR(I)
20  CONTINUE
    RETURN
30  DO 40 I=1,NCELLS
      DELR(I)=DIST(I+1)-DIST(I)
      RBAR(I)=0.5*(DIST(I+1)+DIST(I))
      AREA(I)=2*PI*DIST(I+1)
      VOL(I)=2.*PI*DELR(I)*RBAR(I)
40  CONTINUE
    RETURN
50  DO 60 I=1,NCELLS
      DELR(I)=DIST(I+1)-DIST(I)
      RBAR(I)=(DIST(I+1)**2+DIST(I+1)*DIST(I)+DIST(I)**2)/3.0
      AREA(I)=4.0*PI*DIST(I+1)**2
      VOL(I)=4.0*PI*RBAR(I)*DELR(I)
      RBAR(I)=SQRT(RBAR(I))
60  CONTINUE
    RETURN
    END
C   SUBROUTINE INPLT (NCELL,NCELL1,NBCL,NBCR,MATS,DIST,NGEOM,NCELLS)
C   DRAW A MAP OF THE PROBLEM GEOMETRY
    DIMENSION MATS(NCELL), DIST(NCELL1), NBOU(2), IGEOM(3)
    COMMON /IO/ NINP, NOUT, IER, NPRINT
    DATA ISTR /1H*/, NBOU(1), NBOU(2) /1H1,1H2/
    DATA IGEOM(1), IGEOM(2), IGEOM(3) /9HSLAB. ,9HCYLINDER.,9HSPHER
1E. /
C   TERMINAL OUTPUT
    NBOX=8
    IF (NPRINT.EQ.1) GO TO 10
C   LINE PRINTER OUTPUT
    NBOX=12
    WRITE (NOUT,180)
    WRITE (NOUT,190) IGEOM(NGEOM)
10  CONTINUE
    WRITE (NOUT,170)
    IF (MOD(NCELLS,NBOX)) 20,30
20  LOOP=(NCELLS/NBOX)+1

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GO TO 40
30 LOOP=(NCELLS/NBOX)
40 ICELL=NCELLS
   ICOUNT=0
   DO 120 I=1,LOOP
   ICOUNT=ICOUNT+1
   IS=1
   IE=MINO(NBOX,ICELL)
   IMM=IE-IS
   IMM1=IMM-1
   IM2=(IMM+1)*8-1
   IM3=IMM*8-1
   NDX=(I*NBOX-NBOX)+1
   NDS=IMM+(I*NBOX-NBOX)
   NDRS=NDS+1
   NDRE=NDRS+1
   ICELL=ICELL-NBOX
   IF (LOOP.EQ.1) GO TO 100
   IF (I.EQ.1) GO TO 50
   IF (ICOUNT.EQ.LOOP) GO TO 70
   WRITE (NOUT,150) ISTR,(ISTR,J=1,IM2)
   WRITE (NOUT,130) ISTR,(ISTR,J=1,IMM)
   WRITE (NOUT,140) ISTR,(MATS(J),ISTR,J=NDX,NDS),MATS(NDS+1)
   WRITE (NOUT,130) ISTR,(ISTR,J=1,IMM)
   WRITE (NOUT,150) ISTR,(ISTR,J=1,IM2)
   WRITE (NOUT,160) (DIST(J),J=NDX,NDRS)
   WRITE (NOUT,170)
   GO TO 120
50 IF ((NGEOM.NE.1).AND.(NBCL.EQ.2)) GO TO 60
   WRITE (NOUT,150) NBOU(NBCL),(ISTR,J=1,IM2)
   WRITE (NOUT,130) NBOU(NBCL),(ISTR,J=1,IMM)
   WRITE (NOUT,140) NBOU(NBCL),(MATS(J),ISTR,J=NDX,NDS),MATS(NDS+1)
   WRITE (NOUT,130) NBOU(NBCL),(ISTR,J=1,IMM)
   WRITE (NOUT,150) NBOU(NBCL),(ISTR,J=1,IM2)
   WRITE (NOUT,160) (DIST(J),J=NDX,NDRS)
   WRITE (NOUT,170)
   GO TO 120
60 WRITE (NOUT,200) (ISTR,J=1,8),NBOU(NBCL),(ISTR,J=1,IM3)
   WRITE (NOUT,130) ISTR,NBOU(NBCL),(ISTR,J=1,IMM1)
   WRITE (NOUT,210) ISTR,MATS(1),NBOU(NBCL),(MATS(J),ISTR,J=2,NDS)
1  ,MATS(NDS+1)
   WRITE (NOUT,130) ISTR,NBOU(NBCL),(ISTR,J=1,IMM1)
   WRITE (NOUT,200) (ISTR,J=1,8),NBOU(NBCL),(ISTR,J=1,IM3)
   WRITE (NOUT,160) (DIST(J),J=NDX,NDRS)
   WRITE (NOUT,170)
   GO TO 120
70 WRITE (NOUT,150) ISTR,(ISTR,J=1,IM2),NBOU(NBCR)
   IF (IMM.EQ.0) GO TO 80
   WRITE (NOUT,130) ISTR,(ISTR,J=1,IMM),NBOU(NBCR)
   WRITE (NOUT,140) ISTR,(MATS(J),ISTR,J=NDX,NDS),MATS(NDS+1),NBOU
1  (NBCR)
   WRITE (NOUT,130) ISTR,(ISTR,J=1,IMM),NBOU(NBCR)
   GO TO 90
80 WRITE (NOUT,130) ISTR,NBOU(NBCR)
   WRITE (NOUT,140) ISTR,MATS(NDS+1),NBOU(NBCR)
   WRITE (NOUT,130) ISTR,NBOU(NBCR)
90 WRITE (NOUT,150) ISTR,(ISTR,J=1,IM2),NBOU(NBCR)
   WRITE (NOUT,160) (DIST(J),J=NDX,NDRE)
   WRITE (NOUT,170)
   GO TO 120
100 IF ((NGEOM.NE.1).AND.(NBCL.EQ.2)) GO TO 110
   WRITE (NOUT,150) NBOU(NBCL),(ISTR,J=1,IM2),NBOU(NBCR)
   WRITE (NOUT,130) NBOU(NBCL),(ISTR,J=1,IMM),NBOU(NBCR)
   WRITE (NOUT,140) NBOU(NBCL),(MATS(J),ISTR,J=NDX,NDS),MATS(NDS+1)
1  ,NBOU(NBCR)
   WRITE (NOUT,130) NBOU(NBCL),(ISTR,J=1,IMM),NBOU(NBCR)
   WRITE (NOUT,150) NBOU(NBCL),(ISTR,J=1,IM2),NBOU(NBCR)
   WRITE (NOUT,160) (DIST(J),J=NDX,NDRE)
   WRITE (NOUT,170)
   GO TO 120
110 WRITE (NOUT,200) (ISTR,J=1,8),NBOU(NBCL),(ISTR,J=1,IM3),NBOU(NBCR)

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        WRITE (NOUT,130) ISTR,NBOU(NBCL),(ISTR,J=1,IMM1),NBOU(NBCR)
        WRITE (NOUT,210) ISTR,MATS(1),NBOU(NBCL),(MATS(J),ISTR,J=2,NDS)
1      ,MATS(NDS+1),NBOU(NBCR)
        WRITE (NOUT,130) ISTR,NBOU(NBCL),(ISTR,J=1,IMM1),NBOU(NBCR)
        WRITE (NOUT,200) (ISTR,J=1,8),NBOU(NBCL),(ISTR,J=1,IM3),NBOU(NBCR)
        WRITE (NOUT,160) (DIST(J),J=NDX,NDRE)
        WRITE (NOUT,170)
120    CONTINUE
        RETURN
C
130    FORMAT (5X,A1,15(7X,A1))
140    FORMAT (5X,A1,15(I4,3X,A1))
150    FORMAT (5X,A1,15(8A1))
160    FORMAT (3X,16(F7.3,1X))
170    FORMAT (/)
180    FORMAT (1H1,/)
190    FORMAT (54X,13HGEOMETRIC MAP,/50X,20H(NOT DRAWN TO SCALE),//43X,35
1      HTHE GEOMETRY FOR THIS PROBLEM IS A ,A9,//37X,47HBOUNDARY CONDITI
2      ON TYPE INDICATED ON BOUNDARIES,/40X,41H MATERIAL TYPE INDICATED IN
3      CENTER OF CELL,/39X,43H RADII GIVEN FROM CENTER LINE IN CENTIMETER
4      S,/)
200    FORMAT (5X,8A1,A1,14(8A1))
210    FORMAT (5X,A1,3X,I1,3X,A1,14(I4,3X,A1))
        END
        SUBROUTINE CONCLPT (NANMAT,CONBOU,DAPLOT,ISO,NCELL,NISO1,NISO
1      ,NTIME,NP,NTIM,NPP,NBCL,NBCR,VOL)
C      PRINT RESULTS OF PROBLEM
        DIMENSION NANMAT(NISO1,9), CONBOU(NISO,2), DAPLOT(NISO,NCELL,NTIME
1      ), NPP(NCELL), VOL(NCELL)
        COMMON /IO/ NINP, NOUT, IER, NPRINT
        COMMON /TIMES/ TINT, TINC, TIMAX
        DATA BNDRY /10HREFLECTED /
        TIME=0.0
C      TERMINAL OUTPUT
        NBOX=4
C      LINE PRINTER OUTPUT
        IF (NPRINT.EQ.0) NBOX=6
        NBOX1=NBOX+1
        NP1=NP-NBOX
        IF (MOD(NP1,NBOX1)) 20,10,10
10     LOOP=NP1/NBOX1+2
        GO TO 30
20     LOOP=NP1/NBOX1+1
30     DO 40 I=1,NP
40     NPP(I)=I
        IF (NBCL.EQ.2) GO TO 60
        DO 50 K=1,ISO
50     CONBOU(K,1)=BNDRY
60     IF (NBCR.EQ.2) GO TO 80
        DO 70 K=1,ISO
70     CONBOU(K,2)=BNDRY
80     DO 470 I=1,NTIM
        INP=NP
        ILINE=0
        ICOUNT=0
        TIME=TINT+((TIMAX-TINT)/TINC)*(I-1)
        IF (NPRINT.EQ.1) GO TO 90
        WRITE (NOUT,490) TIME
        GO TO 100
90     WRITE (NOUT,500) TIME
100    DO 450 II=1,LOOP
        ICOUNT=ICOUNT+1
        IE=MINO(NBOX,INP)
        NDX=(II*NBOX-NBOX)+1
        NDS=IE+(II*NBOX-NBOX)
        INP=INP-NBOX
        IF (LOOP.EQ.1) GO TO 240
        IF (II.EQ.1) GO TO 120
        IF (ICOUNT.EQ.LOOP) GO TO 160
        IE=IE+1
        NDX=NDX+II-2

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NDS=NDS+II-1
INP=INP-1
WRITE (NOUT,550) IE,(NPP(J),J=NDX,NDS)
DO 110 III=1,ISO
110 WRITE (NOUT,560) NANMAT(III,1),(DAPLOT(III,J,I),J=NDX,NDS)
GO TO 440
120 WRITE (NOUT,510) IE,(NPP(J),J=NDX,NDS)
IF (NBCL.EQ.1) GO TO 140
DO 130 III=1,ISO
130 WRITE (NOUT,520) NANMAT(III,1),CONBOU(III,1),(DAPLOT(III,J,I),J
1 =NDX,NDS)
GO TO 440
140 DO 150 III=1,ISO
150 WRITE (NOUT,630) NANMAT(III,1),CONBOU(III,1),(DAPLOT(III,J,I),J
1 =NDX,NDS)
GO TO 440
160 NDX=NDX+II-2
NDS=NDS+II-2
IF (IE.EQ.0) GO TO 200
WRITE (NOUT,570) IE,IE,(NPP(J),J=NDX,NDS)
IF (NBCR.EQ.1) GO TO 180
DO 170 III=1,ISO
170 WRITE (NOUT,580) NANMAT(III,1),IE,(DAPLOT(III,J,I),J=NDX,NDS)
1 ,CONBOU(III,2)
GO TO 440
180 DO 190 III=1,ISO
190 WRITE (NOUT,640) NANMAT(III,1),IE,(DAPLOT(III,J,I),J=NDX,NDS)
1 ,CONBOU(III,2)
GO TO 440
200 WRITE (NOUT,610)
IF (NBCR.EQ.1) GO TO 220
DO 210 III=1,ISO
210 WRITE (NOUT,620) NANMAT(III,1),CONBOU(III,2)
GO TO 440
220 DO 230 III=1,ISO
230 WRITE (NOUT,650) NANMAT(III,1),CONBOU(III,2)
GO TO 440
240 IF (IE.EQ.NBOX) GO TO 320
WRITE (NOUT,590) IE,IE,(NPP(J),J=NDX,NDS)
IF (NBCL.EQ.1.AND.NBCR.EQ.1) GO TO 300
IF (NBCL.EQ.1) GO TO 260
IF (NBCR.EQ.1) GO TO 280
DO 250 III=1,ISO
250 WRITE (NOUT,600) NANMAT(III,1),CONBOU(III,1),IE,(DAPLOT(III,J,I),J
1 =NDX,NDS),CONBOU(III,2)
GO TO 440
260 DO 270 III=1,ISO
270 WRITE (NOUT,660) NANMAT(III,1),CONBOU(III,1),IE,(DAPLOT(III,J,I),J
1 =NDX,NDS),CONBOU(III,2)
GO TO 440
280 DO 290 III=1,ISO
290 WRITE (NOUT,670) NANMAT(III,1),CONBOU(III,1),IE,(DAPLOT(III,J,I),J
1 =NDX,NDS),CONBOU(III,2)
GO TO 440
300 DO 310 III=1,ISO
310 WRITE (NOUT,680) NANMAT(III,1),CONBOU(III,1),IE,(DAPLOT(III,J,I),J
1 =NDX,NDS),CONBOU(III,2)
GO TO 440
320 WRITE (NOUT,510) IE,(NPP(J),J=NDX,NDS)
IF (NBCL.EQ.1.AND.NBCR.EQ.1) GO TO 410
IF (NBCL.EQ.1) GO TO 350
IF (NBCR.EQ.1) GO TO 380
DO 330 III=1,ISO
330 WRITE (NOUT,520) NANMAT(III,1),CONBOU(III,1),(DAPLOT(III,J,I),J
1 =NDX,NDS)
WRITE (NOUT,530)
WRITE (NOUT,610)
DO 340 III=1,ISO
340 WRITE (NOUT,620) NANMAT(III,1),CONBOU(III,2)
GO TO 440
350 DO 360 III=1,ISO

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360 WRITE (NOUT,690) NANMAT(III,1),CONBOU(III,1),(DAPLOT(III,J,I),J
1 =NDX,NDS)
WRITE (NOUT,530)
WRITE (NOUT,610)
DO 370 III=1,ISO
370 WRITE (NOUT,700) NANMAT(III,1),CONBOU(III,2)
GO TO 440
380 DO 390 III=1,ISO
390 WRITE (NOUT,710) NANMAT(III,1),CONBOU(III,1),(DAPLOT(III,J,I),J
1 =NDX,NDS)
WRITE (NOUT,530)
WRITE (NOUT,610)
DO 400 III=1,ISO
400 WRITE (NOUT,720) NANMAT(III,1),CONBOU(III,2)
GO TO 440
410 DO 420 III=1,ISO
420 WRITE (NOUT,730) NANMAT(III,1),CONBOU(III,1),(DAPLOT(III,J,I),J
1 =NDX,NDS)
WRITE (NOUT,530)
WRITE (NOUT,610)
DO 430 III=1,ISO
430 WRITE (NOUT,740) NANMAT(III,1),CONBOU(III,2)
440 WRITE (NOUT,530)
IF (NPRINT.EQ.1) GO TO 450
ILL=ISO+3
ILINES=ILINES+ILL
IF ((ILINES+ILL).GT.55) WRITE (NOUT,540)
450 CONTINUE
ATOMS=0.
DO 460 III=1,ISO
DO 460 J=1,NP
ATOMS=ATOMS+VOL(J)*DAPLOT(III,J,I)
460 CONTINUE
WRITE (NOUT,480) ATOMS
470 CONTINUE
RETURN

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C

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480 FORMAT (15H NO. OF ATOMS =,1PE22.15)
490 FORMAT (1H1,/,37X,23HCELL CONCENTRATIONS AT ,1PE12.5,5H DAYS,/40X
1 ,28H(CONCENTRATIONS IN ATOMS/CC))
500 FORMAT (/,20X,23HCELL CONCENTRATIONS AT ,1PE12.5,5H DAYS,/23X,28H
1(CONCENTRATIONS IN ATOMS/CC))
510 FORMAT (13X,4HLEFT,/22H ISOTOPE BOUNDARY ,=(3X,5HCELL ,I2,3X))
520 FORMAT (1X,A7,1PE13.5,8(1PE13.5))
530 FORMAT (/)
540 FORMAT (1H1,/)
550 FORMAT (9H ISOTOPE ,=(3X,5HCELL ,I2,3X))
560 FORMAT (1X,A7,9(1PE13.5))
570 FORMAT (9X,=(13X),4X,5HRIGHT,/9H ISOTOPE ,=(3X,5HCELL ,I2,3X),10H
1 BOUNDARY)
580 FORMAT (1X,A7,=(1PE13.5),1PE13.5)
590 FORMAT (13X,4HLEFT,4X,=(13X),4X,5HRIGHT,/22H ISOTOPE BOUNDARY
1 ,=(3X,5HCELL ,I2,3X),9H BOUNDARY)
600 FORMAT (1X,A7,1PE13.5,=(1PE13.5),1PE13.5)
610 FORMAT (13X,5HRIGHT,/19H ISOTOPE BOUNDARY)
620 FORMAT (1X,A7,1PE13.5)
630 FORMAT (1X,A7,3X,A10,8(1PE13.5))
640 FORMAT (1X,A7,=(1PE13.5),3X,A10)
650 FORMAT (1X,A7,3X,A10)
660 FORMAT (1X,A7,3X,A10,=(1PE13.5),1PE13.5)
670 FORMAT (1X,A7,1PE13.5,=(1PE13.5),2X,A10)
680 FORMAT (1X,A7,3X,A10,=(1PE13.5),2X,A10)
690 FORMAT (1X,A7,3X,A10,8(1PE13.5))
700 FORMAT (1X,A7,1PE13.5)
710 FORMAT (1X,A7,1PE13.5,8(1PE13.5))
720 FORMAT (1X,A7,3X,A10)
730 FORMAT (1X,A7,3X,A10,8(1PE13.5))
740 FORMAT (1X,A7,3X,A10)
END
SUBROUTINE TEMADJ (TEMPS,TEMCOR,NTEMPS,RBAR,NCELLS,W,A,B,C,NTEM)
EVALUATE TEMPERATURE FIELD FROM DATA SUPPLIED IN INPB

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C

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      DIMENSION TEMPS(NTEM), TEMCOR(NTEM), RBAR(NCELLS), W(NTEM), A(NTEM
1  ), B(NTEM), C(NTEM), IOP(2), TAB(3)
      IJ=1
      IOP(1)=5
      IOP(2)=5
      CALL SPL1D1 (NTEMPS,TEMCOR,TEMPS,W,IOP,IJ,A,B,C)
      DO 10 J=1,NCELLS
      DUM=REAR(J)
      CALL SPL1D2 (NTEMPS,TEMCOR,TEMPS,W,IJ,DUM,TAB)
      A(J)=TAB(1)
10  CONTINUE
      DO 20 J=1,NCELLS
      TEMPS(J)=A(J)
20  CONTINUE
      RETURN
      END
      SUBROUTINE MAKLAM (NANMAT,ANMAT,XSEC,NXSEC,PHI,BRV,ALAM,BB,NISO1
1  ,NXS,NXSP,NBR,NGP,ISO,IXS,IGP,NCELL,K)
C    MAKLAM CONSTRUCTS THE DECAY CHAIN MATRIX
      DIMENSION NANMAT(NISO1,9), ANMAT(NISO1,2), XSEC(NXS,NGP,4), PHI
1  (NCELL,NGP), BRV(NBR), ALAM(ISO,ISO), NXSEC(NXSP,4), BB(ISO,ISO)
      DO 10 IK=1,ISO
      DO 10 JK=1,ISO
      ALAM(IK,JK)=0.0
10  BB(IK,JK)=0.0
      IBR=1
      DO 120 IK=1,ISO
      DO 110 JK=1,ISO
      DO 40 IDX=3,4
C    IDENTIFY DECAY PARENTS AND STORE IN MATRIX ALAM
      IF (IAES(NANMAT(IK,IDX)).NE.JK) GO TO 40
      IF (NANMAT(IK,IDX)) 20,20,30
20  ALAM(IK,JK)=BRV(IBR)*ANMAT(JK,1)
      IBR=IBR+1
      GO TO 40
30  ALAM(IK,JK)=ANMAT(JK,1)
40  CONTINUE
      DO 100 IDX=5,9
C    IDENTIFY NEUTRON REACTION SOURCES
      IF (IAES(NANMAT(IK,IDX)).NE.JK) GO TO 100
      DO 50 J=1,IXS
      IF (JK.NE.NXSEC(J,4)) GO TO 50
      NM=J
      GO TO 60
50  CONTINUE
      PRINT 140, JK
      CALL EXIT
60  CONTINUE
      MM=1
      IF (IDX.EQ.7) MM=2
      IF (IDX.EQ.8) MM=3
      IF (IDX.EQ.9) MM=4
C    WEIGHT CROSS SECTIONS AND STORE IN MATRIX BB
      CALL WXSEC (SIGPHI,PHI,XSEC,NM,MM,IGP,NGP,NXS,NCELL,K)
      IF (NANMAT(IK,IDX)) 70,70,80
70  BB(IK,JK)=SIGPHI*BRV(IBR)
      IBR=IBR+1
      GO TO 90
80  BB(IK,JK)=SIGPHI
90  BB(JK,JK)=BB(JK,JK)-SIGPHI
100 CONTINUE
110 CONTINUE
      ALAM(IK,IK)=-ANMAT(IK,1)
120 CONTINUE
      DO 130 IK=1,ISO
      DO 130 JK=1,ISO
130 ALAM(IK,JK)=-ALAM(IK,JK)-BB(IK,JK)
      RETURN
C
140 FORMAT (1H0,4X,*CROSS SECTIONS CANNOT BE FOUND FOR NUCLIDE *,I4)
      END

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SUBROUTINE DIJADJ (DIJO,AIJS,TEMPS,DIFFK,NISO,NMATS,NCELL,ISO,K,KK
1 )
C USE ARRHENIUS RELATION TO ADJUST DIFFUSION COEFFICIENTS
DIMENSION DIJO(NISO,NISO,NMATS), AIJS(NISO,NISO,NMATS)
DIMENSION DIFFK(ISO,ISO), TEMPS(NCELL)
C R=1.987 CAL/K-MOLE
C T DEGREES KELVIN
C DIJO CM**2/SEC
C AIJS CAL/MOLE
R=1.987
DO 20 J=1,ISO
DO 10 JJ=1,ISO
EXPON=-AIJS(J,JJ,KK)/(R*TEMPS(K))
DIFFK(J,JJ)=DIJO(J,JJ,KK)*EXP(EXPON)
10 CONTINUE
20 CONTINUE
RETURN
END
SUBROUTINE BCONL (BK,AREA,DIFFK,DELR,SOURCE,CONBOU,NCELLS,ISO,NBCL
1 ,NGEOM,NISO,NIC,DUM11,DUM33)
C SET LEFT BOUNDARY CONDITION
DIMENSION AREA(NCELLS), DIFFK(ISO,ISO), DELR(NCELLS), SOURCE(NIC),
1 CONBOU(NISO,2), BK(ISO,ISO), DUM11(ISO), DUM33(NIC)
IF (NBCL.EQ.2) GO TO 30
IF (NBCL.NE.1) GO TO 80
DO 20 I=1,ISO
DO 10 J=1,ISO
BK(I,J)=0.0
10 CONTINUE
20 CONTINUE
RETURN
30 IF (NGEOM.GT.1) GO TO 40
CON=2./DELR(1)
CALL SCALAR (DIFFK,CON,BK,ISO,ISO)
GO TO 50
40 CON=2.*AREA(1)/DELR(2)
CALL SCALAR (DIFFK,CON,BK,ISO,ISO)
50 CONTINUE
DO 60 I=1,ISO
DUM11(I)=CONBOU(I,1)
60 CONTINUE
CALL MATMPY (ISO,ISO,1,BK,ISO,DUM11,NISO,DUM33,NIC)
DO 70 I=1,ISO
70 SOURCE(I)=SOURCE(I)+DUM33(I)
RETURN
80 CONTINUE
PRINT 90
RETURN
C 90 FORMAT (5X,*LEFT BOUNDARY CONDITION IMPROPERLY SPECIFIED*)
END
SUBROUTINE BCONR (AK,AREA,DIFFK,DELR,SOURCE,CONBOU,NCELLS,ISO,NECR
1 ,NISO,NIC,DUM11,DUM22,BK,CKK,ALAM,VOL,DIFDUM1)
C SET RIGHT BOUNDARY CONDITION
DIMENSION AREA(NCELLS), DIFFK(ISO,ISO), DELR(NCELLS), SOURCE(NIC),
1 CONBOU(NISO,2), AK(ISO,ISO), DUM11(ISO), DUM22(ISO)
DIMENSION BK(ISO,ISO), CKK(ISO,ISO), ALAM(ISO,ISO), VOL(NCELLS),
1 DIFDUM1(ISO,ISO)
IF (NECR.EQ.2) GO TO 30
IF (NECR.NE.1) GO TO 90
DO 20 I=1,ISO
DO 10 J=1,ISO
AK(I,J)=0.0
10 CONTINUE
20 CONTINUE
GO TO 60
30 CON=2.*AREA(NCELLS)/DELR(NCELLS)
CALL SCALAR (DIFFK,CON,AK,ISO,ISO)
DO 40 I=1,ISO
DUM11(I)=CONBOU(I,2)
40 CONTINUE

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      CALL MATMPY (ISO,ISO,1,AK,ISO,DUM11,NISO,DUM22,NIC)
      J=NIC-ISO
      DO 50 I=1,ISO
        SOURCE(J+I)=SOURCE(J+I)+DUM22(I)
50    CONTINUE
60    CALL SCALAR (ALAM,VOL(NCELLS),DIFDUM1,ISO,ISO)
      DO 80 I1=1,ISO
        DO 70 I2=1,ISO
          CKK(I1,I2)=-AK(I1,I2)-BK(I1,I2)-DIFDUM1(I1,I2)
70    CONTINUE
80    CONTINUE
      RETURN
90    CONTINUE
      PRINT 100
      RETURN
C
100  FORMAT (5X,*RIGHT BOUNDARY CONDITION IMPROPERLY SPECIFIED*)
      END
      SUBROUTINE BIGEL (DIFFK,DIFFK1,DIFDUM1,DIFDUM2,ALAM,AK,BK,CKK,ISO
C
1  ,AREA,VOL,DELR,NCELLS,IPVT,Z,I)
      EVALUATE ELEMENTS OF BIG MATRIX; A, B, AND K
      DIMENSION DIFFK(ISO,ISO), DIFFK1(ISO,ISO), DIFDUM1(ISO,ISO),
1  DIFDUM2(ISO,ISO), ALAM(ISO,ISO), AK(ISO,ISO), BK(ISO,ISO), CKK
2  (ISO,ISO), IPVT(ISO), Z(ISO), DET(2)
      DIMENSION AREA(NCELLS), VOL(NCELLS), DELR(NCELLS)
      DO 20 I1=1,ISO
        DO 10 I2=1,ISO
          DIFDUM1(I1,I2)=DIFFK(I1,I2)+DIFFK1(I1,I2)
10    CONTINUE
20    CONTINUE
      CALL SGECO (DIFDUM1,ISO,ISO,IPVT,RCOND,Z)
      CALL SGEDI (DIFDUM1,ISO,ISO,IPVT,DET,Z,01)
      CALL MATMPY (ISO,ISO,ISO,DIFDUM1,ISO,DIFFK1,ISO,DIFDUM2,ISO)
      CALL MATMPY (ISO,ISO,ISO,DIFFK,ISO,DIFDUM2,ISO,DIFDUM1,ISO)
      CON=4.*AREA(I)/(DELR(I)+DELR(I+1))
      CALL SCALAR (DIFDUM1,CON,AK,ISO,ISO)
      CALL SCALAR (ALAM,VOL(I),DIFDUM1,ISO,ISO)
      DO 40 I1=1,ISO
        DO 30 I2=1,ISO
          CKK(I1,I2)=-AK(I1,I2)-BK(I1,I2)-DIFDUM1(I1,I2)
          BK(I1,I2)=AK(I1,I2)
30    CONTINUE
40    CONTINUE
      RETURN
C
      END
      SUBROUTINE MAKEB (BIGB,AK,BK,CKK,NIC,ISO,VOL,NCELLS,ICOL,II)
C
      CONSTRUCT BIG MATRIX
      DIMENSION BIGB(NIC,NIC), AK(ISO,ISO), BK(ISO,ISO), CKK(ISO,ISO),
1  VOL(NCELLS)
      LEVEL 2, BIGB
      IVOL=ICOL+II-1
      DO 20 I=1,ISO
        IR1=ICOL*ISO-ISO+I
        IR2=ICOL*ISO+I
        DO 10 J=1,ISO
          IC1=ICOL*ISO-ISO+J
          IC2=ICOL*ISO+J
          BIGB(IR1,IC1)=CKK(I,J)/VOL(IVOL)
          BIGB(IR1,IC2)=AK(I,J)/VOL(IVOL+1)
          BIGB(IR2,IC1)=BK(I,J)/VOL(IVOL)
10    CONTINUE
20    CONTINUE
      ICOL=ICOL+1
      RETURN
      ENTRY MAKEBL
      IVOL=ICOL+II-1
      DO 40 I=1,ISO
        IR1=ICOL*ISO-ISO+I
        DO 30 J=1,ISO
          IC1=ICOL*ISO-ISO+J

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30 BIGE(IR1,IC1)=CKK(I,J)/VOL(IVOL)
40 CONTINUE
   RETURN
   END
C   SUBROUTINE WXSEC (SIGPHI,PHI,XSEC,M,N,IGP,NGP,NXS,NCELL,K)
   WEIGHT CROSS SECTIONS
   DIMENSION PHI(NCELL,NGP), XSEC(NXS,NGP,4)
   SIGPHI=0.0
   DO 10 J=1,IGP
10  SIGPHI=SIGPHI+PHI(K,J)*XSEC(M,J,N)
   RETURN
   END
C   SUBROUTINE MAKVOL (VOLMAT,NIC,VOL,NCELLS,II,ISO)
   CONSTRUCT DIAGONAL VOLUME MATRIX
   DIMENSION VOLMAT(NIC,NIC), VOL(NCELLS)
   LEVEL 2, VOLMAT
   DO 20 I=1,NIC
   DO 10 J=1,NIC
   VOLMAT(I,J)=0.0
   IF (I.NE.J) GO TO 10
   IJ=(I-1)/ISO+II
   VOLMAT(I,J)=VOL(IJ)
10  CONTINUE
20  CONTINUE
   RETURN
   END
C   SUBROUTINE SOLVER (A,B,C,D,E,F,TINCD,I,NN)
C   SOLVER EVALUATES D(A) AND I+A*D(A)
C   THESE VALUES ARE RETURNED IN D AND E.
C   THE FOLLOWING ARE REQUIRED ROUTINES
C       IFACT - CALCULATES FACTORIALS
C       SCALAR - MULTIPLIES A SCALAR TIMES A MATRIX
C       GENID - CREATES AN IDENTITY MATRIX
C       MATMOV - SETS TWO MATRICES EQUAL
C       MPYEC3 - MULTIPLIES TWO LCM MATRICES - CALLS SDOT
C       SDOT - CALCULATES THE DOT PRODUCT OF TWO VECTORS
C   DIMENSION A(NN,NN), B(NN,NN), C(NN,NN), D(NN,NN), E(NN,NN), F(NN
1,NN)
   LEVEL 2, A, B, C, D, E, F
   EPS=1.0E-15
   Y=-ALOG(EPS)
   TLOG=ALOG(2.0)
   DO 10 M=1,20
   FACT=IFACT(M+2)
   X=(M+1)*TLOG+ALOG(FACT)
   IF (X.GE.Y) GO TO 20
10  CONTINUE
20  CONTINUE
   SUM=0.0
   DO 40 JJ=1,I
   DO 30 J=1,I
   SUM=SUM+A(J,JJ)*A(J,JJ)
30  CONTINUE
40  CONTINUE
C   THIS USES SCHUR'S THEOREM FOR THE BOUND OF THE MAXIMUM EIGENVALUE
P=(0.5*ALOG(SUM)+ALOG(TINCD))/TLOG
IF (P) 50,50,60
50  NP=1
   GO TO 70
60  NP=P+1.0
70  CONTINUE
   S=1.
   DO 80 NLOOP=1,NP
   S=S*2.
80  CONTINUE
C   THIS LOOP IS USED IN PLACE OF 2**NP AS THAT WAS SET TO ZERO
C   FOR NP GREATER THAN 48 (CDC-6600)
   T=TINCD/S
   CALL SCAECS (A,T,C,I,NN)
   CALL GENID (D,I,NN)

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C   CALCULATE D(H)
    DO 100 J=1,M
      FM=1.0/(M+2.0-J)
      CALL SCAECS (D,FM,F,I,NN)
      CALL MPYEC3 (I,I,I,C,NN,F,NN,D,NN)
      DO 90 JJ=1,I
        D(JJ,JJ)=D(JJ,JJ)+1.0
    90 CONTINUE
    100 CONTINUE
      CALL MPYEC3 (I,I,I,C,NN,D,NN,E,NN)
      DO 110 JJ=1,I
        E(JJ,JJ)=E(JJ,JJ)+1.0
    110 CONTINUE
C   D AND E CONTAIN THE SCALED DOWN VALUES
      CALL GENID (C,I,NN)
      SI=1.0/S
      DO 130 J=1,NP
        CALL MOVECS (I,I,E,NN,F,NN)
        CALL MPYEC3 (I,I,I,E,NN,F,NN,B,NN)
        CALL MOVECS (I,I,E,NN,E,NN)
        DO 120 JJ=1,I
          F(JJ,JJ)=F(JJ,JJ)+1.0
    120 CONTINUE
      CALL MPYEC3 (I,I,I,C,NN,F,NN,B,NN)
      CALL MOVECS (I,I,E,NN,C,NN)
    130 CONTINUE
C   C CONTAINS THE ENTIRE PRODUCT
      CALL SCAECS (D,SI,F,I,NN)
      CALL MPYEC3 (I,I,I,F,NN,C,NN,D,NN)
C   I + A * D(A) IS IN E
C   TEST E MATRIX FOR ALL ZEROS
      SUM=0.
      DO 150 JJ=1,I
        DO 140 J=1,I
          SUM=SUM+E(J,JJ)
    140 CONTINUE
    150 CONTINUE
      IF (SUM.NE.0.0) RETURN
      PRINT 160
      STOP
    160 FORMAT (32H ALARM SOUNDED.  E MATRIX ZERO. )
      END
      SUBROUTINE FSOLVE (VOLMAT,C,D,E,DUM33,DTIME,NIC,CONINT,SOURCE
1,CONCEN)
C   CONSTRUCT SOLUTION FROM RESULTS OF SOLVER
      DIMENSION VOLMAT(NIC,NIC), C(NIC,NIC), D(NIC,NIC), E(NIC,NIC),
1 DUM33(NIC), CONINT(NIC), SOURCE(NIC), CONCEN(NIC)
      LEVEL 2, VOLMAT, C, D, E
C   CALL PRIMES(VOLMAT,NIC,NIC,NIC,NIC,10H VOLMAT ,10H )
C   CALL PRIV(CONINT,NIC,NIC,10H CONINT ,10H )
      CALL MPYEC1 (NIC,NIC,1,VOLMAT,NIC,CONINT,NIC,CONCEN,NIC)
C   CALL PRIV(CONCEN,NIC,NIC,10H VOLMAT*CO,10HNINT )
      CALL MPYEC1 (NIC,NIC,1,E,NIC,CONCEN,NIC,CONINT,NIC)
C   CALL PRIV(CONINT,NIC,NIC,10H VOLMAT*CO,10HNINT*E )
      DO 10 I=1,NIC
        VOLMAT(I,I)=1./VOLMAT(I,I)
    10 CONTINUE
      CALL MPYEC1 (NIC,NIC,1,VOLMAT,NIC,CONINT,NIC,CONCEN,NIC)
C   CALL PRIV(CONCEN,NIC,NIC,10H FIRST PAR,10HT )
      CALL MPYEC1 (NIC,NIC,1,D,NIC,SOURCE,NIC,CONINT,NIC)
C   CALL PRIV(CONINT,NIC,NIC,10H D*SOURCE ,10H )
      CALL SCAECS (VOLMAT,DTIME,C,NIC,NIC)
C   CALL PRIMES(C,NIC,NIC,NIC,NIC,10H DTIME*VOL,10HMAT )
      CALL MPYEC1 (NIC,NIC,1,C,NIC,CONINT,NIC,DUM33,NIC)
C   CALL PRIV(DUM33,NIC,NIC,10H SECOND PA,10HRT )
      DO 20 I=1,NIC
        VOLMAT(I,I)=1./VOLMAT(I,I)
        CONCEN(I)=CONCEN(I)+DUM33(I)
    20 CONTINUE
C   CALL PRIV(CONCEN,NIC,NIC,10H ANSWER ,10H )
      RETURN
      END

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C      SUBROUTINE SCALAR (A,S,B,N,NDIM)
      SCALAR MULTIPLIES A SCALAR TIMES A MATRIX
      DIMENSION A(NDIM,NDIM), B(NDIM,NDIM)
      DO 10 J=1,N
      DO 10 I=1,N
      B(I,J)=S*A(I,J)
10    CONTINUE
      RETURN
      END
C      SUBROUTINE SCAECS (A,S,B,N,NDIM)
      SCAECS MULTIPLIES A SCALAR TIMES A MATRIX
      LEVEL 2, A, B
      DIMENSION A(NDIM,NDIM), B(NDIM,NDIM)
      DO 10 J=1,N
      DO 10 I=1,N
      B(I,J)=S*A(I,J)
10    CONTINUE
      RETURN
      END
C      FUNCTION IFACT (N)
      EVALUATE N FACTORIAL
      IFACT=1
      IF (N.LE.1) RETURN
      DO 10 I=1,N
      IFACT=IFACT*I
10    CONTINUE
      RETURN
      END
C      SUBROUTINE GENID (A,N,IA)
      GENERATE IDENTITY MATRIX
      DIMENSION A(IA,N)
      LEVEL 2, A
      DO 20 J=1,N
      DO 10 I=1,N
10    A(I,J)=0.0
20    A(J,J)=1.0
      RETURN
      END
C      SUBROUTINE MATMOV (N,M,A,IA,B,IB)
      EQUIVALENCE TWO MATRICES
      DIMENSION A(IA,M), B(IB,M)
      DO 10 J=1,M
      DO 10 I=1,N
10    B(I,J)=A(I,J)
      RETURN
      END
C      SUBROUTINE MOVECS (N,M,A,IA,B,IB)
      EQUIVALENCE TWO LCM MATRICES
      DIMENSION A(IA,M), B(IB,M)
      LEVEL 2, A, B
      DO 10 J=1,M
      DO 10 I=1,N
10    B(I,J)=A(I,J)
      RETURN
      END
C      SUBROUTINE MATMPY (N,M,L,A,IA,B,IB,C,IC)
      MULTIPLY TWO MATRICES
      DIMENSION A(IA,M), B(IB,L), C(IC,L)
      DO 10 J=1,L
      DO 10 I=1,N
10    C(I,J)=SDOT(M,A(I,1),IA,B(1,J),1)
      RETURN
      END
C      SUBROUTINE MPYEC3 (N,M,L,A,IA,B,IB,C,IC)
      MULTIPLY TWO LCM MATRICES
      DIMENSION A(IA,M), B(IB,L), C(IC,L)
      LEVEL 2, A, B, C
      DO 20 J=1,L
      DO 20 I=1,N
      AM=0.0
      DO 10 K=1,M

```

```

10 AM=AM+A(I,K)*B(K,J)
20 C(I,J)=AM
   RETURN
   END
C   SUBROUTINE MPYEC1 (N,M,L,A,IA,B,IB,C,IC)
   MULTIPLY A SCM AND LCM MATRIX
   DIMENSION A(IA,M), B(IB,L), C(IC,L)
   LEVEL 2, A
   DO 20 J=1,L
   DO 20 I=1,N
   AM=0.0
   DO 10 K=1,M
10  AM=AM+A(I,K)*B(K,J)
20  C(I,J)=AM
   RETURN
   END
C   SUBROUTINE PRIM (A,N1,N2,N1D,N2D,TITLE1,TITLE2)
   PRINT A MATRIX
   DIMENSION A(N1D,N2D)
   PRINT 20, TITLE1,TITLE2
   DO 10 J=1,N1
10  PRINT 30, (A(J,JJ),JJ=1,N2)
   RETURN
C
20  FORMAT (/1X,2A10/)
30  FORMAT (6E13.5)
   END
C   SUBROUTINE PRIMES (A,N1,N2,N1D,N2D,TITLE1,TITLE2)
   PRINT A LCM MATRIX
   DIMENSION A(N1D,N2D)
   LEVEL 2, A
   PRINT 20, TITLE1,TITLE2
   DO 10 J=1,N1
10  PRINT 30, (A(J,JJ),JJ=1,N2)
   RETURN
C
20  FORMAT (/1X,2A10/)
30  FORMAT (6E13.5)
   END
C   SUBROUTINE PRIV (A,N1,N1D,TITLE1,TITLE2)
   PRINT A VECTOR
   DIMENSION A(N1D)
   PRINT 10, TITLE1,TITLE2
   PRINT 20, (A(I),I=1,N1)
   RETURN
C
10  FORMAT (/1X,2A10,/)
20  FORMAT (6E13.5)
   END
C   SUBROUTINE REAG (ARRAY,NCOUNT,HOL1,HOL2)
C
C   READS FLOATING POINT DATA
   DIMENSION ARRAY(NCOUNT), V(12), K(12), IN(12)
   COMMON /IO/ NINP, NOUT, IER, NPRINT
   JFLAG=0
   J=1
10  IF (JFLAG.EQ.0) GO TO 30
   DO 20 JJ=1,6
   K(JJ)=K(JJ+6)
   IN(JJ)=IN(JJ+6)
20  V(JJ)=V(JJ+6)
   JFLAG=0
   GO TO 40
30  READ (NINP,200) (K(I),IN(I),V(I),I=1,6)
40  DO 160 I=1,6
   L=K(I)+1
   GO TO (50,60,80,170,120), L
C   NO MODIFICATION
50  ARRAY(J)=V(I)
   J=J+1
   GO TO 160

```

```

C      REPEAT
60    L=IN(I)
      DO 70 M=1,L
      ARRAY(J)=V(I)
70    J=J+1
      GO TO 160
C      INTERPOLATE
80    IF (I-6) 100,90,90
90    READ (NINP,200) (K(JJ),IN(JJ),V(JJ),JJ=7,12)
      JFLAG=1
100   L=IN(I)+1
      DEL=(V(I+1)-V(I))/FLOAT(L)
      DO 110 M=1,L
      ARRAY(J)=V(I)+DEL*FLOAT(M-1)
110   J=J+1
      GO TO 160
C      INTERPOLATE WITH CONSTANT RATIO
120   IF (I.LT.6) GO TO 130
      READ (NINP,200) (K(JJ),IN(JJ),V(JJ),JJ=7,12)
      JFLAG=1
130   L=MAX0(2,IN(I)+1)
      T1=0.
      T2=1.
      DO 140 JJ=1,L
      T1=T1+T2
140   T2=T2*V(I)
      T2=(V(I+1)-ARRAY(J-1))/T1
      L=MAX0(1,IN(I))
      DO 150 JJ=1,L
      ARRAY(J)=ARRAY(J-1)+T2
      T2=T2*V(I)
150   J=J+1
160   CONTINUE
      GO TO 10
C      TERMINATE
170   J=J-1
      WRITE (NOUT,210) HOL1,HOL2,J,(ARRAY(I),I=1,NCOUNT)
      IF (J-NCOUNT) 180,190,180
180   WRITE (NOUT,220) HOL1,HOL2
      IER=1
190   RETURN
C
200   FORMAT (6(I1,I2,E9,3))
210   FORMAT (/1X,2A6,I6/(6E13.5))
220   FORMAT (/33H INCORRECT NUMBER OF INPUT ITEMS ,2A6)
      END
      SUBROUTINE REAI (IARRAY,NCOUNT,HOL1,HOL2)
C
C      READS INTEGER DATA
      DIMENSION IARRAY(NCOUNT), IV(6), K(6), IN(6)
      COMMON /IO/ NINP, NOUT, IER, NPRINT
      J=1
10    READ (NINP,100) (K(I),IN(I),IV(I),I=1,6)
      DO 60 I=1,6
      L=K(I)+1
      GO TO (20,30,50,70), L
C      NO MODIFICATION
20    IARRAY(J)=IV(I)
      J=J+1
      GO TO 60
C      REPEAT
30    L=IN(I)
      DO 40 M=1,L
      IARRAY(J)=IV(I)
40    J=J+1
      GO TO 60
C      INTERPOLATE
50    WRITE (NOUT,120) HOL1,HOL2
      IER=1
      RETURN
60    CONTINUE

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      GO TO 10
C     TERMINATE
70    J=J-1
      WRITE (NOUT,110) HOL1,HOL2,J,(IARRAY(I),I=1,NCOUNT)
      IF (J-NCOUNT) 80,90,80
80    WRITE (NOUT,130) HOL1,HOL2
      IER=1
90    RETURN
C
100   FORMAT (6(I1,I2,I9))
110   FORMAT (/1X,2A6,I6/(6I12))
120   FORMAT (44H0ATTEMPTING TO INTERPOLATE BETWEEN INTEGERS ,2A6)
130   FORMAT (33H0INCORRECT NUMBER OF INPUT ITEMS ,2A6)
      END
      SUBROUTINE DRAW (NANMAT,REAR,DAPLOT,NTIM,NP,CONCEN,DUM33,NISO
1     ,NCELLS,NCELL,NTIME,ISO,NISO1,CONBOU,DIST,NCELL1,NBCL,NBCR)
C     DRAW PLOTS OF RESULTS
      DIMENSION NANMAT(NISO1,2), REAR(NCELLS), CONCEN(NP), DUM33(NP),
1     DAPLOT(NISO,NCELL,NTIME), DIST(NCELL1), CONBOU(NISO,2)
      DIMENSION X(2), Y(2), LABELX(3), LABELY(4)
      CALL GPLOT (1HU,10HDASH PLOTS,10)
      CALL EGNPL (0)
      CALL HEIGHT (0.25)
      Y(1)=0.0
      X(1)=DIST(1)
      X(2)=DIST(NCELLS+1)
      XSCALE=AINT(ALOG10(X(2)))
      XSCLDIV=10.**XSCALE
      IF (NP.EQ.NCELLS) GO TO 40
      IF (XSCALE.GE.2.) GO TO 20
      DO 10 I=1,NP
10     DUM33(I)=REAR(I+1)
      NX=13
      ENCODE (NX,160,LABELX)
      GO TO 80
20     X(2)=X(2)/XSCLDIV
      IXS=XSCALE
      NX=23
      ENCODE (NX,170,LABELX) IXS
      DO 30 I=1,NP
30     DUM33(I)=REAR(I+1)/XSCLDIV
      GO TO 80
40     IF (XSCALE.GE.2.) GO TO 60
      DO 50 I=1,NP
50     DUM33(I)=REAR(I)
      NX=13
      ENCODE (NX,160,LABELX)
      GO TO 80
60     DO 70 I=1,NP
70     DUM33(I)=REAR(I)/XSCLDIV
      X(2)=X(2)/XSCLDIV
      IXS=XSCALE
      NX=23
      ENCODE (NX,170,LABELX) IXS
80     DO 150 I=1,ISO
      Z=0.0
      DO 100 NT=1,NTIM
      DO 90 J=1,NP
      Z=AMAX1(Z,DAPLOT(I,J,NT))
90     CONTINUE
100    CONTINUE
      Y(2)=AMAX1(CONBOU(I,1),CONBOU(I,2),Z)
      IF (NBCL.EQ.1) Y(2)=AMAX1(CONBOU(I,2),Z)
      IF (NBCR.EQ.1) Y(2)=AMAX1(CONBOU(I,1),Z)
      IF (NBCL.EQ.1.AND.NBCR.EQ.1) Y(2)=Z
      YSCALE=AINT(ALOG10(Y(2)))
      YSCLDIV=1.0
      IF (YSCALE.LT.2.) GO TO 110
      YSCLDIV=10.**YSCALE
      Y(2)=Y(2)/YSCLDIV
      IYS=YSCALE
      NY=33

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        ENCODE (NY,180,LABELY) IYS
        GO TO 120
110 NY=23
        ENCODE (NY,190,LABELY)
120 CALL TITLE (NANMAT(1,1),7,LABELX,NX,LABELY,NY,5,5,8.)
        CALL GRAF (X(1),10HSCALE,X(2),Y(1),10HSCALE,Y(2))
        DO 140 NT=1,NTIM
        DO 130 J=1,NP
        CONCEN(J)=DAPLOT(I,J,NT)
130 CONCEN(J)=CONCEN(J)/YSCLDIV
        CALL CURVE (DUM33,CONCEN,NP,0)
140 CONTINUE
        CALL ENDPL (I)
150 CONTINUE
        CALL DONEPL
        RETURN
C
160 FORMAT (13HDISTANCE (CM))
170 FORMAT (21HDISTANCE (CM) X 10**-,I2)
180 FORMAT (31HCONCENTRATION (ATOM/CC) X 10**-,I2)
190 FORMAT (23HCONCENTRATION (ATOM/CC))
        END
        SUBROUTINE SPL1D1 (N,X,F,W,IOP,IJ,A,B,C)
        WHERE N= NUMBER OF POINTS IN THE INTERPOLATION
        X= ORIGIN OF TABLE OF INDEPENDENT VARIABLE
        F= ORIGIN OF TABLE OF DEPENDENT VARIABLE
        W= AN ARRAY OF DIMENSION N WHICH CONTAINS THE CALCULATED
          SECOND DERIVATIVES UPON RETURN
        IOP= AN ARRAY OF DIMENSION 2 WHICH CONTAINS COMBINATIONS OF
          THE INTEGERS 1 THRU 5 USED TO SPECIFY THE BOUNDARY
          CONDITIONS
        IJ= SPACING IN THE F AND W TABLES
        A,B,C= ARRAYS OF DIMENSION N USED FOR TEMPORARY STORAGE
        DIMENSION IOP(2), X(4), F(2), W(2), A(2), B(2), C(2), COMM(6)
        DATA (COMM(J),J=1,6) /8HSPL1D1 N,8H LESS TH,8HAN 4. RE,8HSULTS IN,
1 8HCORRECT.,8H /
        K=N-1
        A(2)=-((X(2)-X(1)))/6.
        B(2)=(X(3)-X(1))/3.
        W(IJ+1)=(F(2*IJ+1)-F(IJ+1))/(X(3)-X(2))-(F(IJ+1)-F(1))/(X(2)-X(1))
        IF (N-3) 10,30,10
10 DO 20 I=3,K
        M=(I-1)*IJ+1
        J1=M+IJ
        J2=M-IJ
        CON=(X(I+1)-X(I-1))/3.
        DON=(X(I)-X(I-1))/6.
        B(I)=CON-(DON**2)/B(I-1)
        E=(F(J1)-F(M))/(X(I+1)-X(I))-(F(M)-F(J2))/(X(I)-X(I-1))
        W(M)=E-(DON*W(J2))/B(I-1)
20 A(I)=-((DON*A(I-1))/B(I-1))
30 K1=(N-2)*IJ+1
        C(N-1)=-((X(N)-X(N-1))/6.)/B(N-1)
        W(K1)=W(K1)/B(N-1)
        A(N-1)=A(N-1)/B(N-1)
        K2=K-1
        IF (N-3) 40,60,40
40 DO 50 I=2,K2
        J=N-I
        CON=(X(J+1)-X(J))/6.
        A(J)=(A(J)-CON*A(J+1))/B(J)
        C(J)=-((CON*C(J+1))/B(J))
        K3=(J-1)*IJ+1
        M=K3+IJ
50 W(K3)=(W(K3)-CON*W(M))/B(J)
60 K4=(N-1)*IJ+1
        IF (IOP(1)-5) 70,90,70
70 C1=W(1)
        IF (IOP(2)-5) 80,110,80
80 C2=W(K4)
        GO TO 130

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90 IF (N-4) 570,100,100
100 A1=X(1)-X(2)
    A2=X(1)-X(3)
    A3=X(1)-X(4)
    A4=X(2)-X(3)
    A5=X(2)-X(4)
    A6=X(3)-X(4)
    W(1)=F(1)*(1./A1+1./A2+1./A3)-A2*A3*F(IJ+1)/(A1*A4*A5)+A1*A3*F(2
1  *IJ+1)/(A2*A4*A6)-A1*A2*F(3*IJ+1)/(A3*A5*A6)
    GO TO 70
110 IF (N-4) 570,120,120
120 B1=X(N)-X(N-3)
    B2=X(N)-X(N-2)
    B3=X(N)-X(N-1)
    B4=X(N-1)-X(N-3)
    B5=X(N-1)-X(N-2)
    B6=X(N-2)-X(N-3)
    L1=K4-IJ
    L2=L1-IJ
    L3=L2-IJ
    W(K4)=-B2*B3*F(L3)/(B6*B4*B1)+B1*B3*F(L2)/(B6*B5*B2)-B1*B2*F(L1)/
1  (B4*B5*B3)+F(K4)*(1./B1+1./B2+1./B3)
    GO TO 80
130 DO 160 I=1,K
    M=(I-1)*IJ+1
    GO TO 170
140 IF (I-1) 150,160,150
150 W(1)=W(1)-BOB*W(M)
    W(K4)=W(K4)-BILL*W(M)
    A(1)=A(1)-BOB*A(I)
    A(N)=A(N)-BILL*A(I)
    C(1)=C(1)-BOB*C(I)
    C(N)=C(N)-BILL*C(I)
160 CONTINUE
    GO TO 550
170 MK=IOP(1)
    GO TO (180,210,260,310,260), MK
180 IF (I-1) 200,190,200
190 A(1)=-1.
    C(1)=0.
    GO TO 340
200 BOB=0.
    GO TO 340
210 IF (I-1) 230,220,230
220 A(1)=-1.
    C(1)=0.
    W(1)=0.
    GO TO 340
230 IF (I-2) 240,240,250
240 BOB=-C1
    GO TO 340
250 BOB=0.
    GO TO 340
260 IF (I-1) 280,270,280
270 A(1)=-(X(2)-X(1))/3.
    C(1)=0.
    W(1)=-C1+(F(IJ+1)-F(1))/(X(2)-X(1))
    GO TO 340
280 IF (I-2) 290,290,300
290 BOB=(X(2)-X(1))/6.
    GO TO 340
300 BOB=0.
    GO TO 340
310 IF (I-1) 330,320,330
320 A(1)=-1.
    C(1)=1.
    W(1)=0.
    GO TO 340
330 BOB=0.
340 ML=ICP(2)
    GO TO (350,380,430,480,430), ML

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350 IF (I-1) 370,360,370
360 A(N)=0.
    C(N)=-1.
    GO TO 140
370 BILL=0.
    GO TO 140
380 IF (I-1) 400,390,400
390 A(N)=0.
    C(N)=-1.
    W(K4)=0.
    GO TO 140
400 IF (I-K) 420,410,420
410 BILL=-C2
    GO TO 140
420 BILL=0.
    GO TO 140
430 IF (I-1) 450,440,450
440 A(N)=0.
    C(N)=(X(N-1)-X(N))/3.
    W(K4)=C2-(F(K4)-F(K1))/(X(N)-X(N-1))
    GO TO 140
450 IF (I-K) 470,460,470
460 BILL=(X(N)-X(N-1))/6.
    GO TO 140
470 BILL=0.
    GO TO 140
480 IF (I-1) 500,490,500
490 A(N)=0.
    C(N)=(X(N-1)+X(1)-X(N)-X(2))/3.
    W(K4)=(F(IJ+1)-F(1))/(X(2)-X(1))-(F(K4)-F(K1))/(X(N)-X(N-1))
    GO TO 140
500 IF (I-2) 520,510,520
510 BILL=(X(2)-X(1))/6.
    GO TO 140
520 IF (I-K) 540,530,540
530 BILL=(X(N)-X(N-1))/6.
    GO TO 140
540 BILL=0.
    GO TO 140
550 CON=A(1)*C(N)-C(1)*A(N)
    D1=-W(1)
    D2=-W(K4)
    W(1)=(D1*C(N)-C(1)*D2)/CON
    W(K4)=(A(1)*D2-D1*A(N))/CON
    DO 560 I=2,K
    M=(I-1)*IJ+1
560 W(M)=W(M)+A(I)*W(1)+C(I)*W(K4)
    GO TO 580
570 CALL LABRT (1,COMM,1)
580 RETURN
END
SUBROUTINE SPL1D2 (N,X,F,W,IJ,Y,TAB)
WHERE N= NUMBER OF POINTS IN THE INTERPOLATION
      X= ORIGIN OF TABLE OF THE INDEPENDENT VARIABLE
      F= ORIGIN OF TABLE OF THE DEPENDENT VARIABLE
      W= ORIGIN OF TABLE OF SECOND DERIVATIVES AS CALCULATED BY
        SPL1D1
      IJ= SPACING IN THE TABLES F AND W
      Y= THE POINT AT WHICH INTERPOLATION IS DESIRED
      TAB= AN ARRAY OF DIMENSION 3 WHICH CONTAINS THE FUNCTION
           VALUE, FIRST DERIVATIVE, AND SECOND DERIVATIVE AT Y
DIMENSION X(3), F(3), W(3), TAB(3)
LOCATE Y IN THE X TABLE
IF (Y-X(1)) 10,10,20
10 I=1
   GO TO 50
20 IF (Y-X(N)) 40,30,30
30 I=N-1

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*
*   IN ORDER TO DO A BINARY SEARCH, X MUST BE IN AN INTERVAL
*   SINCE WE SAVED VALUE OF ILO, WE MUST FORCE INTERVAL WHERE
*   XT(ILO) LT X LT XT(IHI), BY MOVING ILO AND IHI UP OR DOWN XT.
*
SEARCH  DATA  0
        IFECQ  *F,2          CALLED BY FTN
        SX6    A0
        SA6    TEMP
        SB1    1             B1=1
        SA3    X1            X3=X
        SA1    A1+B1
        SB2    X1
        SB2    B2-B1          B2 NOW REFERENCES XT FOR INDEXES
        SA2    B2+B1          X1=XT(1)
        SA1    A1+B1
        SA4    X1             X4=N
        SA1    A1+B1
        SB4    X1             B4=ADDR(NDX)
        SA1    A1+B1
        SA0    X1             A0 =ADDR(MFLAG)
        SB5    B1
        SA5    ILO
        ELSE
        SA3    B1             CALLED BY FUN OR RUN
        SA4    B3             X3 CONTAINS X
        SA0    B5             X4 CONTAINS N
        SB1    1             STORE ADDRESS OF MFLAG
        SA5    ILO            KEEP VALUE OF 1
        SB2    B2-B1          PICK UP BEGINNING VALUE OF ILO
        SB5    B1             B2 NOW REFERENCES XT FOR INDEXES
        SA2    B2+B1          ISTEP = 1
        ENDIF                X1 = XT(1)
        SB3    X4             SET N
        SA4    B2+X4          X4 = XT(N)
        SX7    B1             1
        SB7    X5+B1          IHI = ILO+1
        SB6    X5             SET ILO
        SA7    A5             STORE ILO = 1
        SA1    B2+B7          X1 = XT(IHI)
        IX4    X4-X2          XT(N) - XT(1)
        SA2    B2+B6          X2 = XT(ILO)
*
*   IF XT IS MONOTONIC DECREASING BRANCH TO SWITCH VALUES
*
        NG      X4,SWIT      YES, XT(N) LT XT(1) SWITCH
*
*   CHECK STARTING POINTS TO SEE IF X IS IN AN INTERVAL OF XT(ILO)
*   AND XT(IHI). MUST BE TO BEGIN ACTUAL BINARY SECTION.
*
        GE      B7,B3,IHI2BIG  OPPS IHI IS GT N
*
*   DECR
        IX7     X3-X1          X-XT(IHI)
        IX6     X3-X2          X-XT(ILO)
        ZR      X7,DONE07
        PL      X7,BIGXW       X GT XT(IHI) MUST BRING INTERVAL UP
        ZR      X6,DONE0       X = XT(ILO)
        PL      X6,DONE1       XT(ILO) LT X LT XT(ILO+1) SO DONE
*
*   X IS LESS THAN STARTING VALUE OF ILO THEREFORE MUST BRING
*   INTERVAL DOWN TO DO BINARY SEARCH. MOVE INTERVAL DOWN, DOUBLING
*   STEP SIZE EACH TIME UNTIL XT(ILO) LT X LT XT(IHI).
*
        SMLXW   SB6           B6-B5          DECREASE ILO TO GET THIS STEP
        LT      B6,B1,ILO2SML ILO IS ZERO OR LESS NOT VALID
        SA2     A2-B5          GET NEXT VLAUE
        SB7     B6+B5          IHI = ILO
        SB5     B5+B5          ISTEP = 2*ISTEP
        GT      B6,B3,ILO2BIG
        SX4     B3             X4 = N
        SX7     B6-B5          NEXT DECREASING ILO

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GT      B5,B6,ILO2SML      NEXT INCREASING WILL BE OUT
IX7     X4-X7              N - NEXT STEP(DECREASING)
IX4     X3-X2              X-XT(ILO)
NG      X7,ILO2BIG
NG      X4,SMLXW           INTERVAL NOT FOUND MUST REPEAT
EQ      BSRCH              INTERVAL FORMED PERFORM BINARY.
*
*      XT WAS MONOTONIC DECREASING
*
SWIT     SA1      A2          SWITCH VALUES IN X2 AND X1
        SB7      B6          IHI = ILO
        SB6      B6+B1       ILO = IHI
        SB5      -B5         ISTEP = -1
        SA2      A2+B1       SET X2 = XT(ILO)
        LE       B6,B3,DECR   IF STILL IN RANGE RETURN TO NORMAL CO
        SB6      B1          SET IHI = 1
*
*      ILO2BIG
        PL       X4,BSRCH     INTERVAL FOUND TRY BINARY
        SA1      B2+B1       X1 = XT(1)
        SB7      B6
        SA2      B2+B3       X2 = XT(N)
        SB6      B3          SET ILO TO N
*
        SX7      B1          1
        SX6      B1+B1       2
        SA7      B4          STORE NDX=1
        SA6      A0          STORE MFLAG = 2
        SA7      A5          STORE ILO = 1
        SX7      B3          ILO = N
*
        IX6      X1-X3       XT(1)-X
        IX4      X3-X2       X-XT(N)
        IFEQ     *F,2         CALLED BY FTN
        NG      X6,SEARCH1
        ELSE
        NG      X6,SEARCH     X NOT IN TABLE ALL DONE
        ENDIF
        PL      X4,BSRCH     X IS BETWEEN XT(ILO) AND XT(IHI)
*
        SA7      B4          STORE NDX = N
        SA7      A5
        IFEQ     *F,2         CALLED BY FTN
        EQ      SEARCH1
        ELSE
        EQ      SEARCH        ALL DONE
        ENDIF
*
        ILO2SML
        IX4      X3-X2       XT(ILO)-X
        SA2      B2+B1       X1 = XT(1)
        SX7      B1          1
        SX6      B1+B1       2
        PL      X4,BSRCH     FOUND AN INTERVAL TRY BINARY
        SB6      B1          ILO = 1
*
        SA7      A5          STORE ILO = 1
        SA6      A0          STORE MFLAG = 2
*
        IX4      X3-X2       X-XT(1)
        SA7      B4          STORE NDX = 1
        IFEQ     *F,2         CALLED BY FTN
        NG      X4,SEARCH1
        ELSE
        NG      X4,SEARCH     X IS LT XT(1) ALL DONE
        ENDIF
        EQ      BSRCH        INTERVAL SET TRY BINARY
*
*      IHI2BIG
        SA1      B2+B3       X1 = X(N)
        SB6      B3-B1       ILO = N-1
        SA2      A1-B1       XI = XT(IHI-ISTEP)
*

```

```

SX7      B1              1
SX6      B1+B1          2
SA7      A5              STORE ILO = 1
SA6      A0              STORE MFLAG = 2
SA7      B4              STORE NDX = 1
*
IX4      X1-X3           X-XT(N)
SB5      B3              PLACE ANSWER IN B5
IX6      X3-X2           X-XT(N-1)
IFEQ     *F,2            CALLED BY FTM
LE       B3,B1,SEARCH1
ELSE
LE       B3,B1,SEARCH    XT NOT AN ARRAY    ALL DONE
ENDIF
ZR       X4,DONE00       HAVE ANSWER BRANCH TO RETURN VALUES
SB5      B1              RESTORE ISTEP
NG       X4,IHIGTN       OPPS OUT RETURN RIGHT VALUES
ZR       X6,DONE0        FOUND X EXACT
PL       X6,DONE1        X BETWEEN XT(N-1) AND XT(N)
EQ       SMLXW           STILL MUST FORM INTERVAL
*
X WAS GREATER THAN BEGINNING IHI  NEED TO MOVE INTERVAL DOWN
XT TO DO BINARY SEARCH.  MOVE INTERVAL, DOUBLING STEP SIZE
AT EACH STEP UNTIL XT(ILO) LT X LT XT(IHI)
BIGXW    SA1      A1+B5      X1 = XT(IHI)
          SB6      B7        ILO = IHI
          SB7      B7+B5     IHI = IHI+ISTEP
          SB5      B5+B5     ISTEP = I*ISTEP
          NO
          SX7      B7+B5     NEXT INCREASING VALUE
          SX6      B3        KEEP VALUE OF N
          ZR       X7,IHILT1  NEXT DECREASING VALUE IS OUTP
          NG       X7,IHILT1  NEXT DECREASING VALUE IS OUT
          IX7      X6-X7     N - NEXT STEP(INCREASING)
          IX4      X1-X3     X-XT(IHI)
          NG       X7,IHIGTN  NEXT STEP OUT OF INTERVAL
          NG       X4,BIGXW   STILL DO NOT HAVE INTERVAL  REPEAT
          ZR       X4,DONE07
*
          HAVE INTERVAL MUST SET UP A MID POINT FOR BINARY
BSRCH    ZR       X4,DONE0    FOUND ANSWER EXACTLY
          SX6      B6+B7     IHI + ILO
          SB5      B7        MID = IHI
          AX6      1         NEXT MID POINT MAYBE
          SA2      B2+X6     X2 = XT(MID)
*
          FINALLY  THIS IS ACTUAL BINARY SEARCH SECTION
BSRCH1   SB7      B5         IHI = MID
          SB5      X6        MID POINT
          SX0      B6+X6     X0 = ILO+MID
          SX1      B7+X6     X1 = IHI+MID
          AX6      B1,X0     MID 1 IF X BETWEEN XT(ILO) AND XT(MID)
          AX1      1         MID 2 IF X BETWEEN XT(IHI) AND XT(MID)
          IX0      X2-X3     XT(MID)-X
          IX5      X1-X6     IHI - ILO
          SA2      B2+X6     X2 = XT(MID 1)
          ZR       X5,DONE    MID MATCHES BOUNDRY RETURN ANSWERS
          SA4      B2+X1     X4 = XT(MID 2)
*
          LOOP     ZR       X0,DONE00  X MATCHES XT(MID)  RETURN VALUE
          PL       X0,BSRCH1  X BETWEEN XT(MID) AND XT(IHI)
*
          SB6      B5         ILO = MID
          SB5      X1         NEW MID POINT
          SX6      X1+B6     X6 = MID + ILO
          SX1      X1+B7     X1 = MID + IHI
          AX6      1         MID 1  X BETWEEN XT(MID) AND XT(ILO)
          AX1      1         MID 2  X BETWEEN XT(MID) AND XT(IHI)

```

```

IX0      X4-X3      XT(MID)-X
IX5      X1-X6      IHI-ILO
SA2      B2+X6      X2 = XT(MID 1)
SA4      B2+X1      X4 = XT(MID 2)
NZ       X5,LOOP    HAVE NOT FOUND VALUE TRY AGAIN

*
*      RIGHT ANSWER FOUND IN INTERVAL  XT(X6) LT X LT XT(X6+1)
*
DONE     ZR      X0,DONE00      FOUND RIGHT ANSWER EXACTLY
        SX7     B1
        SA6     B4              1
        SA7     A0              STORE ANSWER IN NDX
        SA6     A5              STORE 1 IN MFLAG
        IFEQ    *F,2            STORE ANSWER IN ILO
        EQ      SEARCH1        CALLED BY FTN
        ELSE
        EQ      SEARCH          ALL DONE
        ENDIF

*
*      RIGHT ANSWER FOUND EXACTLY
*
DONE0    SX6     B6              ANSWER IN B6
        MX7     0
        SA6     B4              STORE ANSWER IN NDX
        SA7     A0              STORE 0 IN MFLAG
        SA6     A5              STORE ANSWER IN ILO
        IFEQ    *F,2            CALLED BY FTN
        EQ      SEARCH1
        ELSE
        EQ      SEARCH          ALL DONE
        ENDIF

DONE00   SX6     B5              ANSWER IN B5
        MX7     0              SET TO 0
        SA6     B4              NDX = ANSWER
        SA7     A0              MFLAG = 0
        SA6     A5              ILO = ANSWER
        IFEQ    *F,2            CALLED BY FTN
        EQ      SEARCH1
        ELSE
        EQ      SEARCH          ALL DONE
        ENDIF

*
*
DONE07   SX6     B7
        MX7     0
        SA6     B4
        SA7     A0
        SA6     A5
        IFEQ    *F,2            CALLED BY FTN
        EQ      SEARCH1
        ELSE
        EQ      SEARCH
        ENDIF

IHIGTN   SA1     B2+B3          X1 = XT(N)
        ZR      X4,DONE07      FOUND INTERVAL
        PL      X4,BSRCH       ILO = N
        SB6     B3

*
        SX6     B3              N
        SX7     B1+B1          2
        SA6     A5              STORE ILO = N
        SA7     A0              STORE MFLAG = 2
        IX4     X1-X3          XT(N)-X
        SA6     B4              STORE NDX = N

*
        IFEQ    *F,2            CALLED BY FTN
        NG      X4,SEARCH1
        ELSE
        NG      X4,SEARCH       X OUT OF RANGE  ALL DONE
        ENDIF
        LT      B5.B0,BSRCH     MUST KEEP POINTERS RIGHT

```

```

      ZR      X4,DONE0      FOUND RIGHT ANSWER
      SB6      B7      OR WONT ZERO IN ON RIGHT
      SB7      B3      SECTION
      EQ      BSRCH      FOUND INTERVAL USE EINARY
*
*
IHILT1  IX4      X1-X3      X - XT(IHI)
      SA2      B2+B1      X4 = XT(1)
      ZR      X4,DONE07
      PL      X4,BSRCH      FOUND INTERVAL
      SB6      1      ILO = 1
*
      SX7      B1      1
      SX6      B1+B1      2
      SA7      A5      STORE ILO = 1
      SA6      A0      STORE MFLAG = 2
*
      IX4      X2-X3      XT(1)-X
      SA7      B4      STORE NDX = 1
      IFEQ      *F,2      CALLED BY FTN
      NG      X4,SEARCH1
      ELSE
      NG      X4,SEARCH      X OUT OF RANGE ALL DONE
      ENDIF
      GT      B5,B0,BSRCH      MONOTONIC DECREASING INTERVAL
      ZR      X4,DONE0      FOUND RIGHT ANSWER
      SB6      B7      INTERVAL MUST BE BACKWARDS
      SB7      B1      IHI = 1
      EQ      BSRCH      FOUND INTERVAL TRY BINARY
      IFEQ      *F,2      CALLED BY FTN
TEMP    BSS      1
      ENDIF
      END
C      THE FOLLOWING SUBROUTINE IS A REPLACEMENT FOR THE
C      ROUTINE SEARCH FOR USE WITH MACHINES THAT DO
C      NOT COMPILE COMPASS.
C      SUBROUTINE SEARCH(X,XT,N,NDX,MFLAG)
C      SEARCH FINDS A GIVEN VALUE X IN A MONOTONIC SERIES
C      DIMENSION XT(1)
C      IF (XT(N)-XT(1)) 140,10,20
C 10 PRINT 260
C      CALL EXIT
C 20 IF (XT(N)-X) 40,30,50
C 30 NDX=N
C      MFLAG=0
C      RETURN
C 40 NDX=N
C      MFLAG=2
C      RETURN
C 50 IF (XT(1)-X) 80,60,70
C 60 NDX=1
C      MFLAG=0
C      RETURN
C 70 NDX=1
C      MFLAG=2
C      RETURN
C 80 NDX=N/2.0+0.5
C      M0=1
C      M2=N
C 90 IF (XT(NDX)-X) 110,100,130
C 100 MFLAG=0
C      RETURN
C 110 M0=NDX
C      NDX=(M2-M0)/2.0+M0
C      IF (NDX-M0) 90,120,90
C 120 MFLAG=1
C      RETURN
C 130 M2=NDX
C      NDX=(M2-M0)/2.0+M0
C      IF (NDX-M0) 90,120,90
C 140 IF (X-XT(1)) 170,150,160

```



```

C 150 NDX=1
C      MFLAG=0
C      RETURN
C 160 NDX=1
C      MFLAG=2
C      RETURN
C 170 IF (X-XT(N)) 190,180,200
C 180 NDX=N
C      MFLAG=0
C      RETURN
C 190 NDX=N
C      MFLAG=2
C      RETURN
C 200 NDX=N/2.0+0.5
C      M0=1
C      M2=N
C 210 IF (XT(NDX)-X) 230,220,250
C 220 MFLAG=0
C      RETURN
C 230 M2=NDX
C      NDX=(M2-M0)/2.0+M0
C      IF (NDX-M0) 210,240,210
C 240 MFLAG=1
C      RETURN
C 250 M0=NDX
C      NDX=(M2-M0)/2.0+M0
C      IF (NDX-M0) 210,240,210
C 260 FORMAT (5X,*YOUR ARRAY IS NOT MONOTONIC*)
C      END
C      SUBROUTINE SGECO(A,LDA,N,IPVT,RCOND,Z)
C      INTEGER LDA,N,IPVT(1)
C      REAL A(LDA,1),Z(1)
C      REAL RCOND
C
C      SGECO FACTORS A REAL MATRIX BY GAUSSIAN ELIMINATION
C      AND ESTIMATES THE CONDITION OF THE MATRIX.
C
C      IF RCOND IS NOT NEEDED, SGEFA IS SLIGHTLY FASTER.
C      TO SOLVE  $A \cdot X = B$ , FOLLOW SGECO BY SGESL.
C      TO COMPUTE  $INVERSE(A) \cdot C$ , FOLLOW SGECO BY SGESL.
C      TO COMPUTE  $DETERMINANT(A)$ , FOLLOW SGECO BY SGEDI.
C      TO COMPUTE  $INVERSE(A)$ , FOLLOW SGECO BY SGEDI.
C
C      ON ENTRY
C
C      A      REAL(LDA, N)
C              THE MATRIX TO BE FACTORED.
C
C      LDA    INTEGER
C              THE LEADING DIMENSION OF THE ARRAY A .
C
C      N      INTEGER
C              THE ORDER OF THE MATRIX A .
C
C      ON RETURN
C
C      A      AN UPPER TRIANGULAR MATRIX AND THE MULTIPLIERS
C              WHICH WERE USED TO OBTAIN IT.
C              THE FACTORIZATION CAN BE WRITTEN  $A = L \cdot U$  WHERE
C              L IS A PRODUCT OF PERMUTATION AND UNIT LOWER
C              TRIANGULAR MATRICES AND U IS UPPER TRIANGULAR.
C
C      IPVT   INTEGER(N)
C              AN INTEGER VECTOR OF PIVOT INDICES.
C
C      RCOND  REAL
C              AN ESTIMATE OF THE RECIPROCAL CONDITION OF A .
C              FOR THE SYSTEM  $A \cdot X = B$ , RELATIVE PERTURBATIONS
C              IN A AND B OF SIZE EPSILON MAY CAUSE
C              RELATIVE PERTURBATIONS IN X OF SIZE EPSILON/RCOND .

```

IF RCOND IS SO SMALL THAT THE LOGICAL EXPRESSION
 $1.0 + RCOND \text{ .EQ. } 1.0$
 IS TRUE, THEN A MAY BE SINGULAR TO WORKING
 PRECISION. IN PARTICULAR, RCOND IS ZERO IF
 EXACT SINGULARITY IS DETECTED OR THE ESTIMATE
 UNDERFLOWS.

Z REAL(N)
 A WORK VECTOR WHOSE CONTENTS ARE USUALLY UNIMPORTANT.
 IF A IS CLOSE TO A SINGULAR MATRIX, THEN Z IS
 AN APPROXIMATE NULL VECTOR IN THE SENSE THAT
 $\text{NORM}(A*Z) = \text{RCOND} * \text{NORM}(A) * \text{NORM}(Z)$.

LINPACK. THIS VERSION DATED 07/14/77 .
 CLEVE MOLER, UNIVERSITY OF NEW MEXICO, ARGONNE NATIONAL LABS.

SUBROUTINES AND FUNCTIONS

LINPACK SGEFA
 BLAS SAXPY,SDOT,SSCAL,SASUM
 FORTRAN ABS,AMAX1,SIGN

INTERNAL VARIABLES

REAL SDOT,EK,T,WK,WKM
 REAL ANORM,S,SASUM,SM,YNORM
 INTEGER INFO,J,K,KB,KP1,L

REAL SIGN

COMPUTE 1-NORM OF A

ANORM = 0.0EO
 DO 10 J = 1, N
 ANORM = AMAX1(ANORM,SASUM(N,A(1,J),1))
 10 CONTINUE

FACTOR

CALL SGEFA(A,LDA,N,IPVT,INFO)

RCOND = 1/(NORM(A)*(ESTIMATE OF NORM(INVERSE(A)))) .
 ESTIMATE = NORM(Z)/NORM(Y) WHERE $A*Z = Y$ AND $\text{TRANS}(A)*Y = E$.
 TRANS(A) IS THE TRANSPOSE OF A . THE COMPONENTS OF E ARE
 CHOSEN TO CAUSE MAXIMUM LOCAL GROWTH IN THE ELEMENTS OF W WHERE
 $\text{TRANS}(U)*W = E$. THE VECTORS ARE FREQUENTLY RESCALED TO AVOID
 OVERFLOW.

SOLVE $\text{TRANS}(U)*W = E$

EK = 1.0EO
 DO 20 J = 1, N
 Z(J) = 0.0EO
 20 CONTINUE
 DO 100 K = 1, N
 IF (Z(K) .NE. 0.0EO) EK = SIGN(EK,-Z(K))
 IF (ABS(EK-Z(K)) .LE. ABS(A(K,K))) GO TO 30
 S = ABS(A(K,K))/ABS(EK-Z(K))
 CALL SSCAL(N,S,Z,1)
 EK = S*EK
 30 CONTINUE
 WK = EK - Z(K)
 WKM = -EK - Z(K)
 S = ABS(WK)
 SM = ABS(WKM)
 IF (A(K,K) .EQ. 0.0EO) GO TO 40
 WK = WK/A(K,K)
 WKM = WKM/A(K,K)
 GO TO 50
 40 CONTINUE
 WK = 1.0EO
 WKM = 1.0EO

```

50    CONTINUE
      KP1 = K + 1
      IF (KP1 .GT. N) GO TO 90
      DO 60 J = KP1, N
        SM = SM + ABS(Z(J)+WKM*A(K,J))
        Z(J) = Z(J) + WK*A(K,J)
        S = S + ABS(Z(J))
60    CONTINUE
      IF (S .GE. SM) GO TO 80
      T = WKM - WK
      WK = WKM
      DO 70 J = KP1, N
        Z(J) = Z(J) + T*A(K,J)
70    CONTINUE
80    CONTINUE
90    CONTINUE
      Z(K) = WK
100   CONTINUE
      S = 1.0EO/SASUM(N,Z,1)
      CALL SSCAL(N,S,Z,1)
C
C
C    SOLVE TRANS(L)*Y = V
      DO 120 KB = 1, N
        K = N + 1 - KB
        IF (K .LT. N) Z(K) = Z(K) + SDOT(N-K,A(K+1,K),1,Z(K+1),1)
        IF (ABS(Z(K)) .LE. 1.0EO) GO TO 110
        S = 1.0EO/ABS(Z(K))
        CALL SSCAL(N,S,Z,1)
110   CONTINUE
        L = IPVT(K)
        T = Z(L)
        Z(L) = Z(K)
        Z(K) = T
120   CONTINUE
      S = 1.0EO/SASUM(N,Z,1)
      CALL SSCAL(N,S,Z,1)
C
C
C    YNORM = 1.0EO
C
C    SOLVE L*V = Y
      DO 140 K = 1, N
        L = IPVT(K)
        T = Z(L)
        Z(L) = Z(K)
        Z(K) = T
        IF (K .LT. N) CALL SAXPY(N-K,T,A(K+1,K),1,Z(K+1),1)
        IF (ABS(Z(K)) .LE. 1.0EO) GO TO 130
        S = 1.0EO/ABS(Z(K))
        CALL SSCAL(N,S,Z,1)
        YNORM = S*YNORM
130   CONTINUE
140   CONTINUE
      S = 1.0EO/SASUM(N,Z,1)
      CALL SSCAL(N,S,Z,1)
      YNORM = S*YNORM
C
C
C    SOLVE U*Z = V
      DO 160 KB = 1, N
        K = N + 1 - KB
        IF (ABS(Z(K)) .LE. ABS(A(K,K))) GO TO 150
        S = ABS(A(K,K))/ABS(Z(K))
        CALL SSCAL(N,S,Z,1)
        YNORM = S*YNORM
150   CONTINUE
        IF (A(K,K) .NE. 0.0EO) Z(K) = Z(K)/A(K,K)
        IF (A(K,K) .EQ. 0.0EO) Z(K) = 1.0EO
        T = -Z(K)
        CALL SAXPY(K-1,T,A(1,K),1,Z(1),1)
160   CONTINUE

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```

C      MAKE ZNORM = 1.0
      S = 1.0EO/SASUM(N,Z,1)
      CALL SSCAL(N,S,Z,1)
      YNORM = S*YNORM
C
      IF (ANORM .NE. 0.0EO) RCOND = YNORM/ANORM
      IF (ANORM .EQ. 0.0EO) RCOND = 0.0EO
      RETURN
      END
      SUBROUTINE SGEFA(A,LDA,N,IPVT,INFO)
      INTEGER LDA,N,IPVT(1),INFO
      REAL A(LDA,1)

      SGEFA FACTORS A REAL MATRIX BY GAUSSIAN ELIMINATION.

      SGEFA IS USUALLY CALLED BY SGECO, BUT IT CAN BE CALLED
      DIRECTLY WITH A SAVING IN TIME IF RCOND IS NOT NEEDED.
      (TIME FOR SGECO) = (1 + 9/N)*(TIME FOR SGEFA) .

      ON ENTRY

      A      REAL(LDA, N)
              THE MATRIX TO BE FACTORED.

      LDA    INTEGER
              THE LEADING DIMENSION OF THE ARRAY  A .

      N      INTEGER
              THE ORDER OF THE MATRIX  A .

      ON RETURN

      A      AN UPPER TRIANGULAR MATRIX AND THE MULTIPLIERS
              WHICH WERE USED TO OBTAIN IT.
              THE FACTORIZATION CAN BE WRITTEN  $A = L*U$  WHERE
              L IS A PRODUCT OF PERMUTATION AND UNIT LOWER
              TRIANGULAR MATRICES AND U IS UPPER TRIANGULAR.

      IPVT   INTEGER(N)
              AN INTEGER VECTOR OF PIVOT INDICES.

      INFO   INTEGER
              = 0  NORMAL VALUE.
              = K  IF  $U(K,K) \leq 0.0$  . THIS IS NOT AN ERROR
                  CONDITION FOR THIS SUBROUTINE, BUT IT DOES
                  INDICATE THAT SGESL OR SGEDI WILL DIVIDE BY ZERO
                  IF CALLED. USE RCOND IN SGECO FOR A RELIABLE
                  INDICATION OF SINGULARITY.

      LINPACK. THIS VERSION DATED 07/14/77 .
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      SUBROUTINES AND FUNCTIONS

      BLAS SAXPY,SSCAL,ISAMAX

      INTERNAL VARIABLES

      REAL T
      INTEGER ISAMAX,J,K,KP1,L,NM1

      GAUSSIAN ELIMINATION WITH PARTIAL PIVOTING

      INFO = 0
      NM1 = N - 1
      IF (NM1 .LT. 1) GO TO 70
      DO 60 K = 1, NM1
        KP1 = K + 1
        FIND L = PIVOT INDEX

```

```

C      L = ISAMAX(N-K+1,A(K,K),1) + K - 1
C      IPVT(K) = L
C      ZERO PIVOT IMPLIES THIS COLUMN ALREADY TRIANGULARIZED
C      IF (A(L,K) .EQ. 0.0EO) GO TO 40
C      INTERCHANGE IF NECESSARY
C      IF (L .EQ. K) GO TO 10
C      T = A(L,K)
C      A(L,K) = A(K,K)
C      A(K,K) = T
10     CONTINUE
C      COMPUTE MULTIPLIERS
C      T = -1.0EO/A(K,K)
C      CALL SSCAL(N-K,T,A(K+1,K),1)
C      ROW ELIMINATION WITH COLUMN INDEXING
C      DO 30 J = KP1, N
C      T = A(L,J)
C      IF (L .EQ. K) GO TO 20
C      A(L,J) = A(K,J)
C      A(K,J) = T
20     CONTINUE
C      CALL SAXPY(N-K,T,A(K+1,K),1,A(K+1,J),1)
30     CONTINUE
C      GO TO 50
40     CONTINUE
C      INFO = K
50     CONTINUE
60     CONTINUE
70     CONTINUE
C      IPVT(N) = N
C      IF (A(N,N) .EQ. 0.0EO) INFO = N
C      RETURN
C      END
C      SUBROUTINE SGEDI(A,LDA,N,IPVT,DET,WORK,JOB)
C      INTEGER LDA,N,IPVT(1),JOB
C      REAL A(LDA,1),DET(1),WORK(1)
C
C      SGEDI COMPUTES THE DETERMINANT AND INVERSE OF A MATRIX
C      USING THE FACTORS COMPUTED BY SGECO OR SGEFA.
C
C      ON ENTRY
C
C      A      REAL(LDA, N)
C             THE OUTPUT FROM SGECO OR SGEFA.
C
C      LDA    INTEGER
C             THE LEADING DIMENSION OF THE ARRAY A .
C
C      N      INTEGER
C             THE ORDER OF THE MATRIX A .
C
C      IPVT   INTEGER(N)
C             THE PIVOT VECTOR FROM SGECO OR SGEFA.
C
C      WORK   REAL(N)
C             WORK VECTOR.  CONTENTS DESTROYED.
C
C      JOB    INTEGER
C             = 11  BOTH DETERMINANT AND INVERSE.
C             = 01  INVERSE ONLY.
C             = 10  DETERMINANT ONLY.

```

```
C
C
C      ON RETURN
C
C      A          INVERSE OF ORIGINAL MATRIX IF REQUESTED.
C                  OTHERWISE UNCHANGED.
C
C      DET        REAL(2)
C                  DETERMINANT OF ORIGINAL MATRIX IF REQUESTED.
C                  OTHERWISE NOT REFERENCED.
C                  DETERMINANT = DET(1) * 10.0**DET(2)
C                  WITH 1.0 .LE. ABS(DET(1)) .LT. 10.0
C                  OR DET(1) .EQ. 0.0 .
C
C      ERROR CONDITION
C
C      A DIVISION BY ZERO WILL OCCUR IF THE INPUT FACTOR CONTAINS
C      A ZERO ON THE DIAGONAL AND THE INVERSE IS REQUESTED.
C      IT WILL NOT OCCUR IF THE SUBROUTINES ARE CALLED CORRECTLY
C      AND IF SGECO HAS SET RCOND .GT. 0.0 OR SGEFA HAS SET
C      INFO .EQ. 0 .
C
C      LINPACK. THIS VERSION DATED 07/14/77 .
C      CLEVE MOLER, UNIVERSITY OF NEW MEXICO, ARGONNE NATIONAL LABS.
C
C      SUBROUTINES AND FUNCTIONS
C
C      BLAS SAXPY,SSCAL,SSWAP
C      FORTRAN ABS,MOD
C
C      INTERNAL VARIABLES
C
C      REAL T
C      REAL TEN
C      INTEGER I,J,K,KB,KP1,L,NM1
C
C      COMPUTE DETERMINANT
C
C      IF (JOB/10 .EQ. 0) GO TO 70
C         DET(1) = 1.0EO
C         DET(2) = 0.0EO
C         TEN = 10.0EO
C         DO 50 I = 1, N
C            IF (IPVT(I) .NE. I) DET(1) = -DET(1)
C            DET(1) = A(I,I)*DET(1)
C            ...EXIT
C         IF (DET(1) .EQ. 0.0EO) GO TO 60
C10       IF (ABS(DET(1))) .GE. 1.0EO) GO TO 20
C           DET(1) = TEN*DET(1)
C           DET(2) = DET(2) + 1.0EO
C           GO TO 10
C20       CONTINUE
C30       IF (ABS(DET(1))) .LT. TEN) GO TO 40
C           DET(1) = DET(1)/TEN
C           DET(2) = DET(2) + 1.0EO
C           GO TO 30
C40       CONTINUE
C50       CONTINUE
C60       CONTINUE
C70     CONTINUE
C
C      COMPUTE INVERSE(U)
C
C      IF (MOD(JOB,10) .EQ. 0) GO TO 150
C      DO 100 K = 1, N
C         A(K,K) = 1.0EO/A(K,K)
C         T = -A(K,K)
C         CALL SSCAL(K-1,T,A(1,K),1)
C         KP1 = K + 1
C         IF (N .LT. KP1) GO TO 90
C         DO 80 J = KP1, N
C            T = A(K,J)
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      A(K,J) = 0.0E0
      CALL SAXPY(K,T,A(1,K),1,A(1,J),1)
80      CONTINUE
90      CONTINUE
100     CONTINUE
C
C      FORM INVERSE(U)*INVERSE(L)
C
      NM1 = N - 1
      IF (NM1 .LT. 1) GO TO 140
      DO 130 KB = 1, NM1
        K = N - KB
        KP1 = K + 1
        DO 110 I = KP1, N
          WORK(I) = A(I,K)
          A(I,K) = 0.0E0
110      CONTINUE
        DO 120 J = KP1, N
          T = WORK(J)
          CALL SAXPY(N,T,A(1,J),1,A(1,K),1)
120      CONTINUE
        L = IPVT(K)
        IF (L .NE. K) CALL SSWAP(N,A(1,K),1,A(1,L),1)
130      CONTINUE
140      CONTINUE
150      CONTINUE
      RETURN
      END
      INTEGER FUNCTION ISAMAX (N,SX,INCX)
C
C      FINDS THE INDEX OF ELEMENT HAVING MAX. ABSOLUTE VALUE.
C      JACK DONGARRA, LINPACK, 3/11/78.
C
      REAL SX(1), SMAX
      INTEGER I, INCX, IX, N
C
      ISAMAX=0
      IF (N.LT.1) RETURN
      ISAMAX=1
      IF (N.EQ.1) RETURN
      IF (INCX.EQ.1) GO TO 30
C
C      CODE FOR INCREMENT NOT EQUAL TO 1
C
      IX=1
      SMAX=ABS(SX(1))
      IX=IX+INCX
      DO 20 I=2,N
        IF (ABS(SX(IX)).LE.SMAX) GO TO 10
        ISAMAX=I
        SMAX=ABS(SX(IX))
10      IX=IX+INCX
20      CONTINUE
      RETURN
C
C      CODE FOR INCREMENT EQUAL TO 1
C
30      SMAX=ABS(SX(1))
      DO 40 I=2,N
        IF (ABS(SX(I)).LE.SMAX) GO TO 40
        ISAMAX=I
        SMAX=ABS(SX(I))
40      CONTINUE
      RETURN
      END
      REAL FUNCTION SASUM (N,SX,INCX)
C
C      TAKES THE SUM OF THE ABSOLUTE VALUES.
C      USES UNROLLED LOOPS FOR INCREMENT EQUAL TO ONE.
C      JACK DONGARRA, LINPACK, 3/11/78.
C

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REAL SX(1), STEMP
INTEGER I, INCX, M, MP1, N, NINCX
C
SASUM=0.0E0
STEMP=0.0E0
IF (N.LE.0) RETURN
IF (INCX.EQ.1) GO TO 20
C
C
C      CODE FOR INCREMENT NOT EQUAL TO 1
C
NINCX=N*INCX
DO 10 I=1,NINCX,INCX
STEMP=STEMP+ABS(SX(I))
10 CONTINUE
SASUM=STEMP
RETURN
C
C
C      CODE FOR INCREMENT EQUAL TO 1
C
C
C      CLEAN-UP LOOP
C
20 M=MOD(N,6)
IF (M.EQ.0) GO TO 40
DO 30 I=1,M
STEMP=STEMP+ABS(SX(I))
30 CONTINUE
IF (N.LT.6) GO TO 60
40 MP1=M+1
DO 50 I=MP1,N,6
STEMP=STEMP+ABS(SX(I))+ABS(SX(I+1))+ABS(SX(I+2))+ABS(SX(I+3))+ABS
1 (SX(I+4))+ABS(SX(I+5))
50 CONTINUE
60 SASUM=STEMP
RETURN
END
SUBROUTINE SAXPY (N,SA,SX,INCX,SY,INCY)
C
C      CONSTANT TIMES A VECTOR PLUS A VECTOR.
C      USES UNROLLED LOOP FOR INCREMENTS EQUAL TO ONE.
C      JACK DONGARRA, LINPACK, 3/11/78.
C
REAL SX(1), SY(1), SA
INTEGER I, INCX, INCY, IX, IY, M, MP1, N
C
IF (N.LE.0) RETURN
IF (SA.EQ.0.0) RETURN
IF (INCX.EQ.1.AND.INCY.EQ.1) GO TO 20
C
C
C      CODE FOR UNEQUAL INCREMENTS OR EQUAL INCREMENTS
C      NOT EQUAL TO 1
C
IX=1
IY=1
IF (INCX.LT.0) IX=(-N+1)*INCX+1
IF (INCY.LT.0) IY=(-N+1)*INCY+1
DO 10 I=1,N
SY(IY)=SY(IY)+SA*SX(IX)
IX=IX+INCX
IY=IY+INCY
10 CONTINUE
RETURN
C
C
C      CODE FOR BOTH INCREMENTS EQUAL TO 1
C
C
C      CLEAN-UP LOOP
C
20 M=MOD(N,4)
IF (M.EQ.0) GO TO 40
DO 30 I=1,M
SY(I)=SY(I)+SA*SX(I)
30 CONTINUE

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      IF (N.LT.4) RETURN
40  MP1=M+1
      DO 50 I=MP1,N,4
      SY(I)=SY(I)+SA*SX(I)
      SY(I+1)=SY(I+1)+SA*SX(I+1)
      SY(I+2)=SY(I+2)+SA*SX(I+2)
      SY(I+3)=SY(I+3)+SA*SX(I+3)
50  CONTINUE
      RETURN
      END
      REAL FUNCTION SDOT (N,SX,INCX,SY,INCY)
C
C      FORMS THE DOT PRODUCT OF TWO VECTORS.
C      USES UNROLLED LOOPS FOR INCREMENTS EQUAL TO ONE.
C      JACK DONGARRA, LINPACK, 3/11/78.
C
      REAL SX(1), SY(1), STEMP
      INTEGER I, INCX, INCY, IX, IY, M, MP1, N
C
      STEMP=0.0E0
      SDOT=0.0E0
      IF (N.LE.0) RETURN
      IF (INCX.EQ.1.AND.INCY.EQ.1) GO TO 20
C
      CODE FOR UNEQUAL INCREMENTS OR EQUAL INCREMENTS
      NOT EQUAL TO 1
C
      IX=1
      IY=1
      IF (INCX.LT.0) IX=(-N+1)*INCX+1
      IF (INCY.LT.0) IY=(-N+1)*INCY+1
      DO 10 I=1,N
      STEMP=STEMP+SX(IX)*SY(IY)
      IX=IX+INCX
      IY=IY+INCY
10  CONTINUE
      SDOT=STEMP
      RETURN
C
      CODE FOR BOTH INCREMENTS EQUAL TO 1
C
      CLEAN-UP LOOP
C
20  M=MOD(N,5)
      IF (M.EQ.0) GO TO 40
      DO 30 I=1,M
      STEMP=STEMP+SX(I)*SY(I)
30  CONTINUE
      IF (N.LT.5) GO TO 60
40  MP1=M+1
      DO 50 I=MP1,N,5
      STEMP=STEMP+SX(I)*SY(I)+SX(I+1)*SY(I+1)+SX(I+2)*SY(I+2)+SX(I+3)*SY
1  (I+3)+SX(I+4)*SY(I+4)
50  CONTINUE
60  SDOT=STEMP
      RETURN
      END
      SUBROUTINE SSCAL (N,SA,SX,INCX)
C
C      SCALES A VECTOR BY A CONSTANT.
C      USES UNROLLED LOOPS FOR INCREMENT EQUAL TO 1.
C      JACK DONGARRA, LINPACK, 3/11/78.
C
      REAL SA, SX(1)
      INTEGER I, INCX, M, MP1, N, NINCX
C
      IF (N.LE.0) RETURN
      IF (INCX.EQ.1) GO TO 20
C
      CODE FOR INCREMENT NOT EQUAL TO 1

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      NINCX=N*INCX
      DO 10 I=1,NINCX,INCX
      SX(I)=SA*SX(I)
10  CONTINUE
      RETURN

C
C      CODE FOR INCREMENT EQUAL TO 1
C
C      CLEAN-UP LOOP
C
20  M=MOD(N,5)
      IF (M.EQ.0) GO TO 40
      DO 30 I=1,M
      SX(I)=SA*SX(I)
30  CONTINUE
      IF (N.LT.5) RETURN
40  MP1=M+1
      DO 50 I=MP1,N,5
      SX(I)=SA*SX(I)
      SX(I+1)=SA*SX(I+1)
      SX(I+2)=SA*SX(I+2)
      SX(I+3)=SA*SX(I+3)
      SX(I+4)=SA*SX(I+4)
50  CONTINUE
      RETURN
      END
      SUBROUTINE SSWAP (N,SX,INCX,SY,INCY)

C
C      INTERCHANGES TWO VECTORS.
C      USES UNROLLED LOOPS FOR INCREMENTS EQUAL TO 1.
C      JACK DONGARRA, LINPACK, 3/11/78.
C
      REAL SX(1), SY(1), STEMP
      INTEGER I, INCX, INCY, IX, IY, M, MP1, N

C
      IF (N.LE.0) RETURN
      IF (INCX.EQ.1.AND.INCY.EQ.1) GO TO 20

C
C      CODE FOR UNEQUAL INCREMENTS OR EQUAL INCREMENTS NOT EQUAL
C      TO 1
C
      IX=1
      IY=1
      IF (INCX.LT.0) IX=(-N+1)*INCX+1
      IF (INCY.LT.0) IY=(-N+1)*INCY+1
      DO 10 I=1,N
      STEMP=SX(IX)
      SX(IX)=SY(IY)
      SY(IY)=STEMP
      IX=IX+INCX
      IY=IY+INCY
10  CONTINUE
      RETURN

C
C      CODE FOR BOTH INCREMENTS EQUAL TO 1
C
C      CLEAN-UP LOOP
C
20  M=MOD(N,3)
      IF (M.EQ.0) GO TO 40
      DO 30 I=1,M
      STEMP=SX(I)
      SX(I)=SY(I)
      SY(I)=STEMP
30  CONTINUE
      IF (N.LT.3) RETURN
40  MP1=M+1
      DO 50 I=MP1,N,3
      STEMP=SX(I)
      SX(I)=SY(I)
      SY(I)=STEMP

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50

DASH TEST PROBLEM (with Output)

Problem input:

	1	0										
A			1	0	0	0	0	0	0	0	8.0225E-07	
B			2	1	0	0	0	0	0	0	1.6045E-06	
	24	1	2		2	4	3	1				
0.0					5.0			10.0				
223			0.0				5.03					
108				1108			2108					
									33			
	1000.0				1000.0			1000.0			1000.0	3
	0.0				2.0			3.0			5.0	3
	5.426E-06				0.0			0.0			2.713E-063	
104	0.0			3								
	1.266E-05				0.0			0.0			6.330E-063	
104	0.0			3								
	1.808E-06				0.0			0.0			9.042E-073	
104				0.03								
	1.000E+10				5.000E+093							
102	0.0			3								
148	0.0			3								
148	0.0			3								

Problem output:

DECAY CHAINS AND NUCLIDE RELATED DATA

NUCLIDE	ID	DECAY PARENT		CAPTURE PARENT		N-2N	N-ALPHA	N-P	DECAY CONSTANT
		1	2	1	2				
A	1	0	0	0	0	0	0	0	8.02250E-07
B	2	1	0	0	0	0	0	0	1.60450E-06

THE GEOMETRY FOR THIS PROBLEM IS A SLAB.
 THE LEFT BOUNDARY CONDITION IS = 2
 THE RIGHT BOUNDARY CONDITION IS = 2

RADII	25							
0.	.20833E+00	.41667E+00	.62500E+00	.83333E+00	.10417E+01			
.12500E+01	.14583E+01	.16667E+01	.18750E+01	.20833E+01	.22917E+01			
.25000E+01	.27083E+01	.29167E+01	.31250E+01	.33333E+01	.35417E+01			
.37500E+01	.39583E+01	.41667E+01	.43750E+01	.45833E+01	.47917E+01			
.50000E+01								

MATERIALS	24							
1	1	1	1	1	1	1	1	1
2	2	2	2	2	2	2	2	2
3	3	3	3	3	3	3	3	3

TEMPERATURES	4							
.10000E+04	.10000E+04	.10000E+04	.10000E+04					

TEMP RADII	4							
0.	.20000E+01	.30000E+01	.50000E+01					

DIJ-0	4							
.54260E-05	0.	0.	.27130E-05					

AIJ	4							
0.	0.	0.	0.					

DIJ-0	4							
.12660E-04	0.	0.	.63300E-05					

AIJ	4							
0.	0.	0.	0.					

DIJ-0	4							
.18080E-05	0.	0.	.90420E-06					

AIJ	4							
0.	0.	0.	0.					

LEFT CONCEN 2
.10000E+11 .50000E+10

RIGHT CONCEN 2
0. 0.

INITIAL CONC 48
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.

SOURCE INPUT 48
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0.

2*****
2 * * * * *
2 1 * 1 * 1 * 1 * 1 * 1 *
2 * * * * *
2*****
0.000 .208 .417 .625 .833 1.042 1.250 1.458

* * * * *
* 2 * 2 * 2 * 2 * 2 * 2 *
* * * * *

1.667 1.875 2.083 2.292 2.500 2.708 2.917 3.125

*****2
* * * * *2
* 3 * 3 * 3 * 3 * 3 * 3 *2
* * * * *2
*****2
3.333 3.542 3.750 3.958 4.167 4.375 4.583 4.792 5.000

RBAR

.10417E+00	.31250E+00	.52083E+00	.72917E+00	.93750E+00	.11458E+01
.13542E+01	.15625E+01	.17708E+01	.19792E+01	.21875E+01	.23958E+01
.26042E+01	.28125E+01	.30208E+01	.32292E+01	.34375E+01	.36458E+01
.38542E+01	.40625E+01	.42708E+01	.44792E+01	.46875E+01	.48958E+01

MESH TEMPERATURES

.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04
.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04
.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04
.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04	.10000E+04

		CELL CONCENTRATIONS AT 0. (CONCENTRATIONS IN ATOMS/CC)				DAYS
ISOTOPE	LEFT BOUNDARY	CELL 1	CELL 2	CELL 3	CELL 4	
A	1.00000E+10	0.	0.	0.	0.	
B	5.00000E+09	0.	0.	0.	0.	
ISOTOPE	CELL 5	CELL 6	CELL 7	CELL 8	CELL 9	
A	0.	0.	0.	0.	0.	
B	0.	0.	0.	0.	0.	
ISOTOPE	CELL 10	CELL 11	CELL 12	CELL 13	CELL 14	
A	0.	0.	0.	0.	0.	
B	0.	0.	0.	0.	0.	
ISOTOPE	CELL 15	CELL 16	CELL 17	CELL 18	CELL 19	
A	0.	0.	0.	0.	0.	
B	0.	0.	0.	0.	0.	
ISOTOPE	CELL 20	CELL 21	CELL 22	CELL 23	CELL 24	
A	0.	0.	0.	0.	0.	
B	0.	0.	0.	0.	0.	
ISOTOPE	RIGHT BOUNDARY					
A	0.					
B	0.					

NO. OF ATOMS = 0.

		CELL CONCENTRATIONS AT 2.00000E+00 DAYS (CONCENTRATIONS IN ATOMS/CC)			
ISOTOPE	LEFT BOUNDARY	CELL 1	CELL 2	CELL 3	CELL 4
A	1.00000E+10	9.29795E+09	7.96461E+09	6.71483E+09	5.55947E+09
B	5.00000E+09	4.58334E+09	3.76847E+09	3.00574E+09	2.32140E+09
ISOTOPE	CELL 5	CELL 6	CELL 7	CELL 8	CELL 9
A	4.50618E+09	3.55868E+09	2.71648E+09	1.97513E+09	1.51218E+09
B	1.73153E+09	1.24114E+09	8.45226E+08	5.31159E+08	3.53010E+08
ISOTOPE	CELL 10	CELL 11	CELL 12	CELL 13	CELL 14
A	1.27135E+09	1.06544E+09	8.92274E+08	7.49647E+08	6.35396E+08
B	2.68117E+08	2.01869E+08	1.51143E+08	1.13164E+08	8.55697E+07
ISOTOPE	CELL 15	CELL 16	CELL 17	CELL 18	CELL 19
A	5.47490E+08	4.84093E+08	3.22124E+08	1.62196E+08	7.73686E+07
B	6.64433E+07	5.43220E+07	2.97671E+07	1.18012E+07	4.56331E+06
ISOTOPE	CELL 20	CELL 21	CELL 22	CELL 23	CELL 24
A	3.49964E+07	1.50226E+07	6.10502E+06	2.28116E+06	5.71744E+05
B	1.72444E+06	6.35629E+05	2.27180E+05	7.65217E+04	1.79805E+04
ISOTOPE	RIGHT BOUNDARY				
A	0.				
B	0.				

NO. OF ATOMS = 1.446715010794452E+10

CELL CONCENTRATIONS AT 4.00000E+00 DAYS
(CONCENTRATIONS IN ATOMS/CC)

LEFT BOUNDARY		CELL 1	CELL 2	CELL 3	CELL 4
ISOTOPE A	1.00000E+10	9.42778E+09	8.34731E+09	7.33075E+09	6.37816E+09
ISOTOPE B	5.00000E+09	4.70421E+09	4.11867E+09	3.55015E+09	3.00805E+09
		CELL 5	CELL 6	CELL 7	CELL 8
ISOTOPE A	5.48958E+09	4.66485E+09	3.90357E+09	3.20501E+09	2.75003E+09
ISOTOPE B	2.49978E+09	2.03055E+09	1.60328E+09	1.21885E+09	9.74220E+08
		CELL 10	CELL 11	CELL 12	CELL 13
ISOTOPE A	2.50298E+09	2.28157E+09	2.08539E+09	1.91402E+09	1.76697E+09
ISOTOPE B	8.44765E+08	7.32089E+08	6.35525E+08	5.54337E+08	4.87757E+08
		CELL 15	CELL 16	CELL 17	CELL 18
ISOTOPE A	1.64372E+09	1.54371E+09	1.23427E+09	8.34885E+08	5.49025E+08
ISOTOPE B	4.35023E+08	3.95409E+08	2.86757E+08	1.67269E+08	9.49803E+07
		CELL 20	CELL 21	CELL 22	CELL 23
ISOTOPE A	3.50278E+08	2.15566E+08	1.25588E+08	6.46189E+07	1.98144E+07
ISOTOPE B	5.26285E+07	2.84312E+07	1.47910E+07	6.97871E+06	2.03949E+06
RIGHT BOUNDARY					
ISOTOPE A	0.				
ISOTOPE B	0.				

NO. OF ATOMS = 2.022416554881128E+10

CELL CONCENTRATIONS AT 6.00000E+00 DAYS
(CONCENTRATIONS IN ATOMS/CC)

LEFT BOUNDARY		CELL 1	CELL 2	CELL 3	CELL 4
ISOTOPE A	1.00000E+10	9.48391E+09	8.51455E+09	7.60570E+09	6.75534E+09
ISOTOPE B	5.00000E+09	4.75291E+09	4.26232E+09	3.78171E+09	3.31659E+09
		CELL 5	CELL 6	CELL 7	CELL 8
ISOTOPE A	5.96166E+09	5.22303E+09	4.53792E+09	3.90483E+09	3.48873E+09
ISOTOPE B	2.87162E+09	2.45057E+09	2.05634E+09	1.69104E+09	1.45176E+09
		CELL 10	CELL 11	CELL 12	CELL 13
ISOTOPE A	3.26026E+09	3.05272E+09	2.86580E+09	2.69920E+09	2.55260E+09
ISOTOPE B	1.32141E+09	1.20432E+09	1.10046E+09	1.00972E+09	9.31905E+08
		CELL 15	CELL 16	CELL 17	CELL 18
ISOTOPE A	2.42566E+09	2.31805E+09	1.96336E+09	1.46521E+09	1.07141E+09
ISOTOPE B	8.66799E+08	8.14129E+08	6.51964E+08	4.43919E+08	2.95522E+08
		CELL 20	CELL 21	CELL 22	CELL 23
ISOTOPE A	7.63947E+08	5.25345E+08	3.38961E+08	1.89046E+08	6.06463E+07
ISOTOPE B	1.92098E+08	1.21154E+08	7.25530E+07	3.82733E+07	1.19153E+07
RIGHT BOUNDARY					
ISOTOPE A	0.				
ISOTOPE B	0.				

NO. OF ATOMS = 2.432060341188196E+10

CELL CONCENTRATIONS AT 8.00000E+00 DAYS
(CONCENTRATIONS IN ATOMS/CC)

LEFT						
ISOTOPE	BOUNDARY	CELL 1	CELL 2	CELL 3	CELL 4	
A	1.00000E+10	9.51807E+09	8.61655E+09	7.77410E+09	6.98778E+09	
B	5.00000E+09	4.78213E+09	4.34920E+09	3.92396E+09	3.51057E+09	
ISOTOPE	CELL 5	CELL 6	CELL 7	CELL 8	CELL 9	
A	6.25491E+09	5.57308E+09	4.94004E+09	4.35369E+09	3.96681E+09	
B	3.11256E+09	2.73290E+09	2.37399E+09	2.03777E+09	1.81489E+09	
ISOTOPE	CELL 10	CELL 11	CELL 12	CELL 13	CELL 14	
A	3.75326E+09	3.55795E+09	3.38056E+09	3.22076E+09	3.07825E+09	
B	1.69186E+09	1.57968E+09	1.47843E+09	1.38814E+09	1.30877E+09	
ISOTOPE	CELL 15	CELL 16	CELL 17	CELL 18	CELL 19	
A	2.95271E+09	2.84382E+09	2.47363E+09	1.93189E+09	1.48164E+09	
B	1.24026E+09	1.18248E+09	9.93692E+08	7.32038E+08	5.28611E+08	
ISOTOPE	CELL 20	CELL 21	CELL 22	CELL 23	CELL 24	
A	1.10836E+09	7.97676E+08	5.35402E+08	3.07533E+08	1.00231E+08	
B	3.72667E+08	2.53864E+08	1.62631E+08	9.02763E+07	2.88938E+07	

ISOTOPE RIGHT
A BOUNDARY
B 0.
0.

NO. OF ATOMS = 2.732894842037402E+10

CELL CONCENTRATIONS AT 1.00000E+01 DAYS
(CONCENTRATIONS IN ATOMS/CC)

LEFT						
ISOTOPE	BOUNDARY	CELL 1	CELL 2	CELL 3	CELL 4	
A	1.00000E+10	9.54047E+09	8.68348E+09	7.88473E+09	7.14074E+09	
B	5.00000E+09	4.80266E+09	4.41044E+09	4.02483E+09	3.64930E+09	
ISOTOPE	CELL 5	CELL 6	CELL 7	CELL 8	CELL 9	
A	6.44833E+09	5.80458E+09	5.20681E+09	4.65250E+09	4.28595E+09	
B	3.28681E+09	2.93978E+09	2.61023E+09	2.29977E+09	2.09257E+09	
ISOTOPE	CELL 10	CELL 11	CELL 12	CELL 13	CELL 14	
A	4.08296E+09	3.89654E+09	3.72633E+09	3.57197E+09	3.43314E+09	
B	1.97730E+09	1.87121E+09	1.77439E+09	1.68690E+09	1.60874E+09	
ISOTOPE	CELL 15	CELL 16	CELL 17	CELL 18	CELL 19	
A	3.30950E+09	3.20077E+09	2.82418E+09	2.25954E+09	1.77606E+09	
B	1.53988E+09	1.48025E+09	1.27831E+09	9.85283E+08	7.45147E+08	
ISOTOPE	CELL 20	CELL 21	CELL 22	CELL 23	CELL 24	
A	1.36081E+09	1.00111E+09	6.84443E+08	3.98429E+08	1.30772E+08	
B	5.49730E+08	3.90608E+08	2.59383E+08	1.47840E+08	4.79880E+07	

ISOTOPE RIGHT
A BOUNDARY
B 0.
0.

NO. OF ATOMS = 2.953406154721277E+10

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